

Package ‘flint’

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Title Fast Library for Number Theory

Description An R interface to 'FLINT' <<https://flintlib.org/>>, a C library for number theory. 'FLINT' extends GNU 'MPFR' <<https://www.mpfr.org/>> and GNU 'MP' <<https://gmplib.org/>> with support for operations on standard rings (the integers, the integers modulo n, finite fields, the rational, p-adic, real, and complex numbers) as well as matrices and polynomials over rings. 'FLINT' implements midpoint-radius interval arithmetic, also known as ball arithmetic, in the real and complex numbers, enabling computation in arbitrary precision with rigorous propagation of rounding and other errors; see Johansson (2017) <[doi:10.1109/TC.2017.2690633](https://doi.org/10.1109/TC.2017.2690633)>. Finally, 'FLINT' provides ball arithmetic implementations of many special mathematical functions, with high coverage of reference works such as the NIST Digital Library of Mathematical Functions <<https://dlmf.nist.gov/>>. The R interface defines S4 classes, generic functions, and methods for representation and basic operations as well as plain R functions mirroring and vectorizing entry points in the C library.

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URL <https://github.com/jaganmn/flint>

BugReports <https://github.com/jaganmn/flint/issues>

Depends R (>= 4.3), methods

Imports stats

Enhances Rmpfr, gmp

SystemRequirements flint (>= 3), mpfr (>= 3.1), gmp

SystemRequirementsNote purely informational as we use configure tests

NeedsCompilation yes

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flint-package	R Package flint
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Description

An R interface to FLINT, a C library for number theory.

Usage

```

flintABI()
flintBits(object)
flintBitsAccurate(object)
flintClass(object)
flintLength(object, exact = TRUE)
flintPrec(prec = NULL)
flintRnd(rnd = NULL)
flintSize(object)
flintTriple(object)
flintVersion()

.initForeign(which = c("Rmpfr", "gmp"),
             where = topenv(parent.frame()))

```

Arguments

object	an R object, typically inheriting from virtual class flint .
exact	a logical indicating if the length should be represented exactly as an object of class ulong .
prec	a new default value for the precision of inexact floating-point operations, if non-NULL. The value should be a positive integer indicating a number of bits.
rnd	a new default value for the rounding mode of inexact floating-point operations, if non-NULL. The value should be a character string indicating a rounding mode for signed floating-point types. Valid characters are '[Uu]' (towards positive infinity), '[Dd]' (towards negative infinity), '[Zz]' (towards zero), '[Aa]' (away from zero), and '[Nn]' (to nearest, with precedence to even significands).
which	a character vector listing package names.
where	an environment for storing methods, by default the flint namespace.

Details

To report a bug or request a feature, use [bug.report](#)(package = "flint").

To render the change log, use [news](#)(package = "flint").

To render the index, use [help](#)(package = "flint")

To render a list of help topics for S4 classes, use [help.search](#)(package = "flint", keyword = "classes")

To render a list of help topics for special mathematical functions, use [help.search](#)(package = "flint", keyword = "math")

Value

flintABI returns the size in bits of C type long int, either 32 or 64. The value is determined when package **flint** is configured. It is checked at configure time and at load time that linked C libraries were configured for the same ABI.

`flintClass` returns a character string naming the direct nonvirtual subclass of virtual class `flint` from which object inherits. (Hence a possible value is `"ulong"` but not the name of any subclass of `ulong`.) If object does not inherit from virtual class `flint`, then the return value is `NA_character_`.

`flintLength` returns a representation of the length of object. If `exact = TRUE`, then the return value is an object of class `ulong` representing the length exactly. Otherwise, if the length is less than or equal to `.Machine[["integer.max"]]`, then the return value is a traditional integer vector representing the length exactly. Otherwise, the return value is a traditional double vector representing the length exactly if and only if $n \leq 2^d - 1$ or $2^{d+p} \leq n < 2^{d+p+1}$ and n is divisible by 2^{p+1} , where n is the length, d is `.Machine[["double.digits"]]`, and $p = 0, 1, \dots$. Lengths not exactly representable in double precision are rounded to the next representable number in the direction of zero. Return values not representing the length exactly have an attribute `off` preserving the rounding error (an integer in $1, \dots, 2^p$). If object does not inherit from virtual class `flint`, then the return value is `NA_integer_`.

`flintPrec` returns the previous default precision.

`flintRnd` returns the previous default rounding mode.

`flintSize` returns an upper bound for the number of bytes used by object, as an object of class `object_size` (following function `object.size` in package `utils`). If no members of the recursive structure share memory, then the upper bound is exact. Recursion starts at the address stored by the R object, not at the address of the object itself. A corollary is that `flintSize(object)` is zero for object of length zero. Another corollary is that the bytes counted by `flintSize` and the bytes counted by `object.size` are disjoint. If object does not inherit from virtual class `flint`, then the return value is `NA_real_` (beneath the class).

`flintTriple` returns a character vector of length 3 containing the class of object, the length of object, and the address stored by object. If object does not inherit from virtual class `flint`, then all of the elements are `NA`.

`flintVersion` returns a named list of numeric versions with elements:

<code>package</code>	the R package version.
<code>flint.h</code>	the FLINT header version.
<code>libflint</code>	the FLINT library version.
<code>mpfr.h</code>	the GNU MPFR header version.
<code>libmpfr</code>	the GNU MPFR library version.
<code>gmp.h</code>	the GNU MP header version.
<code>libgmp</code>	the GNU MP library version.

Header versions are determined at compile time. Library versions are determined at compile time (static linking) or at load time (dynamic linking).

`.initForeign` defines methods for `coerce` enabling coercion between classes in `flint` and analogous classes in the packages named by which. Packages are loaded before methods are defined to ensure that `setAs` is able to find class definitions. A corollary is that an error is signaled if packages are not installed in the library search path. Supported signatures:

```
which="Rmpfr":
  from="mpfr", to="arf"
```

```

    from="arf", to="mpfr"
  which="gmp":
    from="bigz", to="fmpz"
    from="fmpz", to="bigz"
    from="bigq", to="fmpq"
    from="fmpq", to="bigq"

```

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References

FLINT Team (2025). FLINT: Fast Library for Number Theory. <https://flintlib.org/>

Examples

```

flintABI()

oprec <- flintPrec()
nprec <- 100L
stopifnot(identical(flintPrec(nprec), oprec),
           identical(flintPrec(), nprec),
           identical(flintPrec(oprec), nprec),
           identical(flintPrec(), oprec))

ornd <- flintRnd()
nrnd <- "Z"
stopifnot(identical(flintRnd(nrnd), ornd),
           identical(flintRnd(), nrnd),
           identical(flintRnd(ornd), nrnd),
           identical(flintRnd(), ornd))

flintVersion()

```

acb-class

Arbitrary Precision Floating-Point Complex Numbers with Error Bounds

Description

Class `acb` extends virtual class `flint`. It represents vectors of complex numbers with error bounds on the real and imaginary parts. Elements are specified by two pairs of mixed format floating-point numbers: an `arb` real part and an `arb` imaginary part, each specified by an `arf` midpoint and a `mag` radius.

Usage

```
## Class generator functions
```

```
acb(x = 0i, length = 0L, names = NULL, real = 0, imag = 0)
```

```
acb.array(x = 0i, dim = length(x), dimnames = NULL, real = 0, imag = 0)
```

Arguments

<code>x</code>	an atomic or flint vector containing data for conversion to <code>acb</code> .
<code>length</code>	a numeric vector of length one giving the length of the return value. If that exceeds the length of <code>x</code> , then <code>x</code> is recycled. Non-integer values are rounded in the direction of zero.
<code>names</code>	the names slot of the return value, either <code>NULL</code> or a character vector of equal length. Non-character names are coerced to character.
<code>dim</code>	the dim slot of the return value, an integer vector of nonzero length. If the product exceeds the length of <code>x</code> , then <code>x</code> is recycled. Non-integer numeric <code>dim</code> are coerced to integer.
<code>dimnames</code>	the dimnames slot of the return value, either <code>NULL</code> or a list of length equal to the length of <code>dim</code> . The components are either <code>NULL</code> or character vectors of length given by <code>dim</code> . Non-character vector components of <code>dimnames</code> are coerced to character.
<code>real, imag</code>	atomic or flint vectors containing data for conversion to arb . Use these for initialization “by parts” (real and imaginary).

Details

The class generator function has six distinct usages:

```
acb()
acb(length=)
acb(x)
acb(x, length=)
acb(real=, imag=)
acb(real=, imag=, length=)
```

The first usage generates an empty vector. The second usage generates a zero vector of the indicated length. The third usage converts `x`, preserving dimensions, dimension names, and names. The fourth usage converts `x`, recycling its elements to the indicated length and discarding its dimensions, dimension names, and names. The fifth and sixth usages, in which either of `real` and `imag` can be missing, use [arb](#)(`real`) and [arb](#)(`imag`) to separately initialize the real and imaginary parts of the `acb` return value.

Attempts to recycle `real`, `imag`, or `x` of length zero to nonzero length are an error.

Usage of `acb.array` is modelled after [array](#).

Value

An `acb` vector, possibly an array; see ‘Details’.

Conversion

Real numbers and real and imaginary parts of complex numbers are rounded according to the default precision and rounding mode set by `flintPrec` and `flintRnd`. Ball midpoints are the numbers obtained by rounding. Ball radii are upper bounds on the absolute errors incurred by rounding.

Character strings are scanned first for a real part then for an imaginary part. They can use any of three formats: "*sa*", "*tbi*", and "*satbi*", where, recursively, each of *a* and *b* have the format "*(km+/-r)*", defining a ball for each of the real and imaginary parts. *k* and *m* define the sign and absolute value of the signed ball midpoints, and *r* defines the unsigned ball radii. *k* can be empty if the ball midpoint is NaN or non-negative. *s* and *t* are unary or binary plus or minus to be reconciled with *k*; they are optional except in the third format where *t* is mandatory.

The sequences *km* and *r* are converted using function `mpfr_strtofr` from the GNU MPFR library with argument base set to 0 and argument `rnd` set according to the default rounding mode (for the midpoint, whereas the radius is always rounded towards Inf); see <https://www.mpfr.org/mpfr-current/mpfr.html#Assignment-Functions>.

Slots

.xData, dim, dimnames, names inherited from virtual class `flint`.

Methods

Due to constraints imposed by generic functions, methods typically do *not* provide a formal argument `prec` allowing for a precision to be indicated in the function call. Such methods use the current default precision set by `flintPrec`.

```
! signature(x = "acb"):
  equivalent to (but faster than) x == 0.

%*%, crossprod, tcrossprod signature(x = "acb", y = "acb"):
  signature(x = "acb", y = "ANY"):
  signature(x = "ANY", y = "acb"):
  matrix products. The "other" operand must be atomic or inherit from virtual class flint.
  crossprod and tcrossprod behave as if y = x when y is missing or NULL. Operands are
  promoted as necessary and must be conformable (have compatible dimensions). Non-array
  operands of length k are handled as 1-by-k or k-by-1 matrices depending on the call.

+ signature(e1 = "acb", e2 = "missing"):
  returns a copy of the argument.

- signature(e1 = "acb", e2 = "missing"):
  returns the negation of the argument.

Complex signature(z = "acb"):
  mathematical functions of one argument; see S4groupGeneric.

Math signature(x = "acb"):
  mathematical functions of one argument; see S4groupGeneric. Member functions floor,
  ceiling, trunc, cummin, cummax are not implemented.

Math2 signature(x = "acb"):
  decimal rounding according to a second argument digits; see S4groupGeneric. There are
  just two member member functions: round, signif.
```

Ops signature(e1 = "acb", e2 = "acb"):
signature(e1 = "acb", e2 = "ANY"):
signature(e1 = "ANY", e2 = "acb"):
binary arithmetic, comparison, and logical operators; see [S4groupGeneric](#). The “other” operand must be atomic or inherit from virtual class [flint](#). Operands are promoted as necessary. Array operands must be conformable (have identical dimensions). Non-array operands are recycled.

Summary signature(x = "acb"):
univariate summary statistics; see [S4groupGeneric](#). The return value is a logical vector of length 1 (any, all) or an acb vector of length 1 or 2 (sum, prod). Member functions min, max, range are not implemented.

anyNA signature(x = "acb"):
returns TRUE if any element of x has real or imaginary part with midpoint NaN, FALSE otherwise.

as.vector signature(x = "acb"):
returns as.vector(y, mode), where y is a complex vector containing the result of converting the midpoints of the real and imaginary parts of x to the range of double, rounding if the value is not exactly representable in double precision. The rounding mode is to the nearest representable number (with precedence to even significands in case of ties), unless a midpoint exceeds .Machine[["double.xmax"]] in absolute value, in which case -Inf or Inf is introduced with a warning. Coercion to types "character", "symbol" (synonym "name"), "pairlist", "list", and "expression", which are not “number-like”, is handled specially. See also [asVector](#).

backsolve signature(r = "acb", x = "acb"):
signature(r = "acb", x = "ANY"):
signature(r = "ANY", x = "acb"):
solution of the triangular system $\text{op2}(\text{op1}(r)) \%*\% y = x$, where `op1=ifelse(upper.tri, triu, tril)` and `op2=ifelse(transpose, t, identity)` and `upper.tri` and `transpose` are optional logical arguments with default values TRUE and FALSE, respectively. The “other” operand must be atomic or inherit from virtual class [flint](#). If x is missing, then the return value is the inverse of `op2(op1(r))`, as if x were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array x are handled as `length(x)-by-1` matrices.

chol signature(x = "acb"):
returns the upper triangular Cholesky factor of the positive definite matrix whose upper triangular part is the upper triangular part of x (discarding imaginary parts of diagonal entries).

chol2inv signature(x = "acb"):
returns the inverse of the positive definite matrix whose upper triangular Cholesky factor is the upper triangular part of x (discarding imaginary parts of diagonal entries).

coerce signature(from = "ANY", to = "acb"):
returns the value of acb(from).

colSums, colMeans signature(x = "acb"):
returns an acb vector or array containing the column sums or means of x, defined as sums or means over dimensions 1:dims.

det signature(x = "arb"):
returns the determinant of x as an acb vector of length 1.

`determinant signature(x = "acf"):`
 returns a list with components modulus and argument specifying the determinant of `x`, following the **base** function (except for the use of argument instead of sign), hence [determinant](#).

`format signature(x = "acb"):`
 returns a character vector suitable for printing, using string format `"(m +/- r)+(m +/- r)i"` and scientific format for each `m` and `r`. Optional arguments control the output; see [format-methods](#).

`is.finite signature(x = "acb"):`
 returns a logical vector indicating which elements of `x` do not have real or imaginary part with midpoint NaN, `-Inf`, or `Inf` or radius `Inf`.

`is.infinite signature(x = "acb"):`
 returns a logical vector indicating which elements of `x` have real or imaginary part with midpoint `-Inf` or `Inf` or radius `Inf`.

`is.na, is.nan signature(x = "acb"):`
 returns a logical vector indicating which elements of `x` have real or imaginary part with midpoint NaN.

`is.unsorted signature(x = "acb"):`
 signals an error indicating that `<=` is not a total order on the range of `arb`; see `xtfrm` below.

`log signature(x = "acb"):`
 returns the logarithm of the argument. The natural logarithm is computed by default (when optional argument `base` is unset).

`mean signature(x = "acb"):`
 returns the arithmetic mean.

