# Package 'Irstat'

June 19, 2024

Type Package

**Title** Power and Sample Size Calculation for Non-Proportional Hazards and Beyond

Version 0.2.8

Date 2024-06-16

**Description** Performs power and sample size calculation for non-proportional hazards model using the Fleming-Harrington family of weighted log-rank tests. The sequentially calculated log-rank test score statistics are assumed to have independent increments as characterized in Anastasios A. Tsiatis (1982) <doi:10.1080/01621459.1982.10477898>. The mean and variance of log-rank test score statistics are calcu-

lated based on Kaifeng Lu (2021) <doi:10.1002/pst.2069>. The boundary crossing probabilities are calculated using the recursive integration algorithm described in Christopher Jennison and Bruce W. Turnbull (2000, ISBN:0849303168). The package can also be used for continuous, binary, and count data. For continuous data, it can handle missing data through mixed-model for repeated measures (MMRM). In crossover designs, it can estimate direct treatment effects while accounting for carryover effects. For binary data, it can design Simon's 2-stage, modified toxicity probability-2 (mTPI-2), and Bayesian optimal interval (BOIN) trials. For count data, it can design group sequential trials for negative binomial endpoints with censoring. Additionally, it facilitates group sequential equivalence trials for all supported data types. Moreover, it can design adaptive group sequential trials for changes in sample size, error spending function, number and spacing or future looks. Finally, it offers various options for adjusted p-values, including graphical and gatekeeping procedures.

```
License GPL (>= 2)
```

**Imports** Rcpp (>= 1.0.9), mvtnorm (>= 1.1-3), lpSolve (>= 5.6.1), shiny (>= 1.7.1)

LinkingTo Rcpp

**Suggests** testthat (>= 3.0.0), dplyr (>= 1.1.4), tidyr (>= 1.3.0), knitr (>= 1.45), rmarkdown (>= 2.25), survival (>= 3.5-7)

VignetteBuilder knitr

RoxygenNote 7.3.1

**Encoding UTF-8** 

**NeedsCompilation** yes

2 Contents

<b>Depends</b>	R (>=	2.10)
----------------	-------	-------

LazyData true

**Author** Kaifeng Lu [aut, cre] (<a href="https://orcid.org/0000-0002-6160-7119">https://orcid.org/0000-0002-6160-7119</a>)

Maintainer Kaifeng Lu <kaifenglu@gmail.com>

**Repository** CRAN

**Date/Publication** 2024-06-19 07:30:02 UTC

# **Contents**

accrual
adaptDesign
aml 10
BOINTable
caltime
ClopperPearsonCI
covrmst
errorSpent
exitprob
fadjpbon
fadjpdun
fadjpsim
fmodmix
fquantile
fseqbon
fstdmix
fstp2seq
ftrunc
fwgtmat
getAccrualDurationFromN
getADCI
getADRCI
getBound
getCI
getCP
getDesign
getDesignAgreement
getDesignANOVA
getDesignANOVAContrast
getDesignEquiv
getDesignFisherExact
getDesignLogistic
getDesignMeanDiff
getDesignMeanDiffCarryover
getDesignMeanDiffEquiv
getDesignMeanDiffMMRM
getDesignMeanDiffXO

Contents 3

getDesignMeanDiffXOEquiv	
getDesignMeanRatio	
getDesignMeanRatioEquiv	. 88
getDesignMeanRatioXO	. 91
getDesignMeanRatioXOEquiv	. 94
getDesignOddsRatio	. 97
getDesignOddsRatioEquiv	. 101
getDesignOneMean	
getDesignOneMultinom	
getDesignOneProportion	. 109
getDesignOneRateExact	
getDesignOneSlope	
getDesignOrderedBinom	
getDesignPairedMeanDiff	
getDesignPairedMeanDiffEquiv	
getDesignPairedMeanRatio	
getDesignPairedMeanRatioEquiv	
getDesignPairedPropMcNemar	
getDesignRepeatedANOVA	
getDesignRepeatedANOVAContrast	
getDesignRiskDiff	
getDesignRiskDiffEquiv	
getDesignRiskDiffExact	
getDesignRiskDiffExactEquiv	
getDesignRiskRatio	148
getDesignRiskRatioEquiv	
getDesignRiskRatioExact	
getDesignRiskRatioExactEquiv	
getDesignRiskRatioFM	
getDesignSlopeDiff	
getDesignSlopeDiffMMRM	
getDesignTwoMultinom	
getDesignTwoOrdinal	
getDesignTwoWayANOVA	
getDesignUnorderedBinom	
getDesignUnorderedMultinom	
getDesignWilcoxon	
getDurationFromNevents	
getNeventsFromHazardRatio	
getRCI	
heart	
hedgesg	
kmdiff	
kmest	
kmpower	
kmpower1s	
kmpowerequiv	
kmsamplesize	. 203

4 Contents

kmsamplesize1s											
kmsamplesizeequiv .	 	 				 				 	. 211
kmstat	 	 				 				 	. 214
liferegr	 	 				 				 	 . 216
lrpower	 	 				 				 	 . 218
lrpowerequiv	 	 				 				 	 . 223
lrsamplesize	 	 				 				 	 . 228
lrsamplesizeequiv											
lrsim											
lrsim2e											
lrsim2e3a											
lrsim3a											
lrstat											
lrtest											
mnOddsRatioCI											
mnRateDiffCI											
mnRateRatioCI											
mnRiskDiffCI											
mnRiskRatioCI											
mTPI2Table											
nbpower											
nbpower1s											. 203
nbpowerequiv											. 274
											. 274
nbsamplesize											
nbsamplesize1s											. 282
nbsamplesizeequiv .											
nbstat											
phregr											
ptpwexp											
pwexpcuts											
pwexploglik											
qtpwexp											
rawdata											
remlOddsRatio											
remlRateDiff											. 301
remlRateRatio											. 302
remlRiskDiff											
remlRiskRatio											
repeatedPValue											
riskDiffExactCI											
riskDiffExactPValue											
riskRatioExactCI											
riskRatioExactPValue											
rmdiff											
rmest											
rmpower											
rmpower1s											
rmpowerequiv	 	 		 		 			 	 	 . 321

accrual 5

Index		352
	zstatRiskRatio	351
	zstatRiskDiff	350
	zstatRateRatio	349
	zstatRateDiff	348
	zstatOddsRatio	347
	updateGraph	346
	tobin	346
	survQuantile	345
	simonBayesSim	342
	simonBayesAnalysis	341
	simon2stage	340
	runShinyApp	339
	rtpwexp	338
	rmstat	336
	rmst	335
	rmsamplesizeequiv	333
	rmsamplesize1s	329
	rmsamplesize	325

accrual

Number of enrolled subjects

# **Description**

Obtains the number of subjects enrolled by given calendar times.

# Usage

```
accrual(
  time = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  accrualDuration = NA_real_)
```

# **Arguments**

time A vector of calendar times at which to calculate the number of enrolled subjects.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

accrual Duration

Duration of the enrollment period.

#### Value

A vector of total number of subjects enrolled by the specified calendar times.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### **Examples**

adaptDesign

Adaptive design at an interim look

# **Description**

Obtains the conditional power for specified incremental information given the interim results, parameter value, and data-dependent changes in the error spending function, and the number and spacing of interim looks. Conversely, obtains the incremental information needed to attain a specified conditional power given the interim results, parameter value, and data-dependent changes in the error spending function, and the number and spacing of interim looks.

