

# Package ‘hgwrr’

July 28, 2024

**Type** Package

**Title** Hierarchical and Geographically Weighted Regression

**Version** 0.5-0

**Date** 2024-07-04

**Author** Yigong Hu, Richard Harris, Richard Timmerman

**Maintainer** Yigong Hu <yigong.hu@bristol.ac.uk>

**Description** This model divides coefficients into three types, i.e., local fixed effects, global fixed effects, and random effects (Hu et al., 2022)<doi:10.1177/23998083211063885>. If data have spatial hierarchical structures (especially are overlapping on some locations), it is worth trying this model to reach better fitness.

**License** GPL (>= 2)

**URL** <https://github.com/HPDell/hgwrr/>, <https://hpdell.github.io/hgwrr/>

**Imports** Rcpp (>= 1.0.8)

**LinkingTo** Rcpp, RcppArmadillo

**Depends** R (>= 3.5.0), sf, stats, utils

**NeedsCompilation** yes

**Suggests** knitr, rmarkdown, testthat (>= 3.0.0),

**SystemRequirements** GNU make

**RoxygenNote** 7.2.3

**VignetteBuilder** knitr

**Config/Needs/website** tidyverse, ggplot2, tmap, lme4, spdep, GWmodel

**Repository** CRAN

**Date/Publication** 2024-07-28 15:00:02 UTC

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hgwr-package	<i>HGWR: Hierarchical and Geographically Weighted Regression</i>
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## Description

An R and C++ implementation of Hierarchical and Geographically Weighted Regression (HGWR) model is provided in this package. This model divides coefficients into three types: local fixed effects, global fixed effects, and random effects. If data have spatial hierarchical structures (especially are overlapping on some locations), it is worth trying this model to reach better fitness.

## Details

Package:	hgwr
Type:	Package
Title:	Hierarchical and Geographically Weighted Regression
Version:	0.5-0
Date:	2024-07-04
Author:	Yigong Hu, Richard Harris, Richard Timmerman
Maintainer:	Yigong Hu <yigong.hu@bristol.ac.uk>
Description:	This model divides coefficients into three types, i.e., local fixed effects, global fixed effects, and random effects.
License:	GPL (>= 2)
URL:	<a href="https://github.com/HPDell/hgwr/">https://github.com/HPDell/hgwr/</a> , <a href="https://hpdell.github.io/hgwr/">https://hpdell.github.io/hgwr/</a>
Imports:	Rcpp (>= 1.0.8)
LinkingTo:	Rcpp, RcppArmadillo
Depends:	R (>= 3.5.0), sf, stats, utils
NeedsCompilation:	yes
Suggests:	knitr, rmarkdown, testthat (>= 3.0.0),
SystemRequirements:	GNU make
Roxygen:	list(markdown = TRUE)
RoxygenNote:	7.2.3

VignetteBuilder: knitr  
Config/Needs/website: tidyverse, ggplot2, tmap, lme4, spdep, GWmodel

## Note

Acknowledgement: We gratefully acknowledge support from China Scholarship Council.

## Author(s)

Yigong Hu, Richard Harris, Richard Timmerman

## References

Hu, Y., Lu, B., Ge, Y., Dong, G., 2022. Uncovering spatial heterogeneity in real estate prices via combined hierarchical linear model and geographically weighted regression. *Environment and Planning B: Urban Analytics and City Science*. doi:10.1177/23998083211063885

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coef.hgwr	<i>Get estimated coefficients.</i>
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---

## Description

Get estimated coefficients.

## Usage

```
## S3 method for class 'hgwr'  
coef(object, ...)
```

## Arguments

object            An hgwr object returned by `hgwr()`.  
...                Parameter received from other functions.

## Value

A DataFrame object consists of all estimated coefficients.

## See Also

`hgwr()`, `summary.hgwr()`, `fitted.hgwr()` and `residuals.hgwr()`.

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fitted.hgwr	<i>Get fitted response.</i>
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---

### Description

Get fitted response.

### Usage

```
## S3 method for class 'hgwr'
fitted(object, ...)
```

### Arguments

object	An hgwr object returned by <a href="#">hgwr()</a> .
...	Parameter received from other functions.