`rowSums, rowMeans signature(x = "acb"):`
 returns an `acb` vector or array containing the row sums or means of `x`, defined as sums or means over dimensions `(dims+1):length(dim(x))`.

`solve signature(a = "acb", b = "acb"):`
`signature(a = "acb", b = "ANY"):`
`signature(a = "ANY", b = "acb"):`
 solution of the general system `a %*% x = b`. The “other” operand must be atomic or inherit from virtual class [flint](#). If `b` is missing, then the return value is the inverse of `a`, as if `b` were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array `b` are handled as `length(b)-by-1` matrices.

`xtfrm signature(x = "acb"):`
 signals an error indicating that `<=` is not a total order on the range of `arb`: `a <= b || b <= a` is not TRUE for all finite `a` and `b` of class `arb`. Thus, direct sorting of `acb`, which is based on `arb`, is not supported. Users wanting to order the *midpoints* of the real and imaginary parts should operate on `Mid(Real(x))` and `Mid(Imag(x))`.

References

The FLINT documentation of the underlying C type: <https://flintlib.org/doc/acb.html>

Johansson, F. (2017). Arb: efficient arbitrary-precision midpoint-radius interval arithmetic. *IEEE Transactions on Computers*, 66(8), 1281-1292. doi:10.1109/TC.2017.2690633

See Also

Virtual class `flint`. Generic functions `Real` and `Imag` and their replacement forms for getting and setting real and imaginary parts.

Examples

```
showClass("acb")
showMethods(classes = "acb")
```

 acf-class

Arbitrary Precision Floating-Point Complex Numbers

Description

Class `acf` extends virtual class `flint`. It represents vectors of arbitrary precision floating-point complex numbers. Elements have real and imaginary parts, each with arbitrary precision significand and exponent. The underlying C type can represent NaN, -Inf, and Inf real and imaginary parts.

Note that package `stats` exports a function `acf`, referring to autocovariance and autocorrelation functions of time series. It returns objects of *informal* S3 class `acf`, for which a small number of *informal* S3 methods are registered. The *formal* S4 class and methods documented here are unrelated.

The class generator functions are named `ACF` and `ACF.array` instead of `acf` and `acf.array` because an exported function named `acf` would mask the function in package `stats`.

Usage

```
## Class generator functions
```

```
ACF(x = 0i, length = 0L, names = NULL, real = 0, imag = 0)
```

```
ACF.array(x = 0i, dim = length(x), dimnames = NULL, real = 0, imag = 0)
```

Arguments

<code>x</code>	an atomic or <code>flint</code> vector containing data for conversion to <code>acf</code> .
<code>length</code>	a numeric vector of length one giving the length of the return value. If that exceeds the length of <code>x</code> , then <code>x</code> is recycled. Non-integer values are rounded in the direction of zero.
<code>names</code>	the names slot of the return value, either <code>NULL</code> or a character vector of equal length. Non-character names are coerced to character.
<code>dim</code>	the dim slot of the return value, an integer vector of nonzero length. If the product exceeds the length of <code>x</code> , then <code>x</code> is recycled. Non-integer numeric <code>dim</code> are coerced to integer.

dimnames	the dimnames slot of the return value, either NULL or a list of length equal to the length of dim. The components are either NULL or character vectors of length given by dim. Non-character vector components of dimnames are coerced to character.
real, imag	atomic or flint vectors containing data for conversion to arf . Use these instead of x for initialization “by parts” (real and imaginary).

Details

The class generator function has six distinct usages:

```
acf.()
acf.(length=)
acf.(x)
acf.(x, length=)
acf.(real=, imag=)
acf.(real=, imag=, length=)
```

The first usage generates an empty vector. The second usage generates a zero vector of the indicated length. The third usage converts x, preserving dimensions, dimension names, and names. The fourth usage converts x, recycling its elements to the indicated length and discarding its dimensions, dimension names, and names. The fifth and sixth usages, in which either of real and imag can be missing, use [arf](#)(real) and [arf](#)(imag) to separately initialize the real and imaginary parts of the acf return value.

Attempts to recycle real, imag, or x of length zero to nonzero length are an error.

Usage of acf.array is modelled after [array](#).

Value

An acf vector, possibly an array; see ‘Details’.

Conversion

Real numbers and real and imaginary parts of complex numbers are rounded according to the default precision and rounding mode set by [flintPrec](#) and [flintRnd](#).

Character strings are scanned first for a real part then for an imaginary part. They can use any of three formats: “sa”, “tbi”, and “satbi”, where s and a define the sign and absolute value of the real part and t and b define the sign and absolute value of the imaginary part. s can be empty if the real part is NaN or non-negative. t can be empty if the imaginary part is NaN or non-negative, but only in the second format.

The sequences sa and tb are converted using function mpfr_strtobr from the GNU MPFR library with argument base set to 0 and argument rnd set according to the default rounding mode; see <https://www.mpfr.org/mpfr-current/mpfr.html#Assignment-Functions>.

Slots

.xData, dim, dimnames, names inherited from virtual class [flint](#).

Methods

Due to constraints imposed by generic functions, methods typically do *not* provide a formal argument `prec` allowing for a precision to be indicated in the function call. Such methods use the current default precision set by `flintPrec`.

```
! signature(x = "acf"):
    equivalent to (but faster than) x == 0.

%*%, crossprod, tcrossprod signature(x = "acf", y = "acf"):
    signature(x = "acf", y = "ANY"):
    signature(x = "ANY", y = "acf"):
    matrix products. The "other" operand must be atomic or inherit from virtual class flint.
    crossprod and tcrossprod behave as if y = x when y is missing or NULL. Operands are
    promoted as necessary and must be conformable (have compatible dimensions). Non-array
    operands of length k are handled as 1-by-k or k-by-1 matrices depending on the call. The
    return value is approximate insofar that it may not be correctly rounded.

+ signature(e1 = "acf", e2 = "missing"):
    returns a copy of the argument.

- signature(e1 = "acf", e2 = "missing"):
    returns the negation of the argument.

Complex signature(z = "acf"):
    mathematical functions of one argument; see S4groupGeneric.

Math signature(x = "acf"):
    mathematical functions of one argument; see S4groupGeneric. Member functions floor,
    ceiling, trunc, cummin, cummax are not implemented.

Math2 signature(x = "acf"):
    decimal rounding according to a second argument digits; see S4groupGeneric. There are
    just two member member functions: round, signif.

Ops signature(e1 = "acf", e2 = "acf"):
    signature(e1 = "acf", e2 = "ANY"):
    signature(e1 = "ANY", e2 = "acf"):
    binary arithmetic, comparison, and logical operators; see S4groupGeneric. The "other"
    operand must be atomic or inherit from virtual class flint. Operands are promoted as neces-
    sary. Array operands must be conformable (have identical dimensions). Non-array operands
    are recycled.

Summary signature(x = "acf"):
    univariate summary statistics; see S4groupGeneric. The return value is a logical vector of
    length 1 (any, all) or an acf vector of length 1 or 2 (sum, prod). Member functions min, max,
    range are not implemented.

anyNA signature(x = "acf"):
    returns TRUE if any element of x has real or imaginary part NaN, FALSE otherwise.

as.vector signature(x = "acf"):
    returns as.vector(y, mode), where y is a complex vector containing the result of con-
    verting the real and imaginary parts of x to the range of double, rounding if the value is
    not exactly representable in double precision. The rounding mode is to the nearest repre-
    sentable number (with precedence to even significands in case of ties), unless parts exceed
```

.Machine[["double.xmax"]] in absolute value, in which case $-\text{Inf}$ or Inf is introduced with a warning. Coercion to types "character", "symbol" (synonym "name"), "pairlist", "list", and "expression", which are not "number-like", is handled specially. See also [asVector](#).

```
backsolve signature(r = "acf", x = "acf"):
  signature(r = "acf", x = "ANY"):
  signature(r = "ANY", x = "acf"):
  solution of the triangular system  $\text{op2}(\text{op1}(r)) \%*\% y = x$ , where  $\text{op1} = \text{ifelse}(\text{upper.tri}, \text{triu}, \text{tril})$  and  $\text{op2} = \text{ifelse}(\text{transpose}, \text{t}, \text{identity})$  and  $\text{upper.tri}$  and  $\text{transpose}$  are optional logical arguments with default values TRUE and FALSE, respectively. The "other" operand must be atomic or inherit from virtual class flint. If x is missing, then the return value is the inverse of  $\text{op2}(\text{op1}(r))$ , as if x were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array x are handled as  $\text{length}(x)$ -by-1 matrices.
```

```
chol signature(x = "acf"):
  returns the upper triangular Cholesky factor of the positive definite matrix whose upper triangular part is the upper triangular part of x (discarding imaginary parts of diagonal entries).
```

```
chol2inv signature(x = "acf"):
  returns the inverse of the positive definite matrix whose upper triangular Cholesky factor is the upper triangular part of x (discarding imaginary parts of diagonal entries).
```

```
coerce signature(from = "ANY", to = "acf"):
  returns the value of acf.(from).
```

```
colSums, colMeans signature(x = "acf"):
  returns an acf vector or array containing the column sums or means of x, defined as sums or means over dimensions 1:dims.
```

```
det signature(x = "acf"):
  returns the determinant of x as an acf vector of length 1.
```

```
determinant signature(x = "acf"):
  returns a list with components modulus and argument specifying the determinant of x, following the base function (except for the use of argument instead of sign), hence see determinant.
```

```
format signature(x = "acf"):
  returns a character vector suitable for printing, using string format "a+bi" and scientific format for each a and b. Optional arguments control the output; see format-methods.
```

```
is.finite signature(x = "acf"):
  returns a logical vector indicating which elements of x do not have real or imaginary part NaN,  $-\text{Inf}$ , or  $\text{Inf}$ .
```

```
is.infinite signature(x = "acf"):
  returns a logical vector indicating which elements of x have real or imaginary part  $-\text{Inf}$  or  $\text{Inf}$ .
```

```
is.na, is.nan signature(x = "acf"):
  returns a logical vector indicating which elements of x have real or imaginary part NaN.
```

```
is.unsorted signature(x = "acf"):
  returns a logical indicating if x is not sorted in nondecreasing order (increasing order if optional argument strictly is set to TRUE) by real part then by imaginary part.
```

```

mean signature(x = "acf"):
    returns the arithmetic mean.

rowSums, rowMeans signature(x = "acf"):
    returns an acf vector or array containing the row sums or means of x, defined as sums or
    means over dimensions (dims+1):length(dim(x)).

solve signature(a = "acf", b = "acf"):
    signature(a = "acf", b = "ANY"):
    signature(a = "ANY", b = "acf"):
    solution of the general system  $a \%* \% x = b$ . The “other” operand must be atomic or inherit
    from virtual class flint. If b is missing, then the return value is the inverse of a, as if b
    were the identity matrix. Operands are promoted as necessary and must be conformable (have
    compatible dimensions). Non-array b are handled as length(b)-by-1 matrices.

xtfrm signature(x = "acf"):
    returns a numeric vector that sorts in the same order as x. The permutation order(xtfrm(x),
    ...) orders x first by its real part then by its imaginary part, with the caveat that all  $a + \text{NaN}i$ 
    and  $\text{NaN} + bi$  have equal precedence (for compatibility with base).

```

See Also

Virtual class `flint`. Generic functions `Real` and `Imag` and their replacement forms for getting and setting real and imaginary parts.

Examples

```

showClass("acf")
showMethods(classes = "acf")

```

arb-class

Arbitrary Precision Floating-Point Real Numbers with Error Bounds

Description

Class `arb` extends virtual class `flint`. It represents vectors of arbitrary precision floating-point real numbers with error bounds. Elements are specified by a pair of mixed format floating-point numbers: an `arf` midpoint and a `mag` radius.

Arithmetic on `arb` vectors is midpoint-radius interval arithmetic, also known as ball arithmetic, enabling computation with rigorous propagation of errors. Logic and comparison involving `arb` vectors are defined as follows: unary `op(x)` is true if and only if `op` is true for all elements of the interval `x`, and binary `op(x, y)` is true if and only if `op` is true for all elements of the Cartesian product of the intervals `x` and `y`. A corollary is that the operator `<=` does not define a *total order* on the range of `arb` (that is, the set of intervals $[m - r, m + r]$), and a consequence is that methods for generic functions that necessitate a total order tend to signal an error.

Usage

```
## Class generator functions
```

```
arb(x = 0, length = 0L, names = NULL, mid = 0, rad = 0)
```

```
arb.array(x = 0, dim = length(x), dimnames = NULL, mid = 0, rad = 0)
```

Arguments

x	an atomic or flint vector containing data for conversion to arb.
length	a numeric vector of length one giving the length of the return value. If that exceeds the length of x, then x is recycled. Non-integer values are rounded in the direction of zero.
names	the names slot of the return value, either NULL or a character vector of equal length. Non-character names are coerced to character.
dim	the dim slot of the return value, an integer vector of nonzero length. If the product exceeds the length of x, then x is recycled. Non-integer numeric dim are coerced to integer.
dimnames	the dimnames slot of the return value, either NULL or a list of length equal to the length of dim. The components are either NULL or character vectors of length given by dim. Non-character vector components of dimnames are coerced to character.
mid, rad	atomic or flint vectors containing data for conversion to arf and mag , respectively. Use these for initialization “by parts” (midpoint and radius).

Details

The class generator function has six distinct usages:

```
arb()
arb(length=)
arb(x)
arb(x, length=)
arb(mid=, mid=)
arb(mid=, mid=, length=)
```

The first usage generates an empty vector. The second usage generates a zero vector of the indicated length. The third usage converts x, preserving dimensions, dimension names, and names. The fourth usage converts x, recycling its elements to the indicated length and discarding its dimensions, dimension names, and names. The fifth and sixth usages, in which either of mid and rad can be missing, use [arf](#)(mid) and [mag](#)(rad) to separately initialize the midpoints and radii of the arb return value.

Attempts to recycle mid, rad, or x of length zero to nonzero length are an error.

Usage of arb.array is modelled after [array](#).

Value

An arb vector, possibly an array; see ‘Details’.

Conversion

Real numbers and real parts of complex numbers are rounded according to the default precision and rounding mode set by `flintPrec` and `flintRnd`. Ball midpoints are the numbers obtained by rounding. Ball radii are upper bounds on the absolute errors incurred by rounding. Imaginary parts of complex numbers are discarded.

Character strings are scanned for format " $s(km+/-r)$ ", where k and m define the sign and absolute value of the signed ball midpoint, and r defines the unsigned ball radius. k can be empty if the ball midpoint is NaN or non-negative. s is an optional unary plus or minus to be reconciled with k .

The sequences km and r are converted using function `mpfr_strtofr` from the GNU MPFR library with argument base set to 0 and argument `rnd` set according to the default rounding mode (for the midpoint, whereas the radius is always rounded towards Inf); see <https://www.mpfr.org/mpfr-current/mpfr.html#Assignment-Functions>.

Slots

`.xData`, `dim`, `dimnames`, `names` inherited from virtual class `flint`.