# Usage

```
adaptDesign(
  betaNew = NA_real_,
  INew = NA_real_,
  L = NA_integer_,
  zL = NA_real_,
  theta = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
```

```
alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  spendingTime = NA_real_,
 MullerSchafer = 0L,
  kNew = NA_integer_,
 informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  futilityStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  typeBetaSpendingNew = "none",
  parameterBetaSpendingNew = NA_real_,
  userBetaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_,
  varianceRatio = 1
)
```

### **Arguments**

betaNew The type II error for the secondary trial.

INew The maximum information of the secondary trial. Either betaNew or INew

should be provided while the other one should be missing.

L The interim adaptation look of the primary trial.

zL The z-test statistic at the interim adaptation look of the primary trial.

theta The parameter value.

IMax The maximum information of the primary trial. Must be provided if futilityBounds

is missing and typeBetaSpending is not equal to "none", or if conditional

power calculation is desired.

kMax The maximum number of stages of the primary trial.

informationRates

The information rates of the primary trial.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage of the primary

trial. Defaults to true if left unspecified.

 ${\it futilityStopping}$ 

Indicators of whether futility stopping is allowed at each stage of the primary

trial. Defaults to true if left unspecified.

criticalValues The upper boundaries on the z-test statistic scale for efficacy stopping for the

primary trial.

alpha The significance level of the primary trial. Defaults to 0.025.

#### typeAlphaSpending

The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpending

The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

### userAlphaSpending

The user defined alpha spending for the primary trial. Cumulative alpha spent up to each stage.

futilityBounds The lower boundaries on the z-test statistic scale for futility stopping for the primary trial. Defaults to rep(-6, kMax-1) if left unspecified.

#### typeBetaSpending

The type of beta spending for the primary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value of beta spending for the primary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

spendingTime

The error spending time of the primary trial. Defaults to missing, in which case, it is the same as informationRates.

MullerSchafer

Whether to use the Muller and Schafer (2001) method for trial adaptation.

kNew

The number of looks of the secondary trial.

#### informationRatesNew

The spacing of looks of the secondary trial.

### efficacyStoppingNew

The indicators of whether efficacy stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

# ${\it futilityStoppingNew}$

The indicators of whether futility stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

### typeAlphaSpendingNew

The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpendingNew

The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### typeBetaSpendingNew

The type of beta spending for the secondary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpendingNew

The parameter value of beta spending for the secondary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

### userBetaSpendingNew

The user defined cumulative beta spending. Cumulative beta spent up to each stage of the secondary trial.

### spendingTimeNew

The error spending time of the secondary trial. Defaults to missing, in which case, it is the same as informationRatesNew.

varianceRatio The ratio of the variance under H0 to the variance under H1.

#### Value

An adaptDesign object with two list components:

- primaryTrial: A list of selected information for the primary trial, including L, zL, theta, kMax, informationRates, efficacyBounds, futilityBounds, and MullerSchafer.
- secondaryTrial: A design object for the secondary trial.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### References

Lu Chi, H. M. James Hung, and Sue-Jane Wang. Modification of sample size in group sequential clinical trials. Biometrics 1999;55:853-857.

Hans-Helge Muller and Helmut Schafer. Adaptive group sequential designs for clinical trials: Combining the advantages of adaptive and of classical group sequential approaches. Biometrics 2001;57:886-891.

### See Also

```
getDesign
```

10 aml

parameterAlphaSpending = -4))

```
# interim look results
L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)
t = des1$byStageResults$informationRates
# conditional power with sample size increase
(des2 = adaptDesign(
  betaNew = NA, INew = 420/(4*sigma1^2),
  L, zL, theta = delta1,
  IMax = n/(4*sigma1^2), kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4))
# Muller & Schafer (2001) method to design the secondary trial:
# 3-look gamma(-2) spending with 84% power at delta = 4.5 and sigma = 20
(des2 = adaptDesign(
  betaNew = 0.16, INew = NA,
  L, zL, theta = delta1,
  IMax = n/(4*sigma1^2), kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2))
# incremental sample size for sigma = 20
(nNew = 4*sigma1^2*des2$secondaryTrial$overallResults$information)
```

aml

Acute myelogenous leukemia survival data from the survival package

# **Description**

Survival in patients with acute myelogenous leukemia.

```
time Survival or censoring time
status censoring status
x maintenance chemotherapy given or not
```

### Usage

aml

BOINTable 11

# **Format**

An object of class data. frame with 23 rows and 3 columns.

BOINTable

BOIN decision table

# **Description**

Obtains the decision table for the Bayesian optimal interval (BOIN) design.

# Usage

```
BOINTable(
  nMax = NA_integer_,
  pT = 0.3,
  phi1 = 0.6 * pT,
  phi2 = 1.4 * pT,
  a = 1,
  b = 1,
  pExcessTox = 0.95
)
```

### **Arguments**

nMax	The maximum number of subjects in a dose cohort.
рТ	The target toxicity probability. Defaults to 0.3.
phi1	The lower equivalence limit for target toxicity probability.
phi2	The upper equivalence limit for target toxicity probability.
a	The prior toxicity parameter for the beta prior.
b	The prior non-toxicity parameter for the beta prior.
pExcessTox	The threshold for excessive toxicity, i.e., if Prob(p > pT   Data) > pExcessTox, then the current and all higher doses will be excluded and never be used again in the remainder of the trial to avoid any other subjects receiving treatment at those doses. Defaults to 0.95.

### Value

An S3 class BOINTable object with the following components:

- settings: The input settings data frame with the following variables:
  - nMax: The maximum number of subjects in a dose cohort.
  - pT: The target toxicity probability.
  - phi1: The lower equivalence limit for target toxicity probability.
  - phi2: The upper equivalence limit for target toxicity probability.
  - lambda1: The lower decision boundary for observed toxicity probability.

12 caltime

- lambda2: The upper decision boundary for observed toxicity probability.
- a: The prior toxicity parameter for the beta prior.
- b: The prior non-toxicity parameter for the beta prior.
- pExcessTox: The threshold for excessive toxicity.
- decisionDataFrame: The decision data frame for the BOIN design. It includes the following variables:
  - n: The sample size.
  - y: The number of toxicities.
  - decision: The dosing decision.
- decisionMatrix: The decision matrix corresponding to the decision data frame.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
BOINTable(nMax = 18, pT = 0.3, phi = 0.6*0.3, phi2 = 1.4*0.3)
```

caltime

Calendar times for target number of events

### **Description**

Obtains the calendar times needed to reach the target number of subjects experiencing an event.

# Usage

```
caltime(
  nevents = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L
)
```

caltime 13

### Arguments

nevents A vector of target number of events.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g.,  $c(\emptyset, 3)$  breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

#### Value

A vector of calendar times expected to yield the target number of events.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by # the end of 1 year. caltime(nevents = c(24, 80), allocationRatioPlanned = 1,
```

14 ClopperPearsonCI

```
accrualTime = seq(0, 8),

accrualIntensity = 26/9*seq(1, 9),

piecewiseSurvivalTime = c(0, 6),

stratumFraction = c(0.2, 0.8),

lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),

lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),

gamma1 = -log(1-0.05)/12,

gamma2 = -log(1-0.05)/12,

accrualDuration = 22,

followupTime = 18, fixedFollowup = FALSE)
```

ClopperPearsonCI

Clopper-Pearson confidence interval for one-sample proportion

### **Description**

Obtains the Clopper-Pearson exact confidence interval for a one-sample proportion.