### Value

A vector consists of fitted response values.

### See Also

[hgwr\(\)](#), [summary.hgwr\(\)](#), [coef.hgwr\(\)](#) and [residuals.hgwr\(\)](#).

---

hgwr	<i>Hierarchical and Geographically Weighted Regression</i>
------	--

---

### Description

A Hierarchical Linear Model (HLM) with local fixed effects.

### Usage

```
hgwr(
  formula,
  data,
  ...,
  bw = "CV",
  kernel = c("gaussian", "bisquared"),
  alpha = 0.01,
  eps_iter = 1e-06,
  eps_gradient = 1e-06,
  max_iters = 1e+06,
  max_retries = 1e+06,
```

```
ml_type = c("D_Only", "D_Beta"),
verbose = 0
)

## S3 method for class 'sf'
hgwr(
  formula,
  data,
  ...,
  bw = "CV",
  kernel = c("gaussian", "bisquared"),
  alpha = 0.01,
  eps_iter = 1e-06,
  eps_gradient = 1e-06,
  max_iters = 1e+06,
  max_retries = 1e+06,
  ml_type = c("D_Only", "D_Beta"),
  verbose = 0
)

## S3 method for class 'data.frame'
hgwr(
  formula,
  data,
  ...,
  coords,
  bw = "CV",
  kernel = c("gaussian", "bisquared"),
  alpha = 0.01,
  eps_iter = 1e-06,
  eps_gradient = 1e-06,
  max_iters = 1e+06,
  max_retries = 1e+06,
  ml_type = c("D_Only", "D_Beta"),
  verbose = 0
)

hgwr_fit(
  formula,
  data,
  coords,
  bw = c("CV", "AIC"),
  kernel = c("gaussian", "bisquared"),
  alpha = 0.01,
  eps_iter = 1e-06,
  eps_gradient = 1e-06,
  max_iters = 1e+06,
  max_retries = 1e+06,
```

```

ml_type = c("D_Only", "D_Beta"),
verbose = 0
)

```

### Arguments

formula	<p>A formula. Its structure is similar to <code>lmer</code> function in <b>lme4</b> package. Models can be specified with the following form:</p> $\text{response} \sim \text{L}(\text{local.fixed}) + \text{global.fixed} + (\text{random} \mid \text{group})$ <p>For more information, please see the formula subsection in details.</p>
data	The data.
...	Further arguments for the specified type of data.
bw	<p>A numeric value. It is the value of bandwidth or "CV". In this stage this function only support adaptive bandwidth. And its unit must be the number of nearest neighbours. If "CV" is specified, the algorithm will automatically select an optimized bandwidth value.</p>
kernel	<p>A character value. It specify which kernel function is used in GWR part. Possible values are</p> <p>gaussian Gaussian kernel function <math>k(d) = \exp\left(-\frac{d^2}{b^2}\right)</math></p> <p>bisquared Bi-squared kernel function. If <math>d &lt; b</math> then <math>k(d) = \left(1 - \frac{d^2}{b^2}\right)^2</math> else <math>k(d) = 0</math></p>
alpha	A numeric value. It is the size of the first trial step in maximum likelihood algorithm.
eps_iter	A numeric value. Terminate threshold of back-fitting.
eps_gradient	A numeric value. Terminate threshold of maximum likelihood algorithm.
max_iters	An integer value. The maximum of iteration.
max_retries	An integer value. If the algorithm tends to be diverge, it stops automatically after trying <i>max_retries</i> times.
ml_type	<p>An integer value. Represent which maximum likelihood algorithm is used. Possible values are:</p> <p>D_Only Only <i>D</i> is specified by maximum likelihood.</p> <p>D_Beta Both <i>D</i> and <i>beta</i> is specified by maximum likelihood.</p>
verbose	<p>An integer value. Determine the log level. Possible values are:</p> <p><b>0</b> no log is printed.</p> <p><b>1</b> only logs in back-fitting are printed.</p> <p><b>2</b> all logs are printed.</p>
coords	A 2-column matrix. It consists of coordinates for each group.