Methods

Due to constraints imposed by generic functions, methods typically do *not* provide a formal argument `prec` allowing for a precision to be indicated in the function call. Such methods use the current default precision set by `flintPrec`.

```
! signature(x = "arb"):
    equivalent to (but faster than) x == 0.

%*, crossprod, tcrossprod signature(x = "arb", y = "arb"):
    signature(x = "arb", y = "ANY"):
    signature(x = "ANY", y = "arb"):
    matrix products. The "other" operand must be atomic or inherit from virtual class flint.
    crossprod and tcrossprod behave as if  $y = x$  when  $y$  is missing or NULL. Operands are
    promoted as necessary and must be conformable (have compatible dimensions). Non-array
    operands of length  $k$  are handled as 1-by- $k$  or  $k$ -by-1 matrices depending on the call.

+ signature(e1 = "arb", e2 = "missing"):
    returns a copy of the argument.

- signature(e1 = "arb", e2 = "missing"):
    returns the negation of the argument.

Complex signature(z = "arb"):
    mathematical functions of one argument; see S4groupGeneric.

Math signature(x = "arb"):
    mathematical functions of one argument; see S4groupGeneric.

Math2 signature(x = "arb"):
    decimal rounding according to a second argument digits; see S4groupGeneric. There are
    just two member member functions: round, signif.

Ops signature(e1 = "arb", e2 = "arb"):
    signature(e1 = "arb", e2 = "ANY"):
    signature(e1 = "ANY", e2 = "arb"):
```


binary arithmetic, comparison, and logical operators; see [S4groupGeneric](#). The “other” operand must be atomic or inherit from virtual class [flint](#). Operands are promoted as necessary. Array operands must be conformable (have identical dimensions). Non-array operands are recycled.

Summary signature(x = "arb"):

univariate summary statistics; see [S4groupGeneric](#). The return value is a logical vector of length 1 (any, all) or an arb vector of length 1 or 2 (sum, prod, min, max, range).

anyNA signature(x = "arb"):

returns TRUE if any element of x has midpoint NaN, FALSE otherwise.

as.vector signature(x = "arb"):

returns `as.vector(y, mode)`, where y is a double vector containing the result of converting the midpoints of x to the range of double, rounding if the value is not exactly representable in double precision. The rounding mode is to the nearest representable number (with precedence to even significands in case of ties), unless a midpoint exceeds `.Machine[["double.xmax"]]` in absolute value, in which case `-Inf` or `Inf` is introduced with a warning. Coercion to types "character", "symbol" (synonym "name"), "pairlist", "list", and "expression", which are not “number-like”, is handled specially. See also [asVector](#).

backsolve signature(r = "arb", x = "arb"):

signature(r = "arb", x = "ANY"):

signature(r = "ANY", x = "arb"):

solution of the triangular system `op2(op1(r)) %*% y = x`, where `op1=ifelse(upper.tri, triu, tril)` and `op2=ifelse(transpose, t, identity)` and `upper.tri` and `transpose` are optional logical arguments with default values TRUE and FALSE, respectively. The “other” operand must be atomic or inherit from virtual class [flint](#). If x is missing, then the return value is the inverse of `op2(op1(r))`, as if x were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array x are handled as `length(x)-by-1` matrices.

chol signature(x = "arb"):

returns the upper triangular Cholesky factor of the positive definite matrix whose upper triangular part is the upper triangular part of x.

chol2inv signature(x = "arb"):

returns the inverse of the positive definite matrix whose upper triangular Cholesky factor is the upper triangular part of x.

coerce signature(from = "ANY", to = "arb"):

returns the value of `arb(from)`.

colSums, colMeans signature(x = "arb"):

returns an arb vector or array containing the column sums or means of x, defined as sums or means over dimensions `1:dims`.

det signature(x = "arb"):

returns the determinant of x as an arb vector of length 1.

determinant signature(x = "arb"):

returns a list with components `modulus` and `sign` specifying the determinant of x, following the **base** function, hence see [determinant](#). The sign is NA if the interval computed by `det(x)` contains both negative numbers and positive numbers.

`format signature(x = "arb"):`
 returns a character vector suitable for printing, using string format " $(m \pm r)$ " and scientific format for m and r . Optional arguments control the output; see [format-methods](#).

`is.finite signature(x = "arb"):`
 returns a logical vector indicating which elements of x do not have midpoint NaN, $-\text{Inf}$, or Inf or radius Inf .

`is.infinite signature(x = "arb"):`
 returns a logical vector indicating which elements of x have midpoint $-\text{Inf}$ or Inf or radius Inf .

`is.na, is.nan signature(x = "arb"):`
 returns a logical vector indicating which elements of x have midpoint NaN.

`is.unsorted signature(x = "arb"):`
 signals an error indicating that $\leq$ is not a total order on the range of arb ; see `xtfrm` below.

`log signature(x = "arb"):`
 returns the logarithm of the argument. The natural logarithm is computed by default (when optional argument `base` is unset).

`mean signature(x = "arb"):`
 returns the arithmetic mean.

`rowSums, rowMeans signature(x = "arb"):`
 returns an arb vector or array containing the row sums or means of x , defined as sums or means over dimensions $(\text{dims}+1):\text{length}(\text{dim}(x))$.

`solve signature(a = "arb", b = "arb"):`
`signature(a = "arb", b = "ANY"):`
`signature(a = "ANY", b = "arb"):`
 solution of the general system $a \%*\% x = b$. The "other" operand must be atomic or inherit from virtual class [flint](#). If b is missing, then the return value is the inverse of a , as if b were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array b are handled as $\text{length}(b)$ -by-1 matrices.

`xtfrm signature(x = "arb"):`
 signals an error indicating that $\leq$ is not a total order on the range of arb : $a \leq b \mid \mid b \leq a$ is not TRUE for all finite a and b of class arb . Thus, direct sorting of arb is not supported. Users wanting to order the *midpoints* should operate on [Mid](#)(x).

References

The FLINT documentation of the underlying C type: <https://flintlib.org/doc/arb.html>

Johansson, F. (2017). Arb: efficient arbitrary-precision midpoint-radius interval arithmetic. *IEEE Transactions on Computers*, 66(8), 1281-1292. doi:10.1109/TC.2017.2690633

See Also

Virtual class [flint](#). Generic functions [Mid](#) and [Rad](#) and their replacement forms for getting and setting midpoints and radii.

Examples

```
showClass("arb")
showMethods(classes = "arb")
```

arb_dirichlet_zeta *Zeta and Related Functions*

Description

Compute the Riemann zeta function, the Hurwitz zeta function, or Lerch's transcendent. Lerch's transcendent $\Phi(z, s, a)$ is defined by

$$\sum_{k=0}^{\infty} \frac{z^k}{(k+a)^s}$$

for $|z| < 1$ and by analytic continuation elsewhere in the z -plane. The Riemann and Hurwitz zeta functions are the special cases $\zeta(s) = \Phi(1, s, 1)$ and $\zeta(s, a) = \Phi(1, s, a)$, respectively. See the references for restrictions on s and a .

Usage

```
arb_dirichlet_zeta(s, prec = flintPrec())
acb_dirichlet_zeta(s, prec = flintPrec())

arb_dirichlet_hurwitz(s, a = 1, prec = flintPrec())
acb_dirichlet_hurwitz(s, a = 1, prec = flintPrec())

## arb_dirichlet_lerch_phi(z = 1, s, a = 1, prec = flintPrec())
## acb_dirichlet_lerch_phi(z = 1, s, a = 1, prec = flintPrec())
```

Arguments

`z, s, a` numeric, complex, [arb](#), or [acb](#) vectors.

`prec` a numeric or [slong](#) vector indicating the desired precision as a number of bits.

Value

An [arb](#) or [acb](#) vector storing function values with error bounds. Its length is the maximum of the lengths of the arguments or zero (zero if any argument has length zero). The arguments are recycled as necessary.

References

The FLINT documentation of the underlying C functions: https://flintlib.org/doc/acb_dirichlet.html

NIST Digital Library of Mathematical Functions: <https://dlmf.nist.gov/25>

See Also

Classes [arb](#) and [acb](#).

Examples

```
dzet <- acb_dirichlet_zeta
dhur <- acb_dirichlet_hurwitz
dler <- acb_dirichlet_lerch_phi

## Somewhat famous particular values :
debugging <- tolower(Sys.getenv("R_FLINT_CHECK_EXTRA")) == "true"
s <- acb(x = c(-1, 0, 2, 4))
zeta.s <- acb(x = c(-1/12, -1/2, pi^2/6, pi^4/90))
stopifnot(all.equal(dzet(s), zeta.s),
          all.equal(dhur(s, 1), zeta.s),
          !debugging ||
          {
            print(cbind(as.complex(dler(1, s, 1)), as.complex(zeta.s)))
            all.equal(dler(1, s, 1), zeta.s) # FLINT bug, report this
          })

set.seed(0xabcdL)
r <- 10L
eps <- 0x1p-4
a <- flint::complex.runif(r, modulus = c(0, 1/eps))
z.l1 <- flint::complex.runif(r, modulus = c(0, 1-eps))
z.g1 <- flint::complex.runif(r, modulus = c(1+eps, 1/eps))
z <- acb(x = c(z.l1, z.g1))

## A relation with the hypergeometric function from
## http://dlmf.nist.gov/25.14.E3_3 :
h2f1 <- acb_hypgeom_2f1
stopifnot(all.equal(dler(z.l1, 1, a), h2f1(a, 1, a + 1, z.l1)/a))

## TODO: test values also for z[Mod(z) > 1] ...
```

arb_hypgeom_2f1

Hypergeometric Functions

Description

Computes the principal branch of the hypergeometric function ${}_2F_1(a, b, c, z)$, defined by

$$\sum_{k=0}^{\infty} \frac{(a)_k (b)_k}{(c)_k} \frac{z^k}{k!}$$

for $|z| < 1$ and by analytic continuation elsewhere in the z -plane, or the principal branch of the *regularized* hypergeometric function ${}_2F_1(a, b, c, z)/\Gamma(c)$.

Usage

```
arb_hypgeom_2f1(a, b, c, x, flags = 0L, prec = flintPrec())
acb_hypgeom_2f1(a, b, c, z, flags = 0L, prec = flintPrec())
```

Arguments

a, b, c, x, z	numeric, complex, arb , or acb vectors.
flags	an integer vector. The lowest bit of the integer element(s) indicates whether to regularize. Later bits indicate special cases for which an alternate algorithm may be used. Non-experts should use flags = 0L or 1L, leaving the later bits unset.
prec	a numeric or slong vector indicating the desired precision as a number of bits.

Value

An [arb](#) or [acb](#) vector storing function values with error bounds. Its length is the maximum of the lengths of the arguments or zero (zero if any argument has length zero). The arguments are recycled as necessary.

References

The FLINT documentation of the underlying C functions: https://flintlib.org/doc/arb_hypgeom.html, https://flintlib.org/doc/acb_hypgeom.html

NIST Digital Library of Mathematical Functions: <https://dlmf.nist.gov/15>

See Also

Classes [arb](#) and [acb](#).

Examples

```
h2f1 <- acb_hypgeom_2f1

set.seed(0xbcdeL)
r <- 10L
eps <- 0x1p-4
z.l1 <- flint::complex.runif(r, modulus = c( 0, 1-eps))
z.g1 <- flint::complex.runif(r, modulus = c(1+eps, 1/eps))
z <- acb(x = c(z.l1, z.g1))

## Elementary special cases from http://dlmf.nist.gov/15.4 :
stopifnot(all.equal(h2f1(1.0, 1.0, 2.0, z ),
                    -log(1 - z)/z),
          all.equal(h2f1(0.5, 1.0, 1.5, z^2),
                    0.5 * (log(1 + z) - log(1 - z))/z),
          all.equal(h2f1(0.5, 1.0, 1.5, -z^2),
                    atan(z)/z))
## [ see more in ../tests/hypgeom.R ]
```

Description

Compute the principal branches of the (modified) Bessel functions of the first and second kind. The Bessel functions of the first and second kind solve Bessel's equation

$$z^2 \frac{d^2 w}{dz^2} + z \frac{dw}{dz} + (z^2 - \nu^2)w = 0$$

and are given by

$$J_\nu(z) = \left(\frac{1}{2}z\right)^\nu \sum_{k=0}^{\infty} (-1)^k \frac{\left(\frac{1}{4}z^2\right)^k}{k! \Gamma(\nu + k + 1)}$$

$$Y_\nu(z) = \frac{Y_\nu(z) \cos(\nu\pi) - J_{-\nu}(z)}{\sin(\nu\pi)}$$

The modified Bessel functions of the first and second kind solve the modified Bessel's equation

$$z^2 \frac{d^2 w}{dz^2} + z \frac{dw}{dz} - (z^2 + \nu^2)w = 0$$

and are given by

$$I_\nu(z) = \left(\frac{1}{2}z\right)^\nu \sum_{k=0}^{\infty} \frac{\left(\frac{1}{4}z^2\right)^k}{k! \Gamma(\nu + k + 1)}$$

$$K_\nu(z) = \frac{\pi}{2} \frac{I_{-\nu}(z) - I_\nu(z)}{\sin(\nu\pi)}$$

Usage

```
arb_hypgeom_bessel_j(nu, x, prec = flintPrec())
acb_hypgeom_bessel_j(nu, z, prec = flintPrec())
```

```
arb_hypgeom_bessel_y(nu, x, prec = flintPrec())
acb_hypgeom_bessel_y(nu, z, prec = flintPrec())
```

```
arb_hypgeom_bessel_i(nu, x, prec = flintPrec())
acb_hypgeom_bessel_i(nu, z, prec = flintPrec())
```

```
arb_hypgeom_bessel_k(nu, x, prec = flintPrec())
acb_hypgeom_bessel_k(nu, z, prec = flintPrec())
```

Arguments

nu, x, z	numeric, complex, arb , or acb vectors.
prec	a numeric or slong vector indicating the desired precision as a number of bits.

Value

An [arb](#) or [acb](#) vector storing function values with error bounds. Its length is the maximum of the lengths of the arguments or zero (zero if any argument has length zero). The arguments are recycled as necessary.

References

The FLINT documentation of the underlying C functions: https://flintlib.org/doc/arb_hypgeom.html, https://flintlib.org/doc/acb_hypgeom.html

NIST Digital Library of Mathematical Functions: <https://dlmf.nist.gov/10>

See Also

Classes [arb](#) and [acb](#); [arb_hypgeom_gamma_lower](#) and [arb_hypgeom_beta_lower](#) for the “incomplete” gamma and beta functions.

Examples

```
## TODO
```

arb_hypgeom_gamma	<i>Gamma and Related Functions</i>
-------------------	------------------------------------

Description

Compute the gamma function, the reciprocal gamma function, the logarithm of the absolute value of the gamma function, the polygamma function, or the beta function. The gamma function $\Gamma(z)$ is defined by

$$\int_0^{\infty} t^{z-1} e^{-t} dt$$

for $\Re(z) > 0$ and by analytic continuation elsewhere in the z -plane, excluding poles at $z = 0, -1, \dots$. The beta function $B(a, b)$ is defined by

$$\int_0^1 t^{a-1} (1-t)^{b-1} dt$$

for $\Re(a), \Re(b) > 0$ and by analytic continuation to all other (a, b) .

Usage

```
arb_hypgeom_gamma(x, prec = flintPrec())
acb_hypgeom_gamma(z, prec = flintPrec())

arb_hypgeom_rgamma(x, prec = flintPrec())
acb_hypgeom_rgamma(z, prec = flintPrec())

arb_hypgeom_lgamma(x, prec = flintPrec())
```

```

acb_hypgeom_lgamma(z, prec = flintPrec())

## arb_hypgeom_polygamma(s = 0, z, prec = flintPrec())
  acb_hypgeom_polygamma(s = 0, z, prec = flintPrec())

arb_hypgeom_beta(a, b, prec = flintPrec())
acb_hypgeom_beta(a, b, prec = flintPrec())

```

Arguments

`x, z, s, a, b` numeric, complex, [arb](#), or [acb](#) vectors.