### Usage

```
ClopperPearsonCI(n, y, cilevel = 0.95)
```

# **Arguments**

n The sample size.

y The number of responses.

cilevel The confidence interval level.

### Value

A data frame with the following variables:

- n: The sample size.
- y: The number of responses.
- phat: The observed proportion of responses.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

```
ClopperPearsonCI(20, 3)
```

covrmst 15

covrmst

Covariance between restricted mean survival times

#### Description

Obtains the covariance between restricted mean survival times at two different time points.

### Usage

```
covrmst(
   t2 = NA_real_,
   tau1 = NA_real_,
   tau2 = NA_real_,
   allocationRatioPlanned = 1,
   accrualTime = 0L,
   accrualIntensity = NA_real_,
   piecewiseSurvivalTime = 0L,
   lambda1 = NA_real_,
   lambda2 = NA_real_,
   gamma1 = 0L,
   gamma2 = 0L,
   accrualDuration = NA_real_,
   maxFollowupTime = NA_real_,
)
```

#### **Arguments**

tau1 The milestone time for analysis 2.
tau2 The milestone time for analysis 1.
tau2 The milestone time for analysis 2.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda1 A vector of hazard rates for the event for the active treatment group. One for

each analysis time interval.

lambda2 A vector of hazard rates for the event for the control group. One for each analysis

time interval.

16 errorSpent

gamma1 The hazard rate for exponential dropout, or a vector of hazard rates for piecewise

exponential dropout for the active treatment group.

gamma2 The hazard rate for exponential dropout, or a vector of hazard rates for piecewise

exponential dropout for the control group.

accrualDuration

Duration of the enrollment period.

maxFollowupTime

Follow-up time for the first enrolled subject. For fixed followup, maxFollowupTime = minFollowupTime. For variable followup, maxFollowupTime = accrualDuration

+ minFollowupTime.

#### Value

The covariance between the restricted mean survival times for each treatment group.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### **Examples**

```
covrmst(t2 = 25, tau1 = 16, tau2 = 18, allocationRatioPlanned = 1, accrualTime = c(0, 3), accrualIntensity = c(10, 20), piecewiseSurvivalTime = c(0, 6), lambda1 = c(0.0533, 0.0309), lambda2 = c(0.0533, 0.0533), gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12, accrualDuration = 12, maxFollowupTime = 30)
```

errorSpent

Error spending

#### **Description**

Obtains the error spent at given spending times for the specified error spending function.

### Usage

```
errorSpent(t, error, sf = "sf0F", sfpar = NA)
```

# **Arguments**

sf

t A vector of spending times, typically equal to information fractions.

error The total error to spend.

The spending function. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim &

DeMets spending function, and "sfHSD" for Hwang, Shi & DeCani spending

function. Defaults to "sfOF".

exitprob 17

sfpar

The parameter for the spending function. Corresponds to rho for "sfKD" and gamma for "sfHSD".

### Value

A vector of errors spent up to the interim look.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
errorSpent(t = 0.5, error = 0.025, sf = "sf0F")
errorSpent(t = c(0.5, 0.75, 1), error = 0.025, sf = "sfHSD", sfpar = -4)
```

exitprob

Stagewise exit probabilities

### **Description**

Obtains the stagewise exit probabilities for both efficacy and futility stopping.

# Usage

```
exitprob(b, a = NA, theta = 0, I = NA)
```

# **Arguments**

b	Upper boundaries on the z-test statistic scale.
a	Lower boundaries on the z-test statistic scale. Defaults to $c(rep(-6.0, kMax-1), b[kMax])$ if left unspecified, where $kMax = length(b)$ .
theta	Stagewise parameter of interest, e.g., -U/V for weighted log-rank test, where U is the mean and V is the variance of the weighted log-rank test score statistic at each stage. For proportional hazards and conventional log-rank test, use the scalar input, theta = -log(HR). Defaults to 0 corresponding to the null hypothesis.
I	Stagewise cumulative information, e.g., V, the variance of the weighted log-rank test score statistic at each stage. For conventional log-rank test, information can be approximated by phi*(1-phi)*D, where phi is the probability of being allocated to the active arm, and D is the total number of events at each stage.

# Value

A list of stagewise exit probabilities:

• exitProbUpper: The vector of efficacy stopping probabilities

Defaults to seq(1, kMax) if left unspecified.

• exitProbLower: The vector of futility stopping probabilities.

18 fadjpbon

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
exitprob(b = c(3.471, 2.454, 2.004), theta = -\log(0.6),

I = c(50, 100, 150)/4)

exitprob(b = c(2.963, 2.359, 2.014),

a = c(-0.264, 0.599, 2.014),

theta = c(0.141, 0.204, 0.289),

I = c(81, 121, 160))
```

fadjpbon

Adjusted p-values for Bonferroni-based graphical approaches

# Description

Obtains the adjusted p-values for graphical approaches using weighted Bonferroni tests.

### Usage

```
fadjpbon(w, G, p)
```

# Arguments

- w The vector of initial weights for elementary hypotheses.
- G The initial transition matrix.
- p The raw p-values for elementary hypotheses.

### Value

A matrix of adjusted p-values.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### References

Frank Bretz, Willi Maurer, Werner Brannath and Martin Posch. A graphical approach to sequentially rejective multiple test procedures. Statistics in Medicine. 2009; 28:586-604.

fadjpdun 19

### **Examples**

fadjpdun

Adjusted p-values for Dunnett-based graphical approaches

# **Description**

Obtains the adjusted p-values for graphical approaches using weighted Dunnett tests.

# Usage

```
fadjpdun(wgtmat, p, family = NULL, corr = NULL)
```

### **Arguments**

matrix for intersection hypotheses.

Description of the raw p-values for elementary hypotheses.

The matrix of family indicators for elementary hypotheses.

The correlation matrix that should be used for the parametric test. Can contain NAs for unknown correlations between families.

# Value

A matrix of adjusted p-values.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### References

Frank Bretz, Martin Posch, Ekkehard Glimm, Florian Klinglmueller, Willi Maurer, and Kornelius Rohmeyer. Graphical approach for multiple comparison procedures using weighted Bonferroni, Simes, or parameter tests. Biometrical Journal. 2011; 53:894-913.

20 fadjpsim

### **Examples**

fadjpsim

Adjusted p-values for Simes-based graphical approaches

### **Description**

Obtains the adjusted p-values for graphical approaches using weighted Simes tests.

### Usage

```
fadjpsim(wgtmat, p, family = NULL)
```

### **Arguments**

wgtmat The weight matrix for intersection hypotheses.

p The raw p-values for elementary hypotheses.

family The matrix of family indicators for elementary hypotheses.

#### Value

A matrix of adjusted p-values.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### References

Frank Bretz, Martin Posch, Ekkehard Glimm, Florian Klinglmueller, Willi Maurer, and Kornelius Rohmeyer. Graphical approach for multiple comparison procedures using weighted Bonferroni, Simes, or parameter tests. Biometrical Journal. 2011; 53:894-913.