## Details

### Effect Specification in Formula:

In the HGWR model, there are three types of effects specified by the formula argument:

**Local fixed effects** Effects wrapped by functional symbol L.

**Random effects** Effects specified outside the functional symbol L but to the left of symbol |.

**Global fixed effects** Other effects

For example, the following formula in the example of this function below is written as

$$y \sim L(g1 + g2) + x1 + (z1 | group)$$

where g1 and g2 are local fixed effects, x1 is the global fixed effects, and z1 is the random effects grouped by the group indicator group. Note that random effects can only be specified once!

## Value

A list describing the model with following fields.

gamma Coefficients of local fixed effects.

beta Coefficients of global fixed effects.

mu Coefficients of random effects.

D Variance-covariance matrix of random effects.

sigma Variance of errors.

effects A list including names of all effects.

call Calling of this function.

frame The DataFrame object sent to this call.

frame.parsed Variables extracted from the data.

groups Unique group labels extracted from the data.

## Functions

- `hgwr_fit()`: Fit a HGWR model

## Examples

```
data(multisampling)
hgwr(formula = y ~ L(g1 + g2) + x1 + (z1 | group),
      data = multisampling$data,
      coords = multisampling$coords,
      bw = 10)
```

---

logLik.hgwrn	<i>Log likelihood function</i>
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---

**Description**

Log likelihood function

**Usage**

```
## S3 method for class 'hgwrn'  
logLik(object, ...)
```

**Arguments**

object	An hgwrn object.
...	Additional arguments.

**Value**

An logLik instance used for S3 method logLik().

---

make.dummy	<i>Make Dummy Variables</i>
------------	-----------------------------

---

**Description**

Function `make.dummy` converts categorical variables in a data frame to dummy variables.

Function `make.dummy.extract` converts a column to dummy variables if necessary and assign appropriate names. See the "detail" section for further information. Users can define their own functions to allow the model deal with some types of variables properly.

**Usage**

```
make.dummy(data)
```

```
make.dummy.extract(col, name)
```

```
## S3 method for class 'character'  
make.dummy.extract(col, name)
```

```
## S3 method for class 'factor'  
make.dummy.extract(col, name)
```

```
## S3 method for class 'logical'  
make.dummy.extract(col, name)
```



```
## Default S3 method:
make.dummy.extract(col, name)
```

### Arguments

<code>data</code>	The data frame from which dummy variables need to be extracted.
<code>col</code>	A vector to extract dummy variables.
<code>name</code>	The vector's name.

### Details

If `col` is a character vector, the function will get unique values of its elements and leave out the last one. Then, all the unique values are combined with the `name` argument as names of new columns.

If `col` is a factor vector, the function will get its levels and leave out the last one. Then, all level labels are combined with the `name` argument as names of new columns.

If `col` is a logical vector, the function will convert it to a numeric vector with value `TRUE` mapped to 1 and `FALSE` to 0.

If `col` is of other types, the default behaviour for extracting dummy variables is just to copy the original value and try to convert it to numeric values.

### Value

The data frame with extracted dummy variables.

### Examples

```
make.dummy(iris["Species"])

make.dummy.extract(iris$Species, "Species")

make.dummy.extract(c("top", "mid", "low", "mid", "top"), "level")

make.dummy.extract(factor(c("far", "near", "near")), "distance")

make.dummy.extract(c(TRUE, TRUE, FALSE), "sold")
```

---

multisampling

*Simulated Spatial Multisampling Data (DataFrame)*

---

### Description

A simulation data of spatial hierarchical structure and samples overlapping on certain locations.

### Usage

```
data(multisampling)
```

**Format**

A list of two items called "data" and "coord". Item "data" is a data frame with 484 observations at 16 locations on the following 6 variables.

*y* a numeric vector, dependent variable *y*  
*g1* a numeric vector, group level independent variable *g*<sub>1</sub>  
*g2* a numeric vector, group level independent variable *g*<sub>2</sub>  
*z1* a numeric vector, sample level independent variable *z*<sub>1</sub>  
*x1* a numeric vector, sample level independent variable *x*<sub>1</sub>  
*group* a numeric vector, group id of each sample

where *g1* and *g2* are used to estimate local fixed effects; *x1* is used to estimate global fixed effects and *z1* is used to estimate random effects.