`prec` a numeric or [slong](#) vector indicating the desired precision as a number of bits.

Details

`acb_hypgeom_polygamma(s, z)` evaluates the polygamma function of order s at z . The order s can be any complex number. For nonnegative integers m , $s = m$ corresponds to the derivative of order m of the digamma function $\psi(z) = \Gamma'(z)/\Gamma(z)$. Use `acb_hypgeom_polygamma(0, z)` to evaluate the digamma function at z .

Value

An [arb](#) or [acb](#) vector storing function values with error bounds. Its length is the maximum of the lengths of the arguments or zero (zero if any argument has length zero). The arguments are recycled as necessary.

References

The FLINT documentation of the underlying C functions: https://flintlib.org/doc/arb_hypgeom.html, https://flintlib.org/doc/acb_hypgeom.html

NIST Digital Library of Mathematical Functions: <https://dlmf.nist.gov/5>

See Also

Classes [arb](#) and [acb](#); [arb_hypgeom_gamma_lower](#) and [arb_hypgeom_beta_lower](#) for the “incomplete” gamma and beta functions.

Examples

```
## TODO
```

arb_hypgeom_gamma_lower

Incomplete Gamma and Related Functions

Description

Compute the principal branch of the (optionally, regularized) incomplete gamma and beta functions. The lower incomplete gamma function $\gamma(s, z)$ is defined by

$$\int_0^z t^{s-1} e^{-t} dt$$

for $\Re(s) > 0$ and by analytic continuation elsewhere in the s -plane, excluding poles at $s = 0, -1, \dots$. The upper incomplete gamma function $\Gamma(s, z)$ is defined by

$$\int_z^\infty t^{s-1} e^{-t} dt$$

for $\Re(s) > 0$ and by analytic continuation elsewhere in the s -plane except at $z = 0$. The incomplete beta function $B(a, b, z)$ is defined by

$$\int_0^z t^{a-1} (1-t)^{b-1} dt$$

for $\Re(a), \Re(b) > 0$ and by analytic continuation to all other (a, b) . It coincides with the beta function at $z = 1$. The regularized functions are $\gamma(s, z)/\Gamma(s)$, $\Gamma(s, z)/\Gamma(s)$, and $B(a, b, z)/B(a, b)$.

Usage

```
arb_hypgeom_gamma_lower(s, x, flags = 0L, prec = flintPrec())
acb_hypgeom_gamma_lower(s, z, flags = 0L, prec = flintPrec())

arb_hypgeom_gamma_upper(s, x, flags = 0L, prec = flintPrec())
acb_hypgeom_gamma_upper(s, z, flags = 0L, prec = flintPrec())

arb_hypgeom_beta_lower(a, b, x, flags = 0L, prec = flintPrec())
acb_hypgeom_beta_lower(a, b, z, flags = 0L, prec = flintPrec())
```

Arguments

<code>x, z, s, a, b</code>	numeric, complex, arb , or acb vectors.
<code>flags</code>	an integer vector with elements 0, 1, or 2 indicating unregularized, regularized, or “alternately” regularized; see the FLINT documentation.
<code>prec</code>	a numeric or slong vector indicating the desired precision as a number of bits.

Value

An [arb](#) or [acb](#) vector storing function values with error bounds. Its length is the maximum of the lengths of the arguments or zero (zero if any argument has length zero). The arguments are recycled as necessary.

References

The FLINT documentation of the underlying C functions: https://flintlib.org/doc/arb_hypgeom.html, https://flintlib.org/doc/acb_hypgeom.html

NIST Digital Library of Mathematical Functions: <https://dlmf.nist.gov/8>

See Also

Classes `arb` and `acb`; `arb_hypgeom_gamma` and `arb_hypgeom_beta` for the “complete” gamma and beta functions.

Examples

```
hg <- acb_hypgeom_gamma
hgl <- acb_hypgeom_gamma_lower
hgu <- acb_hypgeom_gamma_upper

hb <- acb_hypgeom_beta
hbl <- acb_hypgeom_beta_lower

set.seed(0xcdefL)
r <- 10L
eps <- 0x1p-4
a <- flint:::complex.runif(r, modulus = c( 0, 1/eps))
b <- flint:::complex.runif(r, modulus = c( 0, 1/eps))
z <- flint:::complex.runif(r, modulus = c(eps, 1/eps))

## Some trivial identities
stopifnot(# http://dlmf.nist.gov/8.2.E3
          all.equal(hgl(a, z) + hgu(a, z), hg(a), tolerance = 1e-5),
          # https://dlmf.nist.gov/8.4.E5
          all.equal(hgu(1, z), exp(-z), check.class = FALSE))

## Regularization
stopifnot(all.equal(hgl(a, z, flags = 1L), hgl(a, z)/hg(a)),
          all.equal(hgu(a, z, flags = 1L), hgu(a, z)/hg(a)),
          all.equal(hbl(a, b, z, flags = 1L), hbl(a, b, z)/hb(a, b)))

## A relation with the hypergeometric function from
## https://dlmf.nist.gov/8.17.E7 :
h2f1 <- acb_hypgeom_2f1
stopifnot(all.equal(hbl(a, b, z), z^a * h2f1(a, 1 - b, a + 1, z)/a))
```

arb_lambertw

Lambert W function

Description

Computes any branch W_k of the multiple-valued Lambert W function. $W(z)$ is the set of solutions w of the equation $we^w = z$.

Usage

```
arb_lambertw(x,          flags = 0L, prec = flintPrec())
acb_lambertw(z, k = 0L, flags = 0L, prec = flintPrec())
```

Arguments

x, z	numeric, complex, arb , or acb vectors.
k	an integer or fmpz vector listing indices of branches of the function. 0 indicates the principal branch.
flags	for <code>arb_lambertw</code> : an integer vector indicating which of the index 0 and index -1 branches is computed (0 means index 0, 1 means index -1). for <code>acb_lambertw</code> : an integer vector indicating how branch cuts are defined. Nonzero values are nonstandard; see the first reference.
prec	a numeric or slong vector indicating the desired precision as a number of bits.

Value

An [arb](#) or [acb](#) vector storing function values with error bounds. Its length is the maximum of the lengths of the arguments or zero (zero if any argument has length zero). The arguments are recycled as necessary.

References

The FLINT documentation of the underlying C functions: <https://flintlib.org/doc/arb.html>, <https://flintlib.org/doc/acb.html>

NIST Digital Library of Mathematical Functions: <https://dlmf.nist.gov/4.13>

See Also

Classes [arb](#) and [acb](#).

Examples

```
## TODO
```

 arf-class

Arbitrary Precision Floating-Point Real Numbers

Description

Class `arf` extends virtual class [flint](#). It represents vectors of arbitrary precision floating-point real numbers. Elements have arbitrary precision significand and exponent. The underlying C type can represent NaN, -Inf, and Inf.

Usage

```
## Class generator functions
```

```
arf(x = 0, length = 0L, names = NULL)
```

```
arf.array(x = 0, dim = length(x), dimnames = NULL)
```

Arguments

x	an atomic or flint vector containing data for conversion to arf.
length	a numeric vector of length one giving the length of the return value. If that exceeds the length of x, then x is recycled. Non-integer values are rounded in the direction of zero.
names	the names slot of the return value, either NULL or a character vector of equal length. Non-character names are coerced to character.
dim	the dim slot of the return value, an integer vector of nonzero length. If the product exceeds the length of x, then x is recycled. Non-integer numeric dim are coerced to integer.
dimnames	the dimnames slot of the return value, either NULL or a list of length equal to the length of dim. The components are either NULL or character vectors of length given by dim. Non-character vector components of dimnames are coerced to character.

Details

The class generator function has four distinct usages:

```
arf()
arf(length=)
arf(x)
arf(x, length=)
```

The first usage generates an empty vector. The second usage generates a zero vector of the indicated length. The third usage converts x, preserving dimensions, dimension names, and names. The fourth usage converts x, recycling its elements to the indicated length and discarding its dimensions, dimension names, and names. Attempts to recycle x of length zero to nonzero length are an error.

Usage of `arf.array` is modelled after [array](#).

Value

A arf vector, possibly an array; see ‘Details’.

Conversion

Real numbers and real parts of complex numbers are rounded according to the default precision and rounding mode set by [flintPrec](#) and [flintRnd](#). Imaginary parts of complex numbers are discarded.

Character strings are converted using function `mpfr_strtobr` from the GNU MPFR library with argument base set to 0 and argument `rnd` set according to the default rounding mode; see <https://www.mpfr.org/mpfr-current/mpfr.html#Assignment-Functions>.

Slots

`.xData`, `dim`, `dimnames`, `names` inherited from virtual class `flint`.

Methods

Due to constraints imposed by generic functions, methods typically do *not* provide a formal argument `prec` allowing for a precision to be indicated in the function call. Such methods use the current default precision set by `flintPrec`.

`!` `signature(x = "arf")`:
equivalent to (but faster than) `x == 0`.

`%*%, crossprod, tcrossprod` `signature(x = "arf", y = "arf")`:
`signature(x = "arf", y = "ANY")`:
`signature(x = "ANY", y = "arf")`:
matrix products. The “other” operand must be atomic or inherit from virtual class `flint`. `crossprod` and `tcrossprod` behave as if `y = x` when `y` is missing or `NULL`. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array operands of length `k` are handled as 1-by-`k` or `k`-by-1 matrices depending on the call. The return value is approximate insofar that it may not be correctly rounded.

`+` `signature(e1 = "arf", e2 = "missing")`:
returns a copy of the argument.

`-` `signature(e1 = "arf", e2 = "missing")`:
returns the negation of the argument.

`Complex` `signature(z = "arf")`:
mathematical functions of one argument; see `S4groupGeneric`.

`Math` `signature(x = "arf")`:
mathematical functions of one argument; see `S4groupGeneric`. Notably, the logarithmic, exponential, (inverse) trigonometric, (inverse) hyperbolic, and gamma-related member functions are not yet implemented. Users wanting those can (for now) operate on `arb(x)`.

`Math2` `signature(x = "arf")`:
decimal rounding according to a second argument `digits`; see `S4groupGeneric`. There are just two member functions: `round`, `signif`.

`Ops` `signature(e1 = "arf", e2 = "arf")`:
`signature(e1 = "arf", e2 = "ANY")`:
`signature(e1 = "ANY", e2 = "arf")`:
binary arithmetic, comparison, and logical operators; see `S4groupGeneric`. The “other” operand must be atomic or inherit from virtual class `flint`. Operands are promoted as necessary. Array operands must be conformable (have identical dimensions). Non-array operands are recycled.

`Summary` `signature(x = "arf")`:
univariate summary statistics; see `S4groupGeneric`. The return value is a logical vector of length 1 (`any`, `all`) or an `arf` vector of length 1 or 2 (`sum`, `prod`, `min`, `max`, `range`).

`anyNA` signature($x = \text{"arf"}$):
 returns TRUE if any element of x is NaN, FALSE otherwise.

`as.vector` signature($x = \text{"arf"}$):
 returns `as.vector(y, mode)`, where y is a double vector containing the result of converting each element of x to the range of double, rounding if the value is not exactly representable in double precision. The rounding mode is to the nearest representable number (with precedence to even significands in case of ties), unless the element exceeds `.Machine[["double.xmax"]]` in absolute value, in which case `-Inf` or `Inf` is introduced with a warning. Coercion to types `"character"`, `"symbol"` (synonym `"name"`), `"pairlist"`, `"list"`, and `"expression"`, which are not “number-like”, is handled specially. See also [asVector](#).

`backsolve` signature($r = \text{"arf"}$, $x = \text{"arf"}$):
 signature($r = \text{"arf"}$, $x = \text{"ANY"}$):
 signature($r = \text{"ANY"}$, $x = \text{"arf"}$):
 solution of the triangular system `op2(op1(r)) %*% y = x`, where `op1=ifelse(upper.tri, triu, tril)` and `op2=ifelse(transpose, t, identity)` and `upper.tri` and `transpose` are optional logical arguments with default values TRUE and FALSE, respectively. The “other” operand must be atomic or inherit from virtual class [flint](#). If x is missing, then the return value is the inverse of `op2(op1(r))`, as if x were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array x are handled as `length(x)-by-1` matrices.

`chol` signature($x = \text{"arf"}$):
 returns the upper triangular Cholesky factor of the positive definite matrix whose upper triangular part is the upper triangular part of x .

`chol2inv` signature($x = \text{"arf"}$):
 returns the inverse of the positive definite matrix whose upper triangular Cholesky factor is the upper triangular part of x .

`coerce` signature($from = \text{"ANY"}$, $to = \text{"arf"}$):
 returns the value of `arf(from)`.

`colSums`, `colMeans` signature($x = \text{"arf"}$):
 returns an arf vector or array containing the column sums or means of x , defined as sums or means over dimensions `1:dims`.

`det` signature($x = \text{"arf"}$):
 returns the determinant of x as an arf vector of length 1.

`determinant` signature($x = \text{"arf"}$):
 returns a list with components `modulus` and `sign` specifying the determinant of x , following the **base** function, hence see [determinant](#).

`format` signature($x = \text{"arf"}$):
 returns a character vector suitable for printing, using scientific format. Optional arguments control the output; see [format-methods](#).

`is.finite` signature($x = \text{"arf"}$):
 returns a logical vector indicating which elements of x are not NaN, `-Inf`, or `Inf`.

`is.infinite` signature($x = \text{"arf"}$):
 returns a logical vector indicating which elements of x are `-Inf` or `Inf`.

`is.na`, `is.nan` signature($x = \text{"arf"}$):
 returns a logical vector indicating which elements of x are NaN.

```
is.unsorted signature(x = "arf"):
  returns a logical indicating if x is not sorted in nondecreasing order (increasing order if optional argument strictly is set to TRUE).

mean signature(x = "arf"):
  returns the arithmetic mean.

rowSums, rowMeans signature(x = "arf"):
  returns an arf vector or array containing the row sums or means of x, defined as sums or means over dimensions (dims+1):length(dim(x)).

solve signature(a = "arf", b = "arf"):
  signature(a = "arf", b = "ANY"):
  signature(a = "ANY", b = "arf"):
  solution of the general system  $a \%* \% x = b$ . The "other" operand must be atomic or inherit from virtual class flint. If b is missing, then the return value is the inverse of a, as if b were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array b are handled as length(b)-1 matrices.
```

References

The FLINT documentation of the underlying C type: <https://flintlib.org/doc/arf.html>

Johansson, F. (2017). Arb: efficient arbitrary-precision midpoint-radius interval arithmetic. *IEEE Transactions on Computers*, 66(8), 1281-1292. doi:10.1109/TC.2017.2690633

See Also

Virtual class `flint`.

Examples

```
showClass("arf")
showMethods(classes = "arf")
```

asVector

Coerce an Object to a Vector Class

Description

A generalization of `as.vector` enabling coercion from and to `flint` vector classes (in addition to basic vector classes) and providing more uniform handling of attributes.

Usage

```
asVector(x, mode = "any", strict = TRUE)
```

Arguments

<code>x</code>	an R object coercible to the target class.
<code>mode</code>	a character string indicating the target class.
<code>strict</code>	a logical indicating if attributes of <code>x</code> should be discarded and if the class of the return value must match the target class exactly (and hence not be a subclass of the target class).