Kaifeng Lu. Graphical approaches using a Bonferroni mixture of weighted Simes tests. Statistics in Medicine. 2016; 35:4041-4055.

fmodmix 21

### **Examples**

fmodmix

Adjusted p-values for modified mixture gatekeeping procedures

# **Description**

Obtains the adjusted p-values for the modified gatekeeping procedures for multiplicity problems involving serial and parallel logical restrictions.

# Usage

```
fmodmix(
  p,
  family = NULL,
  serial,
  parallel,
  gamma,
  test = "hommel",
  exhaust = 1
)
```

# **Arguments**

p	The raw p-values for elementary hypotheses.
family	The matrix of family indicators for the hypotheses.
serial	The matrix of serial rejection set for the hypotheses.
parallel	The matrix of parallel rejection set for the hypotheses.
gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to $1$ .
test	The component multiple testing procedure. Options include "holm", "hochberg", or "hommel". Defaults to "hommel".
exhaust	Whether to use alpha-exhausting component testing procedure for the last family with active hypotheses. It defaults to TRUE.

22 fquantile

### Value

A matrix of adjusted p-values.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### References

Alex Dmitrienko, George Kordzakhia, and Thomas Brechenmacher. Mixture-based gatekeeping procedures for multiplicity problems with multiple sequences of hypotheses. Journal of Biopharmaceutical Statistics. 2016; 26(4):758–780.

George Kordzakhia, Thomas Brechenmacher, Eiji Ishida, Alex Dmitrienko, Winston Wenxiang Zheng, and David Fuyuan Li. An enhanced mixture method for constructing gatekeeping procedures in clinical trials. Journal of Biopharmaceutical Statistics. 2018; 28(1):113–128.

# **Examples**

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
family = matrix(c(1, 1, 0, 0, 0, 0, 0, 0,
                0, 0, 1, 1, 0, 0, 0, 0,
                0, 0, 0, 0, 1, 1, 0, 0,
                0, 0, 0, 0, 0, 0, 1, 1),
               nrow=4, byrow=TRUE)
0, 0, 0, 0, 0, 0, 0, 0,
                1, 0, 0, 0, 0, 0, 0, 0,
                0, 1, 0, 0, 0, 0, 0, 0,
                0, 0, 1, 0, 0, 0, 0, 0,
                0, 0, 0, 1, 0, 0, 0, 0,
                0, 0, 0, 0, 1, 0, 0, 0,
                0, 0, 0, 0, 0, 1, 0, 0),
               nrow=8, byrow=TRUE)
parallel = matrix(0, 8, 8)
gamma = c(0.6, 0.6, 0.6, 1)
fmodmix(p, family, serial, parallel, gamma, test = "hommel", exhaust = 1)
```

fquantile

The quantiles of a survival distribution

# **Description**

Obtains the quantiles of a survival distribution.

fseqbon 23

# Usage

```
fquantile(S, probs, ...)
```

# Arguments

S The survival function of a univariate survival time.

probs The numeric vector of probabilities.
... Additional arguments to be passed to S.

### Value

A vector of length(probs) for the quantiles.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
fquantile(pweibull, probs = c(0.25, 0.5, 0.75),
shape = 1.37, scale = 1/0.818, lower.tail = FALSE)
```

fseqbon

Group sequential trials using Bonferroni-based graphical approaches

# Description

Obtains the test results for group sequential trials using graphical approaches based on weighted Bonferroni tests.

# Usage

```
fseqbon(
    w,
    G,
    alpha = 0.025,
    kMax,
    typeAlphaSpending = NULL,
    parameterAlphaSpending = NULL,
    incidenceMatrix = NULL,
    maxInformation = NULL,
    p,
    information,
    spendingTime = NULL
)
```

24 fseqbon

#### **Arguments**

W The vector of initial weights for elementary hypotheses.

G The initial transition matrix.

alpha The significance level. Defaults to 0.025.

kMax The maximum number of stages.

typeAlphaSpending

The vector of alpha spending functions. Each element is one of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF" if not provided.

parameterAlphaSpending

The vector of parameter values for the alpha spending functions. Each element corresponds to the value of Delta for "WT", rho for "sfKD", or gamma for "sfHSD". Defaults to missing if not provided.

incidenceMatrix

The incidence matrix indicating whether the specific hypothesis will be tested at the given look. The number of columns of incidenceMatrix must be equal to the maximum number of study looks (kMax). If not provided, defaults to testing each hypothesis at all study looks.

maxInformation The vector of target maximum information for each hypothesis. Defaults to a vector of 1s if not provided.

The matrix of raw p-values for each hypothesis by study look.

information The matrix of observed information for each hypothesis by study look.

spendingTime The spending time for alpha spending by study look. If not provided, it is the same as informationRates calculated from information and maxInformation.

### Value

р

A vector to indicate the first look the specific hypothesis is rejected (0 if the hypothesis is not rejected).

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### References

Willi Maurer and Frank Bretz. Multiple testing in group sequential trials using graphical approaches. Statistics in Biopharmaceutical Research. 2013; 5:311-320.

fstdmix 25

### **Examples**

fstdmix

Adjusted p-values for standard mixture gatekeeping procedures

# **Description**

Obtains the adjusted p-values for the standard gatekeeping procedures for multiplicity problems involving serial and parallel logical restrictions.

# Usage

```
fstdmix(
  p,
  family = NULL,
  serial,
  parallel,
  gamma,
  test = "hommel",
  exhaust = 1
)
```

# **Arguments**

p The raw p-values for elementary hypotheses.

family The matrix of family indicators for the hypotheses.

serial The matrix of serial rejection set for the hypotheses.

parallel The matrix of parallel rejection set for the hypotheses.

26 fstdmix

gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
test	The component multiple testing procedure. Options include "holm", "hochberg", or "hommel". Defaults to "hommel".
exhaust	Whether to use alpha-exhausting component testing procedure for the last family with active hypotheses. It defaults to TRUE.

# Value

A matrix of adjusted p-values.

# Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# References

Alex Dmitrienko and Ajit C Tamhane. Mixtures of multiple testing procedures for gatekeeping applications in clinical trials. Statistics in Medicine. 2011; 30(13):1473–1488.

```
p = c(0.0194, 0.0068, 0.0271, 0.0088, 0.0370, 0.0018, 0.0814, 0.0066)
0, 0, 1, 1, 0, 0, 0, 0,
               0, 0, 0, 0, 1, 1, 0, 0,
               0, 0, 0, 0, 0, 0, 1, 1),
             nrow=4, byrow=TRUE)
0, 0, 0, 0, 0, 0, 0, 0,
               1, 0, 0, 0, 0, 0, 0, 0,
               0, 1, 0, 0, 0, 0, 0, 0,
               0, 0, 1, 0, 0, 0, 0, 0,
               0, 0, 0, 1, 0, 0, 0, 0,
               0, 0, 0, 0, 1, 0, 0, 0,
               0, 0, 0, 0, 0, 1, 0, 0),
             nrow=8, byrow=TRUE)
parallel = matrix(0, 8, 8)
gamma = c(0.6, 0.6, 0.6, 1)
fstdmix(p, family, serial, parallel, gamma, test = "hommel", exhaust = 0)
```

fstp2seq 27

fstp2seq	Adjusted p-values for stepwise testing procedures for two sequences

# Description

Obtains the adjusted p-values for the stepwise gatekeeping procedures for multiplicity problems involving two sequences of hypotheses.