**Author(s)**

Yigong Hu <yigong.hu@bristol.ac.uk>

**Examples**

```
data(multisampling)
hgwr(formula = y ~ L(g1 + g2) + x1 + (z1 | group),
      data = multisampling$data,
      coords = multisampling$coords,
      bw = 10)
```

---

multisampling.large    *Large Scale Simulated Spatial Multisampling Data (DataFrame)*

---

**Description**

A large scale simulation data of spatial hierarchical structure and samples overlapping on certain locations.

**Usage**

```
data(multisampling)
```

**Format**

A list of three items called "data", "coords" and "beta". Item "data" is a data frame with 13862 observations at 200 locations and the following 6 variables.

*y* a numeric vector, dependent variable *y*  
*g1* a numeric vector, group level independent variable *g*<sub>1</sub>  
*g2* a numeric vector, group level independent variable *g*<sub>2</sub>

z1 a numeric vector, sample level independent variable  $z_1$   
 x1 a numeric vector, sample level independent variable  $x_1$   
 group a numeric vector, group id of each sample

where g1 and g2 are used to estimate local fixed effects; x1 is used to estimate global fixed effects and z1 is used to estimate random effects.

### Author(s)

Yigong Hu <yigong.hu@bristol.ac.uk>

### Examples

```
## Not run:
data(multisampling.large)
hgwr(formula = y ~ L(g1 + g2) + x1 + (z1 | group),
      data = multisampling.large$data,
      coords = multisampling.large$coords,
      bw = 32, kernel = "bisquared")

## End(Not run)
```

---

print.hgwrn                      *Print description of a hgwrn object.*

---

### Description

Print description of a hgwrn object.

### Usage

```
## S3 method for class 'hgwrn'
print(x, decimal.fmt = "%.6f", ...)
```

### Arguments

x	An hgwrn object returned by <code>hgwr()</code> .
decimal.fmt	The format string passing to <code>base::sprintf()</code> .
...	Arguments passed on to <code>print.table.md</code>
col.sep	Column separator. Default to "".
header.sep	Header separator. Default to "-".
row.begin	Character at the beginning of each row. Default to col.sep.
row.end	Character at the ending of each row. Default to col.sep.
table.style	Name of pre-defined style. Possible values are "plain", "md" or "latex". Default to "plain".

**Value**

No return.

**See Also**

[summary.hgwrn\(\)](#), [print.table.md\(\)](#).

**Examples**

```
data(multisampling)
model <- hgwr(formula = y ~ L(g1 + g2) + x1 + (z1 | group),
              data = multisampling$data,
              coords = multisampling$coords,
              bw = 10)
print(model)
print(model, table.style = "md")
```

---

```
print.shgt
```

*Print the result of spatial heterogeneity test*

---

**Description**

Print the result of spatial heterogeneity test

**Usage**

```
## S3 method for class 'shgt'
print(x, ...)
```

**Arguments**

```
x          A shgt object.
...        Other unused arguments.
```

---

```
print.summary.hgwrn
```

*Print summary of an hgwrn object.*

---

**Description**

Print summary of an hgwrn object.

**Usage**

```
## S3 method for class 'summary.hgwrn'
print(x, decimal.fmt = "%.6f", ...)
```

**Arguments**

**x** An object returned from `summary.hgwr()`.  
**decimal.fmt** The format string passing to `base::sprintf()`.  
**...** Arguments passed on to `print.table.md`  
**col.sep** Column separator. Default to `" "`.  
**header.sep** Header separator. Default to `"-"`.  
**row.begin** Character at the beginning of each row. Default to `col.sep`.  
**row.end** Character at the ending of each row. Default to `col.sep`.  
**table.style** Name of pre-defined style. Possible values are `"plain"`, `"md"` or `"latex"`. Default to `"plain"`.

**Value**

No return.