Details

Argument `mode` can be one of the basic vector classes `"raw"`, `"logical"`, `"integer"`, `"numeric"` (synonym `"double"`), `"complex"`, `"character"`, `"list"`, and `"expression"`; one of the flint vector classes `"ulong"`, `"slong"`, `"fmpz"`, `"fmpq"`, `"mag"`, `"arf"`, `"acf"`, `"arb"`, and `"acb"`; or one of `"any"`, `"vector"`, and `"flint"`, indicating the vector class, basic vector class, and flint vector class "nearest" the class of `x`. Note that `as.vector` supports `mode` equal to `"name"` (synonym `"symbol"`) or `"pairlist"`. `asVector` does not: names and pairlists are not vectors!

Value

The result of coercing `x` to the target class indicated by `mode`.

See Also

Virtual class [vector](#) and related functions [as.vector](#) and [as](#).

Examples

```
str(J <- diag(ulong(1L), 2L))

as.integer(J)
as.vector(J, "integer")
as(J, "integer")
asVector(J, "integer")
asVector(J, "integer", FALSE)

setClass("ulongExtension", contains = "ulong")
str(J. <- new("ulongExtension", J))

str(asVector(J, "ulong"))
str(asVector(J., "ulong"))
str(asVector(J, "ulong", FALSE))
str(asVector(J., "ulong", FALSE))
```


c.flint

Concatenate Vectors

Description

Function `c` is primitive and internally generic but it dispatches only on its first argument. A corollary is that `c(x, ...)` does *not* dispatch the S4 method with signature `x="flint"` if `x` is not a `flint` vector, even if a `flint` vector appears later in the call as a component of `...`.

Functions `cbind` and `rbind` are internally generic and dispatch on all components of `...`, creating the possibility of dispatch ambiguities; see `cbind2` and `rbind2`.

S3 methods `c.flint`, `cbind.flint` and `rbind.flint` are registered *and exported* to enable users to bypass internal dispatch.

Usage

```
## S3 method for class 'flint'
c(..., recursive = FALSE, use.names = TRUE)
## S3 method for class 'flint'
cbind(..., deparse.level = 1)
## S3 method for class 'flint'
rbind(..., deparse.level = 1)
```

Arguments

<code>...</code>	objects inheriting from virtual class <code>flint</code> or whose type is one of the vector types or one of the non-vector types <code>NULL</code> , <code>pairlist</code> , <code>symbol</code> , and <code>language</code> .
<code>recursive</code>	a logical indicating if pairlists, lists, and expressions should be handled recursively. If <code>TRUE</code> , then the function behaves as if such arguments were replaced by their terminal nodes.
<code>use.names</code>	a logical indicating if names should be preserved.
<code>deparse.level</code>	an integer (0, 1, or 2) indicating how names are chosen for rows or columns derived from untagged, non-matrix arguments. 0 is to use empty names, 2 is to deparse unevaluated arguments, and 1 (the default value) is to deparse unevaluated arguments only if they are symbols and otherwise use empty names.

Value

If none of the arguments is a `flint` vector, then the internal default methods are dispatched.

If at least one argument is a `flint` vector, then the return value is a `flint` vector, unless `recursive = FALSE` and at least one argument is a `pairlist`, `name`, `call`, `list`, or `expression`, in which case the return value is a `list` or `expression`.

If the return value is a `flint` vector, then its class is the most specific subclass of `flint` whose range contains the ranges of the classes of the arguments.

Examples

```
x <- slong(2:5)
c(x, 6L)
c(1L, x) # bad
c.flint(x, 6L)
c.flint(1L, x)
```

Constants

Mathematical Constants Represented to Arbitrary Precision

Description

Compute standard mathematical constants to arbitrary precision.

Usage

```
arb_const_pi(prec = flintPrec())
arb_const_log2(prec = flintPrec())
arb_const_log10(prec = flintPrec())
arb_const_e(prec = flintPrec())
```

Arguments

`prec` a numeric or [slong](#) vector indicating the desired precision as a number of bits.

Value

An [arb](#) vector storing function values with error bounds. Its length is the length of `prec`, typically 1.

References

The FLINT documentation of the underlying C functions: <https://flintlib.org/doc/arb.html>

See Also

Class [arb](#).

Examples

```
prec <- cumprod(rep(c(1, 2), c(1L, 15L)))
arb_const_pi(prec)
```

flint-class	<i>Class of FLINT-Type Vectors</i>
-------------	------------------------------------

Description

Class `flint` is a virtual class representing vectors of any FLINT `C` type. The `C` type is determined by the class attribute and interfaced exactly using R's external pointer type.

Usage

```
## Class generator functions
```

```
flint(class, ...)
```

```
flint.array(class, ...)
```

Arguments

<code>class</code>	a character string giving the name of a nonvirtual subclass of <code>flint</code> , one of <code>"ulong"</code> , <code>"slong"</code> , <code>"fmpz"</code> , <code>"fmpq"</code> , <code>"mag"</code> , <code>"arf"</code> , <code>"acf"</code> , <code>"arb"</code> , and <code>"acb"</code> .
<code>...</code>	arguments passed to the class generator function corresponding to <code>class</code> .

Value

An object of class `class` generated by the corresponding class generator function. For example, `flint("ulong", ...)` returns `ulong(...)` and `flint.array("slong", ...)` returns `slong.array(...)`.

Slots

`.xData` an external pointer. The protected field is an integer vector of length 1 or 2 storing the object length whose size is 32 or 64 bits depending on the ABI; see `flintABI`. The pointer field contains the address of a block of allocated memory of size greater than or equal to the object length times the size of the FLINT `C` type. It is a null pointer if and only if the object length is zero.

Methods for `initialize` set a finalizer on `.xData` (see `reg.finalizer`) to ensure that allocated memory is freed before `.xData` is itself freed by the garbage collector.

`dim` either `NULL`, indicating that the object is not an array, or an integer vector of length `d` greater than 0 and with product equal to the object length, indicating that the object is a `d`-dimensional array with dimensions `dim`. Array entries are stored in colexicographic order, meaning that the first subscript moves fastest.

`dimnames` either `NULL`, indicating that the object is not an array or is an array whose dimensions are not named, or a list of length `d` equal to `length(dim)` such that `dimnames[[i]]` is either `NULL` or a character vector of length `dim[[i]]`, for all `i` in `1L:d`.

`names` either `NULL`, indicating that the object is not named, or a character vector of length equal to the object length. A corollary is that objects whose length exceeds the maximum length of a character vector cannot have names.

Methods

```
$, $<- signature(x = "flint"):
  signals an error as x is "atomic-like" and in any case not recursive or NULL.
```

```
[ signature(x = "flint", i = "ANY", j = "ANY"):
  signature(x = "ANY", i = "flint", j = "ANY"):
  signature(x = "ANY", i = "ANY", j = "flint"):
  returns a traditional vector or flint vector containing the elements of x indexed by (i, j, ...) (the "subscript"). The components of the subscript can be missing, NULL, logical, integer, double, character, ulong, slong, fmpz, or fmpq. Methods for signatures with x = "flint" signal an error for NA and out of bounds subscripts, as the C types interfaced by flint vectors have no representation for missing values. Note that [ does not perform S4 dispatch if its first positional argument is not an S4 object. If it is known that i is a flint vector and not known whether x is a flint vector, then one option is to call [ as `[ (i = i, x = x)` rather than as x[i]. However, it is not guaranteed that such usage of [, which is mostly undocumented, continues to work in future versions of R.
```

```
[<- signature(x = "flint", i = "ANY", j = "ANY", value = "ANY"):
  signature(x = "ANY", i = "flint", j = "ANY", value = "ANY"):
  signature(x = "ANY", i = "ANY", j = "flint", value = "ANY"):
  signature(x = "ANY", i = "ANY", j = "ANY", value = "flint"):
  returns the traditional vector or flint vector obtained by replacing the elements of x indexed by (i, j, ...) (the "subscript") with elements of value, which are recycled as necessary. The components of the subscript can be missing, NULL, logical, integer, double, character, ulong, slong, fmpz, or fmpq. The class of the return value is determined following strict rules from the classes of x and value, which are promoted to the value class as necessary. If the value class is a subclass of flint, then an error is signaled for NA and out of bounds subscripts, as the C types interfaced by flint vectors have no representation for missing values. Note that [<- does not perform S4 dispatch if its first positional argument is not an S4 object. If it is known that i is a flint vector and not known whether x is a flint vector, then one option is to call [<- as `[ (i = i, x = x) <- value` rather than as x[i] <- value. However, it is not guaranteed that such usage of [<-, which is mostly undocumented, continues to work in future versions of R.
```

```
[ signature(x = "flint", i = "ANY", j = "ANY"):
  signature(x = "ANY", i = "flint", j = "ANY"):
  signature(x = "ANY", i = "ANY", j = "flint"):
  similar to [, with differences as documented in Extract, particularly for recursive x.
```

```
[<- signature(x = "flint", i = "ANY", j = "ANY", value = "ANY"):
  signature(x = "ANY", i = "flint", j = "ANY", value = "ANY"):
  signature(x = "ANY", i = "ANY", j = "flint", value = "ANY"):
  signature(x = "ANY", i = "ANY", j = "ANY", value = "flint"):
  similar to [<-, with differences as documented in Extract, particularly for recursive x.
```

```
all.equal signature(x = "flint", y = "flint"):
  signature(x = "flint", y = "ANY"):
  signature(x = "ANY", y = "flint"):
  returns either TRUE, indicating that there is no meaningful difference between x and y, or a character vector describing differences. The implementation (including optional arguments) is adapted from all.equal.numeric, hence see its documentation. Notably, comparison of objects inheriting from different subclasses of virtual class flint and comparison with objects
```

(typically atomic vectors) coercible to virtual class `flint` are supported with `check.class = FALSE`. See the method for `identical` for much stricter comparison of flint objects.

```
anyDuplicated signature(x = "flint"):
  returns anyDuplicated(mtfm(x), ...).

aperm signature(a = "flint"):
  returns the array obtained by permuting the dimensions of a according to a second argument
  perm, following the documented behaviour of the S3 default method for aperm.

as.raw, as.logical, as.integer, as.numeric, as.complex signature(x = "flint"):
  returns the value of as.vector(x, mode = *). Methods for as.vector must be defined for
  subclasses of flint. Note that as.double dispatches internally the method for as.numeric,
  so there is no method for as.double; see also as.numeric, section 'S4 Methods'.

as.matrix, as.array, as.Date, as.POSIXct, as.POSIXlt signature(x = "flint"):
  coerces the argument with as.vector, restores dimensions, dimension names, and names,
  and dispatches. as.matrix and as.array obtain the same result more efficiently.

as.data.frame signature(x = "flint"):
  behaves as as.data.frame.vector, as.data.frame.matrix, or as.data.frame.array,
  depending on the length of the dim slot. It enables the construction of data frames contain-
  ing flint vectors using as.data.frame and functions that call it such as data.frame and
  cbind.data.frame.

asplit signature(x = "flint"):
  returns a list array containing the marginal splits of x indicated by a second argument MARGIN,
  following the documented behaviour of the base function, hence see asplit.

c signature(x = "flint"):
  returns c.flint(x, ...), the concatenation of the arguments. Function c.flint is exported
  to work around the fact that c(x, ...) dispatches only on x.

cbind2 signature(x = "flint", y = "flint"):
  signature(x = "flint", y = "ANY"):
  signature(x = "ANY", y = "flint"):
  returns cbind.flint(x, y, ...), the horizontal concatenation of x and y. These methods
  are dispatched by cbind in case of S3 dispatch ambiguities; see cbind2.

coerce signature(from = "ANY", to = "flint"):
  coerces atomic (except character) vectors from to the most specific subclass of flint whose
  range contains the range of typeof(from).

cut signature(x = "flint"):
  returns findInterval(x=x, vec=breaks, left.open=right, rightmost.closed=include.lowest),
  hence see below. The behaviour is consistent with the S3 default method for cut with argu-
  ment labels set to FALSE, provided that breaks is sorted and no element of x is out of bounds.

diag signature(x = "flint"):
  if x is a matrix, then returns a flint vector containing the diagonal entries of x; otherwise,
  returns a diagonal matrix with diagonal entries taken from x. Optional arguments nrow, ncol,
  and names are handled as by the base function, hence see diag.

diag<- signature(x = "flint", value = "ANY"):
  returns x, which must be a matrix, after setting its main diagonal to value, whose length must
  be equal to 1 or the length of x. Arguments x and value are coerced to a common class
  following the rules used for general subassignment; see the methods for [<- and [[<-.
```

```

dim signature(x = "flint"):
  returns the dim slot of x.
dim<- signature(x = "flint", value = "NULL"):
  returns x with dim and dimnames slots set to NULL.
dim<- signature(x = "flint", value = "numeric"):
  returns x with dim slot set to value and dimnames slot set to NULL. value of double type is
  coerced to integer.
dimnames signature(x = "flint"):
  returns the dimnames slot of x.
dimnames<- signature(x = "flint", value = "NULL"):
  returns x with dimnames slot set to NULL.
dimnames<- signature(x = "flint", value = "list"):
  returns x with dimnames slot set to value. Elements of value of a vector type are coerced
  to character using as.character.default. Exceptionally, factors are coerced to character
  using as.character.factor.
drop signature(x = "flint"):
  returns x with dim, dimnames, and names slots modified following the documented behaviour
  of the base function, hence see drop.
duplicated signature(x = "flint"):
  returns duplicated(mtfm(x), ...).
findInterval returns a ulong vector of length equal to the length of x, following the documented
  behaviour of the base function, hence see findInterval. A caveat is that an error is signaled
  if x contains NaN, because ulong has no representation for R's missing value NA\_integer\_.
identical signature(x = "flint", y = "flint"):
  returns a logical indicating if x and y are "exactly equal". Compared to the default method
  (which is the base function, hence see identical), this method handles the .xData slots of
  x and y specially: by default (if extptr.as.ref is FALSE), it does not test for equality of the
  stored pointers but rather for entrywise equality of the pointed to arrays. Hence by default the
  .xData slots are compared as if they were traditional numeric or complex vectors.
is.array signature(x = "flint"):
  returns a logical indicating if x has a non-NULL dim slot.
is.matrix signature(x = "flint"):
  returns a logical indicating if x has a dim slot of length 2.
is.na<- signature(x = "flint"):
  returns the value of x after x[value] <- na, where na is an NA of integer, double, or complex
  type, depending on the class of x.
isSymmetric signature(x = "flint"):
  returns a logical indicating if x is a Hermitian matrix or if x is a symmetric matrix, depend-
  ing on optional argument trans, following the documented behaviour of the S3 method for
  traditional matrices, hence see isSymmetric.
length signature(x = "flint"):
  returns flintLength(x, exact = FALSE).
length<- signature(x = "flint"):
  returns a flint vector of length given by the second argument value. The first min(length(x),
  value) elements are copied from x and the remaining elements are initialized to zero.