# Usage

```
fstp2seq(p, gamma, test = "hochberg", retest = TRUE)
```

# Arguments

р	The raw p-values for elementary hypotheses.
gamma	The truncation parameters for each family. The truncation parameter for the last family is automatically set to 1.
test	The component multiple testing procedure. It is either "Holm" or "Hochberg", and it defaults to "Hochberg".
retest	Whether to allow retesting. It defaults to TRUE.

# Value

A matrix of adjusted p-values.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

```
 p = c(0.0194,\ 0.0068,\ 0.0271,\ 0.0088,\ 0.0370,\ 0.0018,\ 0.0814,\ 0.0066)  gamma = c(0.6,\ 0.6,\ 0.6,\ 1) fstp2seq(p, gamma, test="hochberg", retest=1)
```

28 ftrunc

Adjusted p-values for Holm, Hochberg, and Hommel procedures

### **Description**

Obtains the adjusted p-values for possibly truncated Holm, Hochberg, and Hommel procedures.

### Usage

```
ftrunc(p, test = "hommel", gamma = 1)
```

# **Arguments**

p The raw p-values for elementary hypotheses.

The test to use, e.g., "holm", "hochberg", or "hommel" (default).

gamma The value of the truncation parameter. Defaults to 1 for the regular Holm,

Hochberg, or Hommel procedure.

### Value

A matrix of adjusted p-values.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### References

Alex Dmitrienko, Ajit C. Tamhane, and Brian L. Wiens. General multistage gatekeeping procedures. Biometrical Journal. 2008; 5:667-677.

fwgtmat 29

fwgtmat

Weight matrix for all intersection hypotheses

# **Description**

Obtains the weight matrix for all intersection hypotheses.

# Usage

```
fwgtmat(w = NA_real_, G = NA_real_)
```

# **Arguments**

w The vector of weights for elementary hypotheses.

G The transition matrix.

# Value

The weight matrix starting with the global null hypothesis.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

getAccrualDurationFromN

Accrual duration to enroll target number of subjects

# **Description**

Obtains the accrual duration to enroll the target number of subjects.

# Usage

```
getAccrualDurationFromN(
  nsubjects = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_)
```

# Arguments

nsubjects The vector of target number of subjects.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

#### Value

A vector of accrual durations.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### **Examples**

```
getAccrualDurationFromN(nsubjects = c(20, 150), accrualTime = c(0, 3), accrualIntensity = c(10, 20))
```

getADCI

Confidence interval after adaptation

# **Description**

Obtains the p-value, median unbiased point estimate, and confidence interval after the end of an adaptive trial.

### Usage

```
getADCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.25,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  L2 = NA_integer_,
  zL2 = NA_real_,
  INew = NA_real_,
```

```
MullerSchafer = 0L,
informationRatesNew = NA_real_,
efficacyStoppingNew = NA_integer_,
typeAlphaSpendingNew = "sf0F",
parameterAlphaSpendingNew = NA_real_,
spendingTimeNew = NA_real_)
```

#### **Arguments**

L The interim adaptation look of the primary trial.

zL The z-test statistic at the interim adaptation look of the primary trial.

IMax The maximum information of the primary trial.

kMax The maximum number of stages of the primary trial.

informationRates

The information rates of the primary trial.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.

 $\hbox{critical Values} \ \ \hbox{The upper boundaries on the $z$-test statistic scale for efficacy stopping for the}$ 

primary trial.

alpha The significance level of the primary trial. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime The error spending time of the primary trial. Defaults to missing, in which case,

it is the same as informationRates.

L2 The termination look of the secondary trial.

zL2 The z-test statistic at the termination look of the secondary trial.

INew The maximum information of the secondary trial.

MullerSchafer Whether to use the Muller and Schafer (2001) method for trial adaptation.

informationRatesNew

The spacing of looks of the secondary trial up to look L2.

efficacyStoppingNew

The indicators of whether efficacy stopping is allowed at each look of the secondary trial up to look L2. Defaults to true if left unspecified.

typeAlphaSpendingNew

The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpendingNew

The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTimeNew

The error spending time of the secondary trial up to look L2. Defaults to missing, in which case, it is the same as informationRatesNew.

#### Value

A data frame with the following variables:

- pvalue: p-value for rejecting the null hypothesis.
- the tahat: Median unbiased point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of confidence interval.
- upper: Upper bound of confidence interval.

# Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### References

Ping Gao, Lingyun Liu and Cyrus Mehta. Exact inference for adaptive group sequential designs. Stat Med. 2013;32(23):3991-4005.

#### See Also

```
adaptDesign
```

```
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)
t = des1$byStageResults$informationRates
# Muller & Schafer (2001) method to design the secondary trial:
des2 = adaptDesign(
  betaNew = 0.2, L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = −4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)
n2 = ceiling(des2$secondaryTrial$overallResults$information*4*20^2)
ns = round(n2*(1:3)/3)
 (des2 = adaptDesign(
   INew = n2/(4*20^2), L = L, zL = zL, theta = 5,
   kMax = 3, informationRates = t,
   alpha = 0.05, typeAlphaSpending = "sfHSD",
   parameterAlphaSpending = -4,
   MullerSchafer = TRUE,
   kNew = 3, informationRatesNew = ns/n2,
   typeAlphaSpendingNew = "sfHSD",
   parameterAlphaSpendingNew = -2))
# termination at the second look of the secondary trial
L2 = 2
delta2 = 6.86
sigma2 = 21.77
zL2 = delta2/sqrt(4/197*sigma2^2)
t2 = des2$secondaryTrial$byStageResults$informationRates[1:L2]
# confidence interval
getADCI(L = L, zL = zL,
        IMax = n/(4*sigma1^2), kMax = 3,
        informationRates = t,
        alpha = 0.05, typeAlphaSpending = "sfHSD",
        parameterAlphaSpending = -4,
        L2 = L2, zL2 = zL2,
        INew = n2/(4*sigma2^2),
        MullerSchafer = TRUE,
        informationRatesNew = t2,
        typeAlphaSpendingNew = "sfHSD",
        parameterAlphaSpendingNew = -2)
```

getADRCI

Repeated confidence interval after adaptation

### **Description**

Obtains the repeated p-value, conservative point estimate, and repeated confidence interval for an adaptive group sequential trial.

### Usage

```
getADRCI(
 L = NA_integer_,
  zL = NA_real_,
  IMax = NA\_real\_
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_,
 L2 = NA_integer_,
  zL2 = NA_real_,
  INew = NA_real_,
 MullerSchafer = 0L,
  informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_
)
```

# **Arguments**

L The interim adaptation look of the primary trial.

zL The z-test statistic at the interim adaptation look of the primary trial.

IMax The maximum information of the primary trial.

kMax The maximum number of stages of the primary trial.

informationRates

The information rates of the primary trial.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.

criticalValues The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.

alpha The significance level of the primary trial. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime The error spending time of the primary trial. Defaults to missing, in which case,

it is the same as informationRates.

L2 The look of interest in the secondary trial.

zL2 The z-test statistic at the look of the secondary trial.

INew The maximum information of the secondary trial.