**See Also**

`summary.hgwr()`, `print.table.md()`.

**Examples**

```

data(multisampling)
model <- hgwr(formula = y ~ L(g1 + g2) + x1 + (z1 | group),
              data = multisampling$data,
              coords = multisampling$coords,
              bw = 10)
summary(model)

```

---

`print.table.md`      *Print a character matrix as a table.*

---

**Description**

Print a character matrix as a table.

**Usage**

```

## S3 method for class 'table.md'
print(
  x,
  col.sep = "",
  header.sep = "",
  row.begin = "",
  row.end = "",
  table.style = c("plain", "md", "latex"),
  ...
)

```

**Arguments**

<code>x</code>	A character matrix.
<code>col.sep</code>	Column separator. Default to <code>""</code> .
<code>header.sep</code>	Header separator. Default to <code>"-"</code> .
<code>row.begin</code>	Character at the beginning of each row. Default to <code>col.sep</code> .
<code>row.end</code>	Character at the ending of each row. Default to <code>col.sep</code> .
<code>table.style</code>	Name of pre-defined style. Possible values are <code>"plain"</code> , <code>"md"</code> or <code>"latex"</code> . Default to <code>"plain"</code> .
<code>...</code>	Additional style control arguments.

**Details**

When `table.style` is specified, `col.sep`, `header.sep`, `row.begin` and `row.end` would not take effects. Because this function will automatically set their values. For each possible value of `table.style`, its corresponding style settings are shown in the following table.

	plain	md	latex
<code>col.sep</code>	<code>""</code>	<code>" "</code>	<code>"&amp;"</code>
<code>header.sep</code>	<code>""</code>	<code>"_"</code>	<code>""</code>
<code>row.begin</code>	<code>""</code>	<code>" "</code>	<code>""</code>
<code>row.end</code>	<code>""</code>	<code>" "</code>	<code>"\\"</code>

In this function, characters are right padded by spaces.

**Value**

No return.

**See Also**

[print.hgwrn\(\)](#), [summary.hgwrn\(\)](#).

---

`residuals.hgwrn`      *Get residuals.*

---

**Description**

Get residuals.

**Usage**

```
## S3 method for class 'hgwrn'
residuals(object, ...)
```

**Arguments**

object            An hgwr object returned by `hgwr()`.  
 ...              Parameter received from other functions.

**Value**

A vector consists of residuals.

**See Also**

`hgwr()`, `summary.hgwrm()`, `coef.hgwrm()` and `fitted.hgwrm()`.

---

`spatial_hetero_test`    *Test the spatial heterogeneity in data based on permutation.*

---

**Description**

Test the spatial heterogeneity in data based on permutation.

**Usage**

```
spatial_hetero_test(
  x,
  coords,
  ...,
  resample = 5000,
  poly = 2,
  bw = 10,
  kernel = c("bisquared", "gaussian"),
  verbose = 0
)
```

**Arguments**

x                    A matrix of data to be tested. Each column is a variable.  
 coords              A matrix of coordinates.  
 ...                  Additional arguments.  
 resample            The total times of resampling with replacement. Default to 5000.  
 poly                 The number of polynomial terms used by the polynomial estimator. Default to 2.  
 bw                   The adaptive bandwidth used by the polynomial estimator. Default to 10.  
 kernel              The kernel function used by the polynomial estimator.  
 verbose             The verbosity level. Default to 0.

**Value**

A shgt object of permutation-test results with the following items:

`vars` The names of variables.

`t0` The value of the statistics (variance of density estimation) on original values.

`t` The value of the same statistics on permuted values.

`p` The p-value for each variable.

**Examples**

```
data(multisampling.large)
spatial_hetero_test(multisampling.large$beta, multisampling.large$coords)
```

---

summary.hgwrn	<i>Summary an hgwrn object.</i>
---------------	---------------------------------

---

**Description**

Summary an hgwrn object.