```

```

match signature(x = "flint", table = "flint"):
  signature(x = "flint", table = "ANY"):
  signature(x = "ANY", table = "flint"):
  returns an integer vector matching x to table after coercing to a common class then "match
  transforming" with mtfrm. The behaviour is parallel to that of the base function, hence see
  match.

mtfrm signature(x = "flint"):
  returns format(x, base = 62L, digits = 0L, digits.mag = 0L), a character vector repre-
  senting the elements of x exactly in base 62 (chosen over smaller bases to reduce the number
  of characters in the output); see also format-methods.

names signature(x = "flint"):
  returns the value of the names slot.

names<- signature(x = "flint", value = "NULL"):
  returns x with names slot set to NULL.

names<- signature(x = "flint", value = "character"):
  returns x with names slot set to value. Attributes of value are stripped. NA\_character\_ are
  appended to value if its length is less than the length of x. An error is signaled if its length is
  greater.

norm signature(x = "flint"):
  returns the matrix norm of x as a flint vector of length 1. The class of the return value can
  depend on the norm type indicated by argument type; see norm.

print signature(x = "flint"):
  prints format\(x\) without quotes and returns x invisibly. The output has a header listing the
  class and length of x and the address stored by its .xData slot. If the output might be differ-
  enced by Rdiff, then one can set optional argument Rdiff to TRUE to indicate that the address
  should be formatted as <pointer: 0x...> rather than as 0x..., as the longer format is recog-
  nized and ignored by Rdiff. The default value NULL is equivalent to getOption("flint.Rdiff",
  FALSE). For greater control over output, consider doing print(format(x, ...), ...) in-
  stead of print(x, ...).

quantile signature(x = "flint"):
  returns a flint vector containing sample quantiles computed according to additional argu-
  ments probs and type; see quantile. Currently, an error is signaled for x of length zero
  and x containing NaN.

rbind2 signature(x = "flint", y = "flint"):
  signature(x = "flint", y = "ANY"):
  signature(x = "ANY", y = "flint"):
  returns rbind.flint\(x, y, ...\), the vertical concatenation of x and y. These methods are
  dispatched by rbind in case of S3 dispatch ambiguities; see rbind2.

rep signature(x = "flint"):
  repeats x (or elements of x) according to optional arguments times, length.out, and each.
  The behaviour is parallel to that of the internal default method, hence see rep. One difference
  is that rep(0-length, length.out=nonzero) signals an error, because the underlying C types
  have no representation for missing values.

rep.int, rep_len signature(x = "flint"):
  analogues of rep(x, times=) and rep(x, length.out=) not preserving names, faster than
  rep when x has names.

```

`seq` signature(... = "flint"):
 generates flint vectors whose elements are equally spaced. This method is dispatched by calls to `seq` or `seq.int` in which the first positional argument is a flint vector. Accepted usage is any of

```
seq(length.out=)
seq(length.out=, by=)
seq(from=, to=)
seq(from=, to=, by=)
seq(from=, to=, length.out=)
seq(from=, by=, length.out=)
seq(to=, by=, length.out=)
```

where `length.out=n` and `along.with=x` are equivalent for `x` of length `n`. Good users name all arguments.

`sequence` signature(nvec = "flint"):
 returns the concatenation of `seq(from = from[i], by = by[i], length.out = nvec[i])` after recycling arguments `nvec`, `from`, and `by` to a common length.

`show` signature(object = "flint"):
 prints `format(object)` and returns NULL invisibly.

`summary` signature(object = "flint"):
 returns a flint vector containing the minimum, first quartile, median, mean, third quartile, maximum, and (if nonzero) the number of NaN, unless object is complex (inherits from `acf` or `acb`) or `x` has error bounds (inherits from `arb` or `acb`) or optional argument `triple` is TRUE, in which case the value is just `flintTriple()` with names.

`t` signature(x = "flint"):
 returns the transpose of `x` if `x` is a matrix, handling non-array `x` as `length(x)-by-1` matrices.

`unique` signature(x = "flint"):
 if `x` is not an array or `MARGIN` is empty, returns a vector containing the unique elements of `x`; otherwise, returns an array containing the unique splits of `x` by margin `MARGIN`. Elements (splits) of `x` are considered distinct if the corresponding elements (splits) of `mtfrm(x)` are not identical.

Methods are on purpose *not* defined for generic functions whose default methods correctly handle objects inheriting from virtual class `flint`, typically by calling *other* generic functions for which methods *are* defined. Examples are `as.character`, `as.list`, `diff`, `rev`, `seq.int`, `sort`, and `split`.

See Also

The nonvirtual subclasses: `ulong`, `slong`, `fmpz`, `fmpq`, `mag`, `arf`, `acf`, `arb`, and `acb`.

Examples

```
showClass("flint")
showMethods(classes = "flint")
```


Description

Class `fmpq` extends virtual class `flint`. It represents vectors of arbitrary precision rational numbers. Elements are specified by a pair of arbitrary precision signed integers: a numerator and a positive, coprime denominator. There is no representation for R's missing value `NA_integer_`.

Usage

```
## Class generator functions
```

```
fmpq(x = 0L, length = 0L, names = NULL, num = 0L, den = 1L)
```

```
fmpq.array(x = 0L, dim = length(x), dimnames = NULL, num = 0L, den = 1L)
```

Arguments

<code>x</code>	an atomic or <code>flint</code> vector containing data for conversion to <code>fmpq</code> .
<code>length</code>	a numeric vector of length one giving the length of the return value. If that exceeds the length of <code>x</code> , then <code>x</code> is recycled. Non-integer values are rounded in the direction of zero.
<code>names</code>	the names slot of the return value, either <code>NULL</code> or a character vector of equal length. Non-character names are coerced to character.
<code>dim</code>	the dim slot of the return value, an integer vector of nonzero length. If the product exceeds the length of <code>x</code> , then <code>x</code> is recycled. Non-integer numeric <code>dim</code> are coerced to integer.
<code>dimnames</code>	the dimnames slot of the return value, either <code>NULL</code> or a list of length equal to the length of <code>dim</code> . The components are either <code>NULL</code> or character vectors of length given by <code>dim</code> . Non-character vector components of <code>dimnames</code> are coerced to character.
<code>num, den</code>	atomic or <code>flint</code> vectors containing data for conversion to <code>fmpz</code> . Use these instead of <code>x</code> for initialization “by parts” (numerator and denominator).

Details

The class generator function has six distinct usages:

```
fmpq()
fmpq(length=)
fmpq(x)
fmpq(x, length=)
fmpq(num=, den=)
fmpq(num=, den=, length=)
```

The first usage generates an empty vector. The second usage generates a zero vector of the indicated length. The third usage converts x , preserving dimensions, dimension names, and names. The fourth usage converts x , recycling its elements to the indicated length and discarding its dimensions, dimension names, and names. The fifth and sixth usages, in which either of `num` and `den` can be missing, use `fmpz(num)` and `fmpz(den)` to separately initialize the numerators and denominators of the `fmpq` return value.

Attempts to recycle `num`, `den`, or `x` of length zero to nonzero length are an error.

Usage of `fmpq.array` is modelled after `array`.

Value

An `fmpq` vector, possibly an array; see ‘Details’.

Conversion

Real numbers and real parts of complex numbers are converted exactly, as floating-point numbers are rational by definition. Imaginary parts of complex numbers are discarded.

Character strings are converted using function `mpq_set_str` from the GNU MP library with argument base set to 0; see <https://gmplib.org/manual/Initializing-Rationals>.

An error is signaled if elements of `num`, `den`, or `x` are NaN, $-\infty$, or ∞ or if elements of `den` are 0.

Slots

`.xData`, `dim`, `dimnames`, `names` inherited from virtual class `flint`.

Methods

```
! signature(x = "fmpq"):
    equivalent to (but faster than) x == 0.

%*, crossprod, tcrossprod signature(x = "fmpq", y = "fmpq"):
    signature(x = "fmpq", y = "ANY"):
    signature(x = "ANY", y = "fmpq"):
    matrix products. The “other” operand must be atomic or inherit from virtual class flint.
    crossprod and tcrossprod behave as if y = x when y is missing or NULL. Operands are
    promoted as necessary and must be conformable (have compatible dimensions). Non-array
    operands of length k are handled as 1-by-k or k-by-1 matrices depending on the call.

+ signature(e1 = "fmpq", e2 = "missing"):
    returns a copy of the argument.

- signature(e1 = "fmpq", e2 = "missing"):
    returns the negation of the argument.

Complex signature(z = "fmpq"):
    mathematical functions of one argument; see S4groupGeneric. Member functions requiring
    promotion to a floating-point type may not be implemented.

Math signature(x = "fmpq"):
    mathematical functions of one argument; see S4groupGeneric. Member functions requiring
    promotion to a floating-point type may not be implemented.
```

Math2 `signature(x = "fmpq")`:
 decimal rounding according to a second argument `digits`; see [S4groupGeneric](#). There are just two member member functions: [round](#), [signif](#).

Ops `signature(e1 = "fmpq", e2 = "fmpq")`:
`signature(e1 = "fmpq", e2 = "ANY")`:
`signature(e1 = "ANY", e2 = "fmpq")`:
 binary arithmetic, comparison, and logical operators; see [S4groupGeneric](#). The “other” operand must be atomic or inherit from virtual class [flint](#). Operands are promoted as necessary. Array operands must be conformable (have identical dimensions). Non-array operands are recycled.

Summary `signature(x = "fmpq")`:
 univariate summary statistics; see [S4groupGeneric](#). The return value is a logical vector of length 1 (`any`, `all`) or an `fmpq` vector of length 1 or 2 (`sum`, `prod`, `min`, `max`, `range`).

anyNA `signature(x = "fmpq")`:
 returns `FALSE`, as `fmpq` has no representation for `NaN`.

as.vector `signature(x = "fmpq")`:
 returns `as.vector(y, mode)`, where `y` is a double vector containing the result of converting each element of `x` to the range of double, rounding if the value is not exactly representable in double precision. The rounding mode is to the nearest representable number in the direction of zero, unless the element exceeds `.Machine[["double.xmax"]]` in absolute value, in which case `-Inf` or `Inf` is introduced with a warning. Coercion to types `"character"`, `"symbol"` (synonym `"name"`), `"pairlist"`, `"list"`, and `"expression"`, which are not “number-like”, is handled specially. See also [asVector](#).

backsolve `signature(r = "fmpq", x = "fmpq")`:
`signature(r = "fmpq", x = "ANY")`:
`signature(r = "ANY", x = "fmpq")`:
 solution of the triangular system `op2(op1(r)) %*% y = x`, where `op1=ifelse(upper.tri, triu, tril)` and `op2=ifelse(transpose, t, identity)` and `upper.tri` and `transpose` are optional logical arguments with default values `TRUE` and `FALSE`, respectively. The “other” operand must be atomic or inherit from virtual class [flint](#). If `x` is missing, then the return value is the inverse of `op2(op1(r))`, as if `x` were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array `x` are handled as `length(x)-by-1` matrices. If `r` and (if not missing) `x` are both formally rational, then the solution is exact and the return value is an [fmpq](#) matrix.

chol `signature(x = "fmpq")`:
 coerces `x` to class [arf](#) and dispatches.

chol2inv `signature(x = "fmpq")`:
 returns the inverse of the positive definite matrix whose upper triangular Cholesky factor is the upper triangular part of `x`. The return value is the exact inverse, being computed as `tcrossprod(backsolve(x))`.

coerce `signature(from = "ANY", to = "fmpq")`:
 returns the value of `fmpq(from)`.

colSums, colMeans `signature(x = "fmpq")`:
 returns an `fmpq` vector or array containing the column sums or means of `x`, defined as sums or means over dimensions `1:dims`.

`colSums` signature($x = \text{"fmpq"}$):
 returns an `fmpq` vector or array containing the column sums of x , defined as sums over dimensions $1:\text{dims}$.

`colMeans` signature($x = \text{"fmpq"}$):
 returns an `fmpq` vector or array containing the column means of x , defined as means over dimensions $1:\text{dims}$.

`det` signature($x = \text{"fmpq"}$):
 returns the determinant of x as an `fmpq` vector of length 1.

`determinant` signature($x = \text{"fmpq"}$):
 returns a list with components `modulus` and `sign` specifying the determinant of x , following the **base** function, hence see `determinant`. Note that `det(x)` and `determinant(x, logarithm = FALSE)` are exact, but `determinant(x)` is not in general due to rounding.

`format` signature($x = \text{"fmpq"}$):
 returns a character vector suitable for printing, using string format `"p/q"`. Optional arguments control the output; see `format-methods`.

`is.finite` signature($x = \text{"fmpq"}$):
 returns a logical vector whose elements are all `TRUE`, as `fmpq` has no representation for `NaN`, `-Inf`, and `Inf`.

`is.infinite, is.na, is.nan` signature($x = \text{"fmpq"}$):
 returns a logical vector whose elements are all `FALSE`, as `fmpq` has no representation for `NaN`, `-Inf`, and `Inf`.

`is.unsorted` signature($x = \text{"fmpq"}$):
 returns a logical indicating if x is not sorted in nondecreasing order (increasing order if optional argument `strictly` is set to `TRUE`).

`mean` signature($x = \text{"fmpq"}$):
 returns the arithmetic mean. An error is signaled if the argument length is 0, because the return type is `fmpq` which cannot represent the result of division by 0.

`rowSums, rowMeans` signature($x = \text{"fmpq"}$):
 returns an `fmpq` vector or array containing the row sums or means of x , defined as sums or means over dimensions $(\text{dims}+1):\text{length}(\text{dim}(x))$.

`solve` signature($a = \text{"fmpq"}$, $b = \text{"fmpq"}$):
 signature($a = \text{"fmpq"}$, $b = \text{"ANY"}$):
 signature($a = \text{"ANY"}$, $b = \text{"fmpq"}$):
 solution of the general system $a \%*\% x = b$. The “other” operand must be atomic or inherit from virtual class `flint`. If b is missing, then the return value is the inverse of a , as if b were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array b are handled as `length(b)`-by-1 matrices. If a and (if not missing) b are both formally rational, then the solution is exact and the return value is an `fmpq` matrix.

References

The FLINT documentation of the underlying C type: <https://flintlib.org/doc/fmpq.html>

See Also

Virtual class [flint](#). Generic functions [Num](#) and [Den](#) and their replacement forms for getting and setting numerators and denominators.

Examples

```
showClass("fmpz")
showMethods(classes = "fmpz")
```

fmpz-class

*Arbitrary Precision Signed Integers***Description**

Class fmpz extends virtual class [flint](#). It represents vectors of arbitrary precision signed integers. There is no representation for R's missing value [NA_integer_](#).

Usage

```
## Class generator functions

fmpz(x = 0L, length = 0L, names = NULL)

fmpz.array(x = 0L, dim = length(x), dimnames = NULL)
```

Arguments

x	an atomic or flint vector containing data for conversion to fmpz.
length	a numeric vector of length one giving the length of the return value. If that exceeds the length of x, then x is recycled. Non-integer values are rounded in the direction of zero.
names	the names slot of the return value, either NULL or a character vector of equal length. Non-character names are coerced to character.
dim	the dim slot of the return value, an integer vector of nonzero length. If the product exceeds the length of x, then x is recycled. Non-integer numeric dim are coerced to integer.
dimnames	the dimnames slot of the return value, either NULL or a list of length equal to the length of dim. The components are either NULL or character vectors of length given by dim. Non-character vector components of dimnames are coerced to character.

Details

The class generator function has four distinct usages:

```
fmpz()
fmpz(length=)
fmpz(x)
fmpz(x, length=)
```

The first usage generates an empty vector. The second usage generates a zero vector of the indicated length. The third usage converts *x*, preserving dimensions, dimension names, and names. The fourth usage converts *x*, recycling its elements to the indicated length and discarding its dimensions, dimension names, and names. Attempts to recycle *x* of length zero to nonzero length are an error.

Usage of `fmpz.array` is modelled after [array](#).

Value

An fmpz vector, possibly an array; see ‘Details’.