MullerSchafer Whether to use the Muller and Schafer (2001) method for trial adaptation.

informationRatesNew

The spacing of looks of the secondary trial.

efficacyStoppingNew

The indicators of whether efficacy stopping is allowed at each look of the secondary trial up to look L2. Defaults to true if left unspecified.

 $type \verb|AlphaSpendingNew|$ 

The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpendingNew

The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTimeNew

The error spending time of the secondary trial. up to look L2. Defaults to missing, in which case, it is the same as informationRatesNew.

#### Value

A data frame with the following variables:

- pvalue: Repeated p-value for rejecting the null hypothesis.
- thetahat: Point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of repeated confidence interval.
- upper: Upper bound of repeated confidence interval.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### References

Cyrus R. Mehta, Peter Bauer, Martin Posch and Werner Brannath. Repeated confidence intervals for adaptive group sequential trials. Stat Med. 2007;26:5422–5433.

#### See Also

adaptDesign

```
# original group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))
# interim look results
L = 1
n1 = n/3
delta1 = 4.5
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)
t = des1$byStageResults$informationRates
# Muller & Schafer (2001) method to design the secondary trial:
des2 = adaptDesign(
  betaNew = 0.2, L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = −4,
  MullerSchafer = TRUE,
  kNew = 3, typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2)
n2 = ceiling(des2$secondaryTrial$overallResults$information*4*20^2)
ns = round(n2*(1:3)/3)
(des2 = adaptDesign(
  INew = n2/(4*20^2), L = L, zL = zL, theta = 5,
  kMax = 3, informationRates = t,
  alpha = 0.05, typeAlphaSpending = "sfHSD",
  parameterAlphaSpending = -4,
  MullerSchafer = TRUE,
  kNew = 3, informationRatesNew = ns/n2,
  typeAlphaSpendingNew = "sfHSD",
  parameterAlphaSpendingNew = -2))
```

getBound 37

```
# termination at the second look of the secondary trial
L2 = 2
delta2 = 6.86
sigma2 = 21.77
zL2 = delta2/sqrt(4/197*sigma2^2)
t2 = des2$secondaryTrial$byStageResults$informationRates[1:L2]
# repeated confidence interval
getADRCI(L = L, zL = zL,
         IMax = n/(4*sigma1^2), kMax = 3,
         informationRates = t,
         alpha = 0.05, typeAlphaSpending = "sfHSD",
         parameterAlphaSpending = -4,
         L2 = L2, zL2 = zL2,
         INew = n2/(4*sigma2^2),
         MullerSchafer = TRUE,
         informationRatesNew = t2,
         typeAlphaSpendingNew = "sfHSD",
         parameterAlphaSpendingNew = -2)
```

getBound

Efficacy boundaries for group sequential design

## **Description**

Obtains the efficacy stopping boundaries for a group sequential design.

## Usage

```
getBound(
   k = NA,
   informationRates = NA,
   alpha = 0.025,
   typeAlphaSpending = "sfOF",
   parameterAlphaSpending = NA,
   userAlphaSpending = NA,
   spendingTime = NA,
   efficacyStopping = NA
)
```

### **Arguments**

k Look number for the current analysis.

informationRates

Information rates up to the current look. Must be increasing and less than or equal to 1.

38 getCI

alpha

The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime

A vector of length k for the error spending time at each analysis. Must be increasing and less than or equal to 1. Defaults to missing, in which case, it is the same as informationRates.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

### **Details**

If typeAlphaSpending is "OF", "P", or "WT", then the boundaries will be based on equally spaced looks.

### Value

A numeric vector of critical values up to the current look.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
getBound(k = 2, informationRates = c(0.5,1),
alpha = 0.025, typeAlphaSpending = "sfOF")
```

getCI

Confidence interval after trial termination

### **Description**

Obtains the p-value, median unbiased point estimate, and confidence interval after the end of a group sequential trial.

getCI 39

### Usage

```
getCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_
```

## **Arguments**

L The termination look.

zL The z-test statistic at the termination look.

IMax The maximum information of the trial.

informationRates

The information rates up to look L.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage up to look L. Defaults to true if left unspecified.

criticalValues The upper boundaries on the z-test statistic scale for efficacy stopping up to look

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value of alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime The error spending time up to look L. Defaults to missing, in which case, it is the same as informationRates.

## Value

A data frame with the following components:

- pvalue: p-value for rejecting the null hypothesis.
- the tahat: Median unbiased point estimate of the parameter.

- cilevel: Confidence interval level.
- lower: Lower bound of confidence interval.
- upper: Upper bound of confidence interval.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## References

Anastasios A. Tsiatis, Gary L. Rosner and Cyrus R. Mehta. Exact confidence intervals following a group sequential test. Biometrics 1984;40:797-803.

## **Examples**

```
# group sequential design with 90% power to detect delta = 6
delta = 6
sigma = 17
n = 282
(des1 = getDesign(IMax = n/(4*sigma^2), theta = delta, kMax = 3,
                  alpha = 0.05, typeAlphaSpending = "sfHSD",
                  parameterAlphaSpending = -4))
# crossed the boundary at the second look
L = 2
n1 = n*2/3
delta1 = 7
sigma1 = 20
zL = delta1/sqrt(4/n1*sigma1^2)
# confidence interval
getCI(L = L, zL = zL, IMax = n/(4*sigma1^2),
      informationRates = c(1/3, 2/3), alpha = 0.05,
      typeAlphaSpending = "sfHSD", parameterAlphaSpending = -4)
```

getCP

Conditional power allowing for varying parameter values

## Description

Obtains the conditional power for specified incremental information given the interim results, parameter values, and data-dependent changes in the error spending function, as well as the number and spacing of interim looks.

## Usage

```
getCP(
  INew = NA_real_,
  L = NA_integer_,
  zL = NA_real_,
  theta = NA_real_,
  IMax = NA_real_,
  kMax = NA_integer_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  spendingTime = NA_real_,
  MullerSchafer = 0L,
  kNew = NA_integer_,
  informationRatesNew = NA_real_,
  efficacyStoppingNew = NA_integer_,
  futilityStoppingNew = NA_integer_,
  typeAlphaSpendingNew = "sfOF",
  parameterAlphaSpendingNew = NA_real_,
  typeBetaSpendingNew = "none",
  parameterBetaSpendingNew = NA_real_,
  spendingTimeNew = NA_real_,
  varianceRatio = 1
)
```

## Arguments

**INew** The maximum information of the secondary trial. ı The interim adaptation look of the primary trial. zL The z-test statistic at the interim adaptation look of the primary trial. A scalar or a vector of parameter values of length kMax + kMax - L if MullerSchafer theta = FALSE or length kMax + kNew if MullerSchafer = TRUE. The maximum information of the primary trial. **IMax** The maximum number of stages of the primary trial. kMax informationRates The information rates of the primary trial. efficacyStopping Indicators of whether efficacy stopping is allowed at each stage of the primary

trial. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage of the primary trial. Defaults to true if left unspecified.

critical Values The upper boundaries on the z-test statistic scale for efficacy stopping for the primary trial.

alpha

The significance level of the primary trial. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending for the primary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value of alpha spending for the primary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending for the primary trial. Cumulative alpha spent up to each stage.

futilityBounds The lower boundaries on the z-test statistic scale for futility stopping for the primary trial. Defaults to rep(-6, kMax-1) if left unspecified.

typeBetaSpending

The type of beta spending for the primary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value of beta spending for the primary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

The error spending time of the primary trial. Defaults to missing, in which case, spendingTime it is the same as informationRates.

Whether to use the Muller and Schafer (2001) method for trial adaptation.

**kNew** The number of looks of the secondary trial.

informationRatesNew

MullerSchafer

The spacing of looks of the secondary trial.

efficacyStoppingNew

The indicators of whether efficacy stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

futilityStoppingNew

The indicators of whether futility stopping is allowed at each look of the secondary trial. Defaults to true if left unspecified.

typeAlphaSpendingNew

The type of alpha spending for the secondary trial. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang &

Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpendingNew

The parameter value of alpha spending for the secondary trial. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### typeBetaSpendingNew

The type of beta spending for the secondary trial. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpendingNew

The parameter value of beta spending for the secondary trial. Corresponds to rho for "sfKD", and gamma for "sfHSD".

#### spendingTimeNew

The error spending time of the secondary trial. Defaults to missing, in which case, it is the same as informationRatesNew.

varianceRatio The ratio of the variance under H0 to the variance under H1.

#### Value

The conditional power given the interim results, parameter values, and data-dependent design changes.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### References

Cyrus R. Mehta and Stuart J. Pocock. Adaptive increase in sample size when interim results are promising: A practical guide with examples. Stat Med. 2011;30:3267–3284.

#### See Also

```
getDesign
```

## **Examples**

```
# Conditional power calculation with delayed treatment effect
# Two interim analyses have occurred with 179 and 266 events,
# respectively. The observed hazard ratio at the second interim
# look is 0.81.

trialsdt = as.Date("2020-03-04")  # trial start date
iadt = c(as.Date("2022-02-01"), as.Date("2022-11-01")) # interim dates
```

```
mo1 = as.numeric(iadt - trialsdt + 1)/30.4375
                                                       # interim months
# Assume a piecewise Poisson enrollment process with a 8-month ramp-up
# and 521 patients were enrolled after 17.94 months
N = 521
                         # total number of patients
Ta = 17.94
                         # enrollment duration
Ta1 = 8
                          # assumed end of enrollment ramp-up
enrate = N / (Ta - Ta1/2) # enrollment rate after ramp-up
# Assume a median survival of 16.7 months for the control group, a
# 5-month delay in treatment effect, and a hazard ratio of 0.7 after
# the delay
lam1 = log(2)/16.7 # control group hazard of exponential distribution
t1 = 5
                    # months of delay in treatment effect
hr = 0.7
                    # hazard ratio after delay
lam2 = hr*lam1
                  # treatment group hazard after delay
# Assume an annual dropout rate of 5%
gam = -\log(1-0.05)/12 # hazard for dropout
# The original target number of events was 298 and the new target is 335
mo2 <- caltime(</pre>
  nevents = c(298, 335),
  allocationRatioPlanned = 1,
  accrualTime = seq(0, Ta1),
  accrualIntensity = enrate*seq(1, Ta1+1)/(Ta1+1),
  piecewiseSurvivalTime = c(0, t1),
  lambda1 = c(lam1, lam2),
  lambda2 = c(lam1, lam1),
  gamma1 = gam,
  gamma2 = gam,
  accrualDuration = Ta,
  followupTime = 1000)
# expected number of events and average hazard ratios
(lr1 <- lrstat(
  time = c(mo1, mo2),
  accrualTime = seq(0, Ta1),
  accrualIntensity = enrate*seq(1, Ta1+1)/(Ta1+1),
  piecewiseSurvivalTime = c(0, t1),
  lambda1 = c(lam1, lam2),
  lambda2 = c(lam1, lam1),
  gamma1 = gam,
  gamma2 = gam,
  accrualDuration = Ta,
  followupTime = 1000,
  predictTarget = 3))
hr2 = 0.81
                              # observed hazard ratio at interim 2
z2 = (-\log(hr2))*sqrt(266/4) # corresponding z-test statistic value
# expected mean of -log(HR) at the original looks and the new final look
```

getDesign 45

```
theta = -log(lr1$HR[c(1,2,3,4)])

# conditional power with sample size increase
getCP(INew = (335 - 266)/4,
        L = 2, zL = z2, theta = theta,
        IMax = 298/4, kMax = 3,
        informationRates = c(179, 266, 298)/298,
        alpha = 0.025, typeAlphaSpending = "sfOF")
```

getDesign

Power and sample size for a generic group sequential design

# Description

Obtains the maximum information and stopping boundaries for a generic group sequential design assuming a constant treatment effect, or obtains the power given the maximum information and stopping boundaries.

## Usage

```
getDesign(
  beta = NA_real_,
  IMax = NA_real_,
  theta = NA_real_,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_,
  varianceRatio = 1
)
```

## **Arguments**

beta The type II error.

IMax The maximum information. Either beta or IMax should be provided while the other one should be missing.

46 getDesign

theta The parameter value.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

varianceRatio The ratio of the variance under H0 to the variance under H1. getDesign 47

#### Value

An S3 class design object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyTheta: The efficacy boundaries on the parameter scale.
  - futilityTheta: The futility boundaries on the parameter scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### References

Christopher Jennison, Bruce W. Turnbull. Group Sequential Methods with Applications to Clinical Trials. Chapman & Hall/CRC: Boca Raton, 2000, ISBN:0849303168

### **Examples**

```
# Example 1: obtain the maximum information given power
(design1 <- getDesign(
   beta = 0.2, theta = -log(0.7),
   kMax = 2, informationRates = c(0.5,1),
   alpha = 0.025, typeAlphaSpending = "sfOF",
   typeBetaSpending = "sfP"))

# Example 2: obtain power given the maximum information
(design2 <- getDesign(
   IMax = 72.5, theta = -log(0.7),
   kMax = 3, informationRates = c(0.5, 0.75, 1),
   alpha = 0.025, typeAlphaSpending = "sfOF",
   typeBetaSpending = "sfP"))</pre>
```

getDesignAgreement

Power and sample size for Cohen's kappa

# Description

Obtains the power given sample size or obtains the sample size given power for Cohen's kappa.

## Usage