**Usage**

```
## S3 method for class 'hgwrn'
summary(object, ..., test_hetero = FALSE, verbose = 0)
```

**Arguments**

<code>object</code>	An hgwrn object returned from <code>hgwr()</code> .
<code>...</code>	Other arguments passed from other functions.
<code>test_hetero</code>	Logical/list value. Whether to test the spatial heterogeneity of local fixed effects. If it is set to FALSE, the test will not be executed. If it is set to TRUE, the test will be executed with default parameters (see details below). It accepts a list to enable the test with specified parameters.
<code>verbose</code>	An Integer value to control whether additional messages during testing spatial heterogeneity should be reported.

**Details**

The parameters used to perform test of spatial heterogeneity are

`bw` Bandwidth (unit: number of nearest neighbours) used to make spatial kernel density estimation. Default: 10.

`poly` The number of polynomial terms used in the local polynomial estimation. Default: 2.

`resample` Total resampling times. Default: 5000.

`kernel` The kernel function used in the local polynomial estimation. Options are "gaussian" and "bisquared". Default: "bisquared".



**Value**

A list containing summary informations of this hgwr object with the following fields.

`diagnostic` A list of diagnostic information.

`random.stddev` The standard deviation of random effects.

`random.corr` The correlation matrix of random effects.

`residuals` The residual vector.

**See Also**

[hgwr\(\)](#).

**Examples**

```
data(multisampling)
m <- hgwr(
  formula = y ~ L(g1 + g2) + x1 + (z1 | group),
  data = multisampling$data,
  coords = multisampling$coords,
  bw = 10
)
summary(m)
summary(m, test_hetero = TRUE)
summary(m, test_hetero = list(kernel = "gaussian"))
```

---

wuhan.hp

*Wuhan Second-hand House Price and POI Data (DataFrame)*

---

**Description**

A data set of second-hand house price in Wuhan, China collected in 2018.

**Usage**

```
data(multisampling)
```

**Format**

A list of two items called "data" and "coords". Item "data" is a data frame with 13862 second-hand properties at 779 neighbourhoods and the following 22 variables.

`Price` House price per square metre.

`Floor.High` 1 if a property is on a high floor, otherwise 0.

`Floor.Low` 1 if a property is on a low floor, otherwise 0.

`Decoration.Fine` 1 if a property is well decorated, otherwise 0.

`PlateTower` 1 if a property is of the plate-tower type, otherwise 0.

Steel 1 if a property is of 'steel' structure, otherwise 0.  
 BuildingArea Building area in square metres.  
 Fee Management fee per square meter per month.  
 d.Commercial Distance to the nearest commercial area.  
 d.Greenland Distance to the nearest green land.  
 d.Water Distance to the nearest river or lake.  
 d.University Distance to the nearest university.  
 d.HighSchool Distance to the nearest high school.  
 d.MiddleSchool Distance to the nearest middle school.  
 d.PrimarySchool Distance to the nearest primary school.  
 d.Kindergarten Distance to the nearest kindergarten.  
 d.SubwayStation Distance to the nearest subway station.  
 d.Supermarket Distance to the nearest supermarket.  
 d.ShoppingMall Distance to the nearest shopping mall.  
 lon Longitude coordinates (Projected CRS: EPSG 3857).  
 lat Latitude coordinates (Projected CRS: EPSE 3857).  
 group Group id of each sample.

The following variables are group level:

- Fee - d.Commercial - d.Greenland - d.Water - d.University - d.HighSchool - d.MiddleSchool  
 - d.PrimarySchool - d.Kindergarten - d.SubwayStation - d.Supermarket - d.ShoppingMall

The following variables are sample level:

- Price - Floor.High - Floor.Low - Decoration.Fine - PlateTower - Steel - BuildingArea

Item "coords" is a 779-by-2 matrix of coordinates of all neighbourhoods.

### Author(s)

Yigong Hu <yigong.hu@bristol.ac.uk>

### Examples

```
## Not run:
data(wuhan.hp)
hgw(
  formula = Price ~ L(d.Water + d.Commercial + d.PrimarySchool +
    d.Kindergarten + Fee) + BuildingArea + (Floor.High | group),
  data = wuhan.hp$data,
  coords = wuhan.hp$coords, bw = 50, kernel = "bisquared")

## End(Not run)
```

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