Conversion

Real numbers and real parts of complex numbers are rounded in the direction of 0. Imaginary parts of complex numbers are discarded.

Character strings are converted using function `mpz_set_str` from the GNU MP library with argument base set to 0; see <https://gmplib.org/manual/Assigning-Integers>.

An error is signaled if elements of *x* are NaN, -Inf, or Inf.

Slots

`.xData`, `dim`, `dimnames`, `names` inherited from virtual class [flint](#).

Methods

```
! signature(x = "fmpz"):
  equivalent to (but faster than) x == 0.

%%, crossprod, tcrossprod signature(x = "fmpz", y = "fmpz"):
  signature(x = "fmpz", y = "ANY"):
  signature(x = "ANY", y = "fmpz"):
  matrix products. The “other” operand must be atomic or inherit from virtual class flint.
  crossprod and tcrossprod behave as if y = x when y is missing or NULL. Operands are
  promoted as necessary and must be conformable (have compatible dimensions). Non-array
  operands of length k are handled as 1-by-k or k-by-1 matrices depending on the call.

+ signature(e1 = "fmpz", e2 = "missing"):
  returns a copy of the argument.

- signature(e1 = "fmpz", e2 = "missing"):
  returns the negation of the argument.
```

Complex signature(z = "fmpz"):
 mathematical functions of one argument; see [S4groupGeneric](#). Member functions requiring promotion to a floating-point type may not be implemented.

Math signature(x = "fmpz"):
 mathematical functions of one argument; see [S4groupGeneric](#). Member functions requiring promotion to a floating-point type may not be implemented.

Math2 signature(x = "fmpz"):
 decimal rounding according to a second argument digits; see [S4groupGeneric](#). There are just two member member functions: [round](#), [signif](#).

Ops signature(e1 = "fmpz", e2 = "fmpz"):
 signature(e1 = "fmpz", e2 = "ANY"):
 signature(e1 = "ANY", e2 = "fmpz"):
 binary arithmetic, comparison, and logical operators; see [S4groupGeneric](#). The “other” operand must be atomic or inherit from virtual class [flint](#). Operands are promoted as necessary. Array operands must be conformable (have identical dimensions). Non-array operands are recycled.

Summary signature(x = "fmpz"):
 univariate summary statistics; see [S4groupGeneric](#). The return value is a logical vector of length 1 (any, all) or an fmpz vector of length 1 or 2 (sum, prod, min, max, range).

anyNA signature(x = "fmpz"):
 returns FALSE, as fmpz has no representation for NaN.

as.vector signature(x = "fmpz"):
 returns as.vector(y, mode), where y is a double vector containing the result of converting each element of x to the range of double, rounding if the value is not exactly representable in double precision. The rounding mode is to the nearest representable number in the direction of zero, unless the element exceeds `.Machine[["double.xmax"]]` in absolute value, in which case `-Inf` or `Inf` is introduced with a warning. Coercion to types "character", "symbol" (synonym "name"), "pairlist", "list", and "expression", which are not “number-like”, is handled specially. See also [asVector](#).

backsolve signature(r = "fmpz", x = "fmpz"):
 signature(r = "fmpz", x = "ANY"):
 signature(r = "ANY", x = "fmpz"):
 solution of the triangular system `op2(op1(r)) %*% y = x`, where `op1=ifelse(upper.tri, triu, tril)` and `op2=ifelse(transpose, t, identity)` and `upper.tri` and `transpose` are optional logical arguments with default values TRUE and FALSE, respectively. The “other” operand must be atomic or inherit from virtual class [flint](#). If x is missing, then the return value is the inverse of `op2(op1(r))`, as if x were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array x are handled as `length(x)-by-1` matrices. If r and (if not missing) x are both formally rational, then the solution is exact and the return value is an [fmpq](#) matrix.

chol signature(x = "fmpz"):
 coerces x to class [arf](#) and dispatches.

chol2inv signature(x = "fmpz"):
 returns the inverse of the positive definite matrix whose upper triangular Cholesky factor is the upper triangular part of x. The return value is the exact inverse, being computed as `tcrossprod(backsolve(x))`.

`coerce` signature(`from` = "ANY", `to` = "fmpz"): returns the value of `fmpz(from)`.

`colSums` signature(`x` = "fmpz"): returns an `fmpz` vector or array containing the column sums of `x`, defined as sums over dimensions 1:dim.

`colMeans` signature(`x` = "fmpz"): returns an `fmpq` vector or array containing the column means of `x`, defined as means over dimensions 1:dim.

`det` signature(`x` = "fmpz"): returns the determinant of `x` as an `fmpz` vector of length 1.

`determinant` signature(`x` = "fmpz"): returns a list with components `modulus` and `sign` specifying the determinant of `x`, following the `base` function, hence see `determinant`. Note that `det(x)` and `determinant(x, logarithm = FALSE)` are exact, but `determinant(x)` is not in general due to rounding.

`format` signature(`x` = "fmpz"): returns a character vector suitable for printing. Optional arguments control the output; see `format-methods`.

`is.finite` returns a logical vector whose elements are all TRUE, as `fmpz` has no representation for NaN, -Inf, and Inf.

`is.infinite, is.na, is.nan` signature(`x` = "fmpz"): returns a logical vector whose elements are all FALSE, as `fmpz` has no representation for NaN, -Inf, and Inf.

`is.unsorted` signature(`x` = "fmpz"): returns a logical indicating if `x` is not sorted in nondecreasing order (increasing order if optional argument `strictly` is set to TRUE).

`mean` signature(`x` = "fmpz"): returns the arithmetic mean. An error is signaled if the argument length is 0, because the return type is `fmpq` which cannot represent the result of division by 0.

`rowSums` signature(`x` = "fmpz"): returns an `fmpz` vector or array containing the row sums of `x`, defined as sums over dimensions (dim+1):length(dim(x)).

`rowMeans` signature(`x` = "fmpz"): returns an `fmpq` vector or array containing the row means of `x`, defined as means over dimensions (dim+1):length(dim(x)).

`solve` signature(`a` = "fmpz", `b` = "fmpz"): signature(`a` = "fmpz", `b` = "ANY"): signature(`a` = "ANY", `b` = "fmpz"): solution of the general system `a %*% x = b`. The "other" operand must be atomic or inherit from virtual class `flint`. If `b` is missing, then the return value is the inverse of `a`, as if `b` were the identity matrix. Operands are promoted as necessary and must be conformable (have compatible dimensions). Non-array `b` are handled as length(`b`)-by-1 matrices. If `a` and (if not missing) `b` are both formally rational, then the solution is exact and the return value is an `fmpq` matrix.

References

The FLINT documentation of the underlying C type: <https://flintlib.org/doc/fmpz.html>

See Also

Virtual class [flint](#).

Examples

```
showClass("fmpz")
showMethods(classes = "fmpz")
```

format-methods

Format FLINT-type Numbers as Strings

Description

Format a [flint](#) vector for pretty printing.

Usage

```
## S4 method for signature 'ulong'
format(x, base = 10L, ...)
## S4 method for signature 'slong'
format(x, base = 10L, ...)
## S4 method for signature 'fmpz'
format(x, base = 10L, ...)
## S4 method for signature 'fmpq'
format(x, base = 10L, ...)
## S4 method for signature 'mag'
format(x, base = 10L, digits.mag = NULL,
       sep = NULL, rnd = flintRnd(), ...)
## S4 method for signature 'arf'
format(x, base = 10L, digits = NULL,
       sep = NULL, rnd = flintRnd(), ...)
## S4 method for signature 'acf'
format(x, base = 10L, digits = NULL,
       sep = NULL, rnd = flintRnd(), ...)
## S4 method for signature 'arb'
format(x, base = 10L, digits = NULL, digits.mag = NULL,
       sep = NULL, rnd = flintRnd(), ...)
## S4 method for signature 'acb'
format(x, base = 10L, digits = NULL, digits.mag = NULL,
       sep = NULL, rnd = flintRnd(), ...)
```

Arguments

<code>x</code>	a flint vector.
<code>base</code>	an integer from 2 to 62 indicating a base for output. Values 2, 10, and 16 correspond to binary, decimal, and hexadecimal output. Digits are represented by characters ‘[0-9A-Za-z]’, in that significance order, hence the maximum $10+26+26=62$.
<code>digits, digits.mag</code>	an integer indicating how many digits of the significand are reported when formatting floating-point numbers. arf and arf components of acf , arb , and acb use <code>digits</code> . mag and mag components of arb and acb use <code>digits.mag</code> . When more than one digit is printed, a radix point is inserted after the first digit. Value 0 is equivalent to the minimum integer <code>d</code> such that all elements of <code>x</code> are represented exactly by <code>d</code> digits in the specified base. The default values <code>NULL</code> are equivalent to <code>getOption("digits")</code> and <code>getOption("digits.mag", 4L)</code> .
<code>sep</code>	a nonempty character string used to separate the significand from the exponent. The default value <code>NULL</code> is equivalent to "e" for base equal to 10 and to "@" for all other bases.
<code>rnd</code>	a nonempty character string whose first character indicates a rounding mode. Methods for arb and acb require <code>rnd</code> of length 2, specifying rounding modes separately for midpoints and radii. See flintRnd for information about valid character strings.
<code>...</code>	further optional arguments, though these are currently unused.

Value

A character vector containing ASCII strings of equal length, preserving the length, dimensions, dimension names, and names of `x`.

Examples

```
q <- fmpq(num = c(-1L, 1L) * 0:5, den = 1:6)
for (b in 2:8) {
  cat("base = ", b, ":\n", sep = "")
  print(format(q, base = b), quote = FALSE, width = 12L)
}

z <- acb(real = arb(mid = pi, rad = 0.5 * pi))
format(z)
format(z, base = 62L, sep = "*[62]^")
strsplit(format(Re(z), digits = 80L), "[( ))")[1L][c(FALSE, TRUE)]
```

Description

Class `mag` extends virtual class `flint`. It represents vectors of fixed precision error bounds. Elements are unsigned floating-point numbers with a 30-bit significand and an arbitrary precision exponent. The underlying C type can represent Inf but not NaN.

Usage

```
## Class generator functions
```

```
mag(x = 0, length = 0L, names = NULL)
```

```
mag.array(x = 0, dim = length(x), dimnames = NULL)
```

Arguments

<code>x</code>	an atomic or <code>flint</code> vector containing data for conversion to <code>mag</code> .
<code>length</code>	a numeric vector of length one giving the length of the return value. If that exceeds the length of <code>x</code> , then <code>x</code> is recycled. Non-integer values are rounded in the direction of zero.
<code>names</code>	the names slot of the return value, either <code>NULL</code> or a character vector of equal length. Non-character names are coerced to character.
<code>dim</code>	the dim slot of the return value, an integer vector of nonzero length. If the product exceeds the length of <code>x</code> , then <code>x</code> is recycled. Non-integer numeric <code>dim</code> are coerced to integer.
<code>dimnames</code>	the dimnames slot of the return value, either <code>NULL</code> or a list of length equal to the length of <code>dim</code> . The components are either <code>NULL</code> or character vectors of length given by <code>dim</code> . Non-character vector components of <code>dimnames</code> are coerced to character.

Details

The class generator function has four distinct usages:

```
mag()
mag(length=)
mag(x)
mag(x, length=)
```

The first usage generates an empty vector. The second usage generates a zero vector of the indicated length. The third usage converts `x`, preserving dimensions, dimension names, and names. The fourth usage converts `x`, recycling its elements to the indicated length and discarding its dimensions, dimension names, and names. Attempts to recycle `x` of length zero to nonzero length are an error.

Usage of `mag.array` is modelled after `array`.

Value

A `mag` vector, possibly an array; see ‘Details’.

Conversion

Magnitudes of real numbers and real parts of complex numbers are rounded in the direction of 0 or Inf according to the default rounding mode set by `flintRnd`. Imaginary parts of complex numbers are discarded.

Character strings are converted using function `mpfr_strtobr` from the GNU MPFR library with argument base set to 0 and argument `rnd` set according to the default rounding mode; see <https://www.mpfr.org/mpfr-current/mpfr.html#Assignment-Functions>.

An error is signaled if elements of `x` are NaN.

Slots

`.xData`, `dim`, `dimnames`, `names` inherited from virtual class `flint`.

Methods

```
! signature(x = "mag"):
  equivalent to (but faster than) x == 0.

%*, crossprod, tcrossprod signature(x = "mag", y = "mag"):
  signature(x = "mag", y = "ANY"):
  signature(x = "ANY", y = "mag"):
  matrix products. The "other" operand must be atomic or inherit from virtual class flint.
  crossprod and tcrossprod behave as if y = x when y is missing or NULL. Operands are
  promoted as necessary and must be conformable (have compatible dimensions). Non-array
  operands of length k are handled as 1-by-k or k-by-1 matrices depending on the call.

+ signature(e1 = "mag", e2 = "missing"):
  returns a copy of the argument.

- signature(e1 = "mag", e2 = "missing"):
  returns a copy of the argument, to be consistent with the binary operation which returns an
  upper bound for the absolute value of the difference.

Complex signature(z = "mag"):
  mathematical functions of one argument; see S4groupGeneric. The return value is an upper
  bound for the absolute value of the exact answer.

Math signature(x = "mag"):
  mathematical functions of one argument; see S4groupGeneric. The return value is an up-
  per bound for the absolute value of the exact answer. Notably, the (inverse) trigonometric,
  (inverse) hyperbolic, and gamma-related member functions are not yet implemented. Users
  wanting those can (for now) operate on arb(x).

Math2 signature(x = "mag"):
  decimal rounding according to a second argument digits; see S4groupGeneric. There are
  just two member functions: round, signif. The return value is an upper bound for the exact
  answer.

Ops signature(e1 = "mag", e2 = "mag"):
  signature(e1 = "mag", e2 = "ANY"):
  signature(e1 = "ANY", e2 = "mag"):
  binary arithmetic, comparison, and logical operators; see S4groupGeneric. The "other"
```

operand must be atomic or inherit from virtual class [flint](#). Operands are promoted as necessary. Array operands must be conformable (have identical dimensions). Non-array operands are recycled. For arithmetic, the return value is a mag vector only if both operands are mag vectors. In that case, the return value is an upper bound for the absolute value of the exact answer. Users wanting “standard” floating-point arithmetic must ensure that at least one operand is not a mag vector.

`Summary` `signature(x = "mag")`:

univariate summary statistics; see [S4groupGeneric](#). The return value is a logical vector of length 1 (any, all) or an mag vector of length 1 or 2 (sum, prod, min, max, range). For sum and prod, the return value is an upper bound for the exact answer.

`anyNA` `signature(x = "mag")`:

returns FALSE, as mag has no representation for NaN.

`as.vector` `signature(x = "mag")`:

returns `as.vector(y, mode)`, where `y` is a double vector containing the result of converting each element of `x` to the range of double, rounding in the direction of Inf, not always to nearest. Coercion to types "character", "symbol" (synonym "name"), "pairlist", "list", and "expression", which are not “number-like”, is handled specially. See also [asVector](#).

`backsolve` `signature(r = "mag", x = "mag")`:

`signature(r = "mag", x = "ANY")`:

`signature(r = "ANY", x = "mag")`:

coerces the mag operand to class [arf](#), [acf](#), [arb](#), or [acb](#) (depending on the class of the other operand) and dispatches.

`chol`, `chol2inv` `signature(x = "mag")`:

coerces `x` to class [arf](#) and dispatches.