```
getDesignAgreement(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  kappaH0 = NA_real_,
  kappa = NA_real_,
  p1 = NA_real_,
  p2 = NA_real_,
  rounding = TRUE,
  alpha = 0.025
)
```

getDesignAgreement 49

## Arguments

beta The type II error.

n The total sample size.

ncats The number of categories.

kappaH0 The kappa coefficient under the null hypothesis.

kappa The kappa coefficient under the alternative hypothesis.

p1 The marginal probabilities for the first rater.

p2 The marginal probabilities for the second rater. Defaults to be equal to the

marginal probabilities for the first rater if not provided.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

alpha The one-sided significance level. Defaults to 0.025.

#### **Details**

The kappa coefficient is defined as

$$\kappa = \frac{\pi_o - \pi_e}{1 - \pi_e},$$

where  $\pi_o = \sum_i \pi_{ii}$  is the observed agreement, and  $\pi_e = \sum_i \pi_{i.} \pi_{.i}$  is the expected agreement by chance.

By Fleiss et al. (1969), the variance of  $\hat{\kappa}$  is given by

$$Var(\hat{\kappa}) = \frac{v_1}{n},$$

where

$$v_1 = \frac{Q_1 + Q_2 - Q_3 - Q_4}{(1 - \pi_e)^4},$$

$$Q_1 = \pi_o (1 - \pi_e)^2,$$

$$Q_2 = (1 - \pi_o)^2 \sum_i \sum_j \pi_{ij} (\pi_{i.} + \pi_{.j})^2,$$

$$Q_3 = 2(1 - \pi_o)(1 - \pi_e) \sum_i \pi_{ii} (\pi_{i.} + \pi_{.i}),$$

$$Q_4 = (\pi_o \pi_e - 2\pi_e + \pi_o)^2.$$

Given  $\kappa$  and marginals  $\{(\pi_{i}, \pi_{i}) : i = 1, ..., k\}$ , we obtain  $\pi_{o}$ . The only unknowns are the double summation in  $Q_{2}$  and the single summation in  $Q_{3}$ .

We find the optimal configuration of cell probabilities that yield the maximum variance of  $\hat{\kappa}$  by treating the problem as a linear programming problem with constraints to match the given marginal probabilities and the observed agreement and ensure that the cell probabilities are nonnegative. This is an extension of Flack et al. (1988) by allowing unequal marginal probabilities of the two raters.

We perform the optimization under both the null and alternative hypotheses to obtain  $\max Var(\hat{\kappa}|\kappa = \kappa_0)$  and  $\max Var(\hat{\kappa}|\kappa = \kappa_1)$  for a single subject, and then calculate the sample size or power according to the following equation:

$$\sqrt{n}|\kappa - \kappa_0| = z_{1-\alpha} \sqrt{\max Var(\hat{\kappa}|\kappa = \kappa_0)} + z_{1-\beta} \sqrt{\max Var(\hat{\kappa}|\kappa = \kappa_1)}.$$

50 getDesignANOVA

### Value

An S3 class designAgreement object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The one-sided significance level.
- n: The total sample size.
- ncats: The number of categories.
- kappaH0: The kappa coefficient under the null hypothesis.
- kappa: The kappa coefficient under the alternative hypothesis.
- p1: The marginal probabilities for the first rater.
- p2: The marginal probabilities for the second rater.
- piH0: The cell probabilities that maximize the variance of estimated kappa under H0.
- pi: The cell probabilities that maximize the variance of estimated kappa under H1.
- rounding: Whether to round up sample size.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## References

V. F. Flack, A. A. Afifi, and P. A. Lachenbruch. Sample size determinations for the two rater kappa statistic. Psychometrika 1988; 53:321-325.

# Examples

```
(design1 <- getDesignAgreement(
  beta = 0.2, n = NA, ncats = 4, kappaH0 = 0.4, kappa = 0.6,
  p1 = c(0.1, 0.2, 0.3, 0.4), p2 = c(0.15, 0.2, 0.24, 0.41),
  rounding = TRUE, alpha = 0.05))</pre>
```

getDesignANOVA

Power and sample size for one-way ANOVA

### **Description**

Obtains the power and sample size for one-way analysis of variance.

getDesignANOVA 51

### Usage

```
getDesignANOVA(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  allocationRatioPlanned = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

## **Arguments**

beta The type II error.

n The total sample size.

ngroups The number of treatment groups.

means The treatment group means.

stDev The common standard deviation.

allocationRatioPlanned

Allocation ratio for the treatment groups. It has length ngroups - 1 or ngroups. If it is of length ngroups - 1, then the last treatment group will assume value 1

for allocation ratio.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

alpha The two-sided significance level. Defaults to 0.05.

# **Details**

Let  $\{\mu_i: i=1,\ldots,k\}$  denote the group means, and  $\{r_i: i=1,\ldots,k\}$  denote the randomization probabilities to the k treatment groups. Let  $\sigma$  denote the common standard deviation, and n denote the total sample size. Then the F-statistic

$$F = \frac{SSR/(k-1)}{SSE/(n-k)} \sim F_{k-1,n-k,\lambda},$$

where

$$\lambda = n \sum_{i=1}^{k} r_i (\mu_i - \bar{\mu})^2 / \sigma^2$$

is the noncentrality parameter, and  $\bar{\mu} = \sum_{i=1}^{k} r_i \mu_i$ .

#### Value

An S3 class designANOVA object with the following components:

• power: The power to reject the null hypothesis that there is no difference among the treatment groups.

- alpha: The two-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The common standard deviation.
- effectsize: The effect size.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
(design1 <- getDesignANOVA( beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0), stDev = 3.5, allocationRatioPlanned = c(2, 2, 2, 1), alpha = 0.05))
```

getDesignANOVAContrast

Power and sample size for one-way ANOVA contrast

### **Description**

Obtains the power and sample size for a single contrast in one-way analysis of variance.

## Usage

```
getDesignANOVAContrast(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  contrast = NA_real_,
  meanContrastH0 = 0,
  allocationRatioPlanned = NA_real_,
  rounding = TRUE,
  alpha = 0.025
)
```

#### **Arguments**

beta The type II error.

n The total sample size.

ngroups The number of treatment groups.

means The treatment group means.

stDev The common standard deviation.

contrast The coefficients for the single contrast.

meanContrastH0 The mean of the contrast under the null hypothesis.

allocationRatioPlanned

Allocation ratio for the treatment groups. It has length ngroups - 1 or ngroups. If it is of length ngroups - 1, then the last treatment group will assume value 1

for allocation ratio.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

alpha The one-sided significance level. Defaults to 0.025.

#### Value

An S3 class designANOVAContrast object with the following components:

- power: The power to reject the null hypothesis for the treatment contrast.
- alpha: The one-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The common standard deviation.
- contrast: The coefficients for the single contrast.
- meanContrastH0: The mean of the contrast under the null hypothesis.
- meanContrast: The mean of the contrast under the alternative hypothesis.
- effectsize: The effect size.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
(design1 <- getDesignANOVAContrast(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 3.5, contrast = c(1, 1, 1, -3)/3,
  allocationRatioPlanned = c(2, 2, 2, 1),
  alpha = 0.025))</pre>
```

getDesignEquiv	Power and sample size for a generic group sequential equivalence design
----------------	---

## **Description**

Obtains the maximum information and stopping boundaries for a generic group sequential equivalence design assuming a constant treatment effect, or obtains the power given the maximum information and stopping boundaries.

## Usage

```
getDesignEquiv(
  beta = NA_real_,
  IMax = NA_real_,
  thetaLower = NA_real_,
  thetaUpper = NA_real_,
  theta = 0,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_,
  varianceRatioH10 = 1,
  varianceRatioH20 = 1,
  varianceRatioH12 = 1,
  varianceRatioH21 = 1
)
```

# **Arguments**

beta The type II error.

IMax The maximum information. Either beta or IMax should be provided while the

other one should be missing.

thetaLower The parameter value at the lower equivalence limit.

thetaUpper The parameter value at the upper equivalence limit.

theta The parameter value under the alternative hypothesis.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if

left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests, e.g., 0.05. typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

varianceRatioH10

The ratio of the variance under H10 to the variance under H1.

varianceRatioH20

The ratio of the variance under H20 to the variance under H1.

varianceRatioH12

The ratio of the variance under H10 to the variance under H20.

varianceRatioH21

The ratio of the variance under H20 to the variance under H10.

## **Details**

Consider the equivalence design with two one-sided hypotheses:