`coerce` `signature(from = "ANY", to = "mag")`:

returns the value of `mag(from)`.

`colSums`, `colMeans` `signature(x = "mag")`:

returns a mag vector or array containing upper bounds on the column sums or means of `x`, defined as sums or means over dimensions 1:dim.

`det`, `determinant` `signature(x = "mag")`:

coerces `x` to class [arf](#) and dispatches.

`format` `signature(x = "mag")`:

returns a character vector suitable for printing, using scientific format. Optional arguments control the output; see [format-methods](#).

`is.finite` `signature(x = "mag")`:

returns a logical vector indicating which elements of `x` are not Inf.

`is.infinite` `signature(x = "mag")`:

returns a logical vector indicating which elements of `x` are Inf.

`is.na`, `is.nan` `signature(x = "mag")`:

returns a logical vector whose elements are all FALSE, as mag has no representation for NaN.

`is.unsorted` `signature(x = "mag")`:

returns a logical indicating if `x` is not sorted in nondecreasing order (increasing order if optional argument `strictly` is set to TRUE).

```
log signature(x = "mag"):
  returns an upper bound for the absolute value of the logarithm of the argument. The natural
  logarithm is computed by default (when optional argument base is unset).

mean signature(x = "mag"):
  returns an upper bound for the arithmetic mean.

rowSums, rowMeans signature(x = "mag"):
  returns a mag vector or array containing upper bounds on the row sums or means of x, defined
  as sums or means over dimensions (dims+1):length(dim(x)).

solve signature(a = "mag", b = "mag"):
  signature(a = "mag", b = "ANY"):
  signature(a = "ANY", b = "mag"):
  coerces the mag operand to class arf, acf, arb, or acb (depending on the class of the other
  operand) and dispatches.
```

References

The FLINT documentation of the underlying C type: <https://flintlib.org/doc/mag.html>

Johansson, F. (2017). Arb: efficient arbitrary-precision midpoint-radius interval arithmetic. *IEEE Transactions on Computers*, 66(8), 1281-1292. doi:10.1109/TC.2017.2690633

See Also

Virtual class [flint](#).

Examples

```
showClass("mag")
showMethods(classes = "mag")
```

OptionalCharacter-class

Unions of 'NULL' and Vector Classes

Description

Class unions in the style of [OptionalFunction](#) from package **methods**, whose purpose is to allow slots `dim`, `dimnames`, and `names` of virtual class [flint](#) to be `NULL` or a vector of suitable type.

`OptionalInteger`, `OptionalList`, and `OptionalCharacter` are the unions of `NULL` and integer, list, and character, respectively.

Examples

```
showClass("OptionalInteger")
showClass("OptionalList")
(oc <- getClass("OptionalCharacter"))

stopifnot(isVirtualClass(oc),
          isClassUnion(oc),
          all(c("NULL", "character") %in% names(oc@subclasses)),
          any(extends("NULL") == "OptionalCharacter"),
          any(extends("character") == "OptionalCharacter"))

getClass("flint")@slots
```

Part

Get or Set One Part of a Vector

Description

The subclasses of virtual class `flint` are interfaces to `C` types in the FLINT `C` library. For types implemented recursively as `C` structs, it is often very natural to get and set the struct members. The functions documented here provide support for this common operation; they are all S4 generic.

Usage

```
Num(q)
Num(q) <- value
Den(q)
Den(q) <- value

Mid(x)
Mid(x) <- value
Rad(x)
Rad(x) <- value

Real(z)
Real(z) <- value
Imag(z)
Imag(z) <- value
```

Arguments

- | | |
|---|--|
| q | a vector-like R object with elements representing quotients of numbers. Package flint provides methods for class <code>fmprq</code> . |
| x | a vector-like R object with elements representing balls in a metric space. Package flint provides methods for class <code>arb</code> . |
| z | a vector-like R object with elements representing complex numbers. Package flint provides methods for classes <code>acf</code> and <code>acb</code> . |

value a vector-like **R** object; the replacement value. Methods in package **flint** support atomic vectors and vectors inheriting from virtual class **flint**, of length equal to 1 or the length of the argument.

Details

Num and Den extract **fmpz** numerators and denominators from **fmpq** *q*. The replacement form of Num constructs a new **fmpq** vector from value (coerced to **fmpz**) and Den(*q*). The replacement form of Den constructs a new **fmpq** vector from Num(*q*) and value (coerced to **fmpz**).

Mid and Rad extract **arf** midpoints and **mag** radii from **arb** *x*. The replacement form of Mid constructs a new **arb** vector from value (coerced to **arf**) and Rad(*x*). The replacement form of Rad constructs a new **arb** vector from Mid(*x*) and value (coerced to **mag**).

Real and Imag extract **arf** real and imaginary parts from **acf** *z* and **arb** real and imaginary parts from **acb** *z*. The replacement form of Real constructs a new **acf** or **acb** vector from value (coerced to **arf** or **arb**) and Imag(*z*). The replacement form of Imag constructs a new **acf** or **acb** vector from Real(*z*) and value (coerced to **arf** or **arb**).

For convenience, Mid and its replacement form also work for **acb** *x*, getting and setting the complex midpoint defined by the midpoints of the real and imaginary parts of *x*.

Value

Num, Den, Mid, Rad, Real, and Imag and their replacement forms return a vector-like **R** object preserving the length, dimensions, dimension names, and names of the argument. See ‘Details’ for behaviour specific to methods in package **flint**.

See Also

Virtual class **flint**.

Examples

```
(q <- q. <- fmpq(num = 1:10, den = 2L))
Num(q)
Den(q)
Num(q) <- Den(q)
q
(m <- Num(q))
(n <- Den(q))
stopifnot(m == 1L, n == 1L, q == 1L)
```

ulong-class

Fixed Precision Unsigned and Signed Integers

Description

Classes **ulong** and **slong** extend virtual class **flint**. They represent vectors of fixed precision unsigned and signed integers, respectively. The integer size is 32 or 64 bits, depending on the ABI; see **flintABI**. There is no representation for R’s missing value **NA_integer_**.

Usage

```
## Class generator functions

ulong(x = 0L, length = 0L, names = NULL)
slong(x = 0L, length = 0L, names = NULL)

ulong.array(x = 0L, dim = length(x), dimnames = NULL)
slong.array(x = 0L, dim = length(x), dimnames = NULL)
```

Arguments

x	an atomic or flint vector containing data for conversion to ulong or slong.
length	a numeric vector of length one giving the length of the return value. If that exceeds the length of x, then x is recycled. Non-integer values are rounded in the direction of zero.
names	the names slot of the return value, either NULL or a character vector of equal length. Non-character names are coerced to character.
dim	the dim slot of the return value, an integer vector of nonzero length. If the product exceeds the length of x, then x is recycled. Non-integer numeric dim are coerced to integer.
dimnames	the dimnames slot of the return value, either NULL or a list of length equal to the length of dim. The components are either NULL or character vectors of length given by dim. Non-character vector components of dimnames are coerced to character.

Details

The class generator functions have four distinct usages:

```
ulong()
ulong(length=)
ulong(x)
ulong(x, length=)

slong()
slong(length=)
slong(x)
slong(x, length=)
```

The first usage generates an empty vector. The second usage generates a zero vector of the indicated length. The third usage converts x, preserving dimensions, dimension names, and names. The fourth usage converts x, recycling its elements to the indicated length and discarding its dimensions, dimension names, and names. Attempts to recycle x of length zero to nonzero length are an error.

Usage of `ulong.array` and `slong.array` is modelled after [array](#).

Value

A ulong or slong vector, possibly an array; see ‘Details’.

Conversion

Real numbers and real parts of complex numbers are rounded in the direction of 0. Imaginary parts of complex numbers are discarded.

Character strings are converted using function `mpz_set_str` from the GNU MP library with argument base set to 0; see <https://gmplib.org/manual/Assigning-Integers>.

An error is signaled if elements of `x` are not in the range of the `C` type, in particular if elements of `x` are NaN, $-\text{Inf}$, or Inf . The range is $(-1, 2^n)$ for `ulong` and $(-2^{n-1} - 1, 2^{n-1})$ for `slong`, where n is the value of `flintABI()`.

Slots

`.xData`, `dim`, `dimnames`, `names` inherited from virtual class `flint`.

Methods

```
! signature(x = "ulong"):
  signature(x = "slong"):
  equivalent to (but faster than) x == 0.

%*%, crossprod, tcrossprod signature(x = "ulong", y = "ulong"):
  signature(x = "slong", y = "slong"):
  signature(x = "ulong", y = "ANY"):
  signature(x = "slong", y = "ANY"):
  signature(x = "ANY", y = "ulong"):
  signature(x = "ANY", y = "slong"):
  matrix products. The "other" operand must be atomic or inherit from virtual class flint.
  crossprod and tcrossprod behave as if y = x when y is missing or NULL. Operands are
  promoted as necessary and must be conformable (have compatible dimensions). Non-array
  operands of length k are handled as 1-by-k or k-by-1 matrices depending on the call.

+ signature(e1 = "ulong", e2 = "missing"):
  signature(e1 = "slong", e2 = "missing"):
  returns a copy of the argument.

- signature(e1 = "ulong", e2 = "missing"):
  signature(e1 = "slong", e2 = "missing"):
  returns the negation of the argument.

Complex signature(z = "ulong"):
  signature(z = "slong"):
  mathematical functions of one argument; see S4groupGeneric. Member functions requiring
  promotion to a floating-point type may not be implemented.

Math signature(x = "ulong"):
  signature(x = "slong"):
  mathematical functions of one argument; see S4groupGeneric. Member functions requiring
  promotion to a floating-point type may not be implemented.

Math2 signature(x = "ulong"):
  signature(x = "slong"):
  decimal rounding according to a second argument digits; see S4groupGeneric. There are
  just two member member functions: round, signif.
```

```
Ops signature(e1 = "ulong", e2 = "ulong"):
  signature(e1 = "slong", e2 = "slong"):
  signature(e1 = "ulong", e2 = "ANY"):
  signature(e1 = "slong", e2 = "ANY"):
  signature(e1 = "ANY", e2 = "ulong"):
  signature(e1 = "ANY", e2 = "slong"):
  binary arithmetic, comparison, and logical operators; see S4groupGeneric. The “other”
  operand must be atomic or inherit from virtual class flint. Operands are promoted as neces-
  sary. Array operands must be conformable (have identical dimensions). Non-array operands
  are recycled.
```

Summary signature(x = "ulong"):
 signature(x = "slong"):
 univariate summary statistics; see [S4groupGeneric](#). The return value is a logical vector of
 length 1 (any, all) or a ulong, slong, or [fmpz](#) vector of length 1 or 2 (sum, prod, min, max,
 range).

```
anyNA signature(x = "ulong"):
  signature(x = "slong"):
  returns FALSE, as ulong and slong have no representation for NaN.
```

as.vector signature(x = "ulong"):
 signature(x = "slong"):
 returns as.vector(y, mode), where y is a double vector containing the result of converting
 each element of x to the range of double, rounding if the value is not exactly representable in
 double precision. The rounding mode is to the nearest representable number in the direction of
 zero. Coercion to types "character", "symbol" (synonym "name"), "pairlist", "list",
 and "expression", which are not “number-like”, is handled specially. See also [asVector](#).

```
backsolve signature(r = "ulong", x = "ulong"):
  signature(r = "slong", x = "slong"):
  signature(r = "ulong", x = "ANY"):
  signature(r = "slong", x = "ANY"):
  signature(r = "ANY", x = "ulong"):
  signature(r = "ANY", x = "slong"):
  solution of the triangular system op2(op1(r)) %*% y = x, where op1=ifelse(upper.tri,
  triu, tril) and op2=ifelse(transpose, t, identity) and upper.tri and transpose
  are optional logical arguments with default values TRUE and FALSE, respectively. The “other”
  operand must be atomic or inherit from virtual class flint. If x is missing, then the return
  value is the inverse of op2(op1(r)), as if x were the identity matrix. Operands are promoted
  as necessary and must be conformable (have compatible dimensions). Non-array x are handled
  as length(x)-by-1 matrices. If r and (if not missing) x are both formally rational, then the
  solution is exact and the return value is an fmpq matrix.
```

```
chol signature(x = "ulong"):
  signature(x = "slong"):
  coerces x to class arf and dispatches.
```

```
chol2inv signature(x = "ulong"):
  signature(x = "slong"):
  returns the inverse of the positive definite matrix whose upper triangular Cholesky factor
  is the upper triangular part of x. The return value is the exact inverse, being computed as
  tcrossprod(backsolve(x)).
```

```

coerce signature(from = "ANY", to = "ulong"):
  signature(from = "ANY", to = "slong"):
    returns the value of ulong(from) or slong(from).

colSums signature(x = "ulong"):
  signature(x = "slong"):
    returns a ulong or (in case of overflow) fmpz vector or array containing the column sums of
    x, defined as sums over dimensions 1:dims.

colMeans signature(x = "ulong"):
  signature(x = "slong"):
    returns an fmpq vector or array containing the column means of x, defined as means over
    dimensions 1:dims.

det, determinant signature(x = "ulong"):
  signature(x = "slong"):
    coerces x to class fmpz and dispatches.

format signature(x = "ulong"):
  signature(x = "slong"):
    returns a character vector suitable for printing. Optional arguments control the output; see
    format-methods.

is.finite signature(x = "ulong"):
  signature(x = "slong"):
    returns a logical vector whose elements are all TRUE, as ulong and slong have no representa-
    tion for NaN, -Inf, and Inf.

is.infinite, is.na, is.nan signature(x = "ulong"):
  signature(x = "slong"):
    returns a logical vector whose elements are all FALSE, as ulong and slong have no represen-
    tation for NaN, -Inf, and Inf.

is.unsorted signature(x = "ulong"):
  signature(x = "slong"):
    returns a logical indicating if x is not sorted in nondecreasing order (increasing order if op-
    tional argument strictly is set to TRUE).

mean signature(x = "ulong"):
  signature(x = "slong"):
    returns the arithmetic mean. An error is signaled if the argument length is 0, because the return
    type is fmpq which cannot represent the result of division by 0.

rowSums signature(x = "ulong"):
  signature(x = "slong"):
    returns a ulong or (in case of overflow) fmpz vector or array containing the row sums of x,
    defined as sums over dimensions (dims+1):length(dim(x)).

rowMeans signature(x = "ulong"):
  signature(x = "slong"):
    returns an fmpq vector or array containing the row means of x, defined as means over dimen-
    sions (dims+1):length(dim(x)).

solve signature(a = "ulong", b = "ulong"):
  signature(a = "slong", b = "slong"):
  signature(a = "ulong", b = "ANY"):

```

```
signature(a = "slong", b = "ANY"):  
signature(a = "ANY", b = "ulong"):  
signature(a = "ANY", b = "slong"):  
solution of the general system  $a \cdot x = b$ . The “other” operand must be atomic or inherit  
from virtual class flint. If b is missing, then the return value is the inverse of a, as if b  
were the identity matrix. Operands are promoted as necessary and must be conformable (have  
compatible dimensions). Non-array b are handled as length(b)-by-1 matrices. If a and (if  
not missing) b are both formally rational, then the solution is exact and the return value is an  
fmpq matrix.
```

References

The FLINT documentation of the underlying C types: <https://flintlib.org/doc/flint.html>

See Also

Virtual class `flint`.

Examples

```
showClass("ulong")  
showClass("slong")  
showMethods(classes = c("ulong", "slong"))
```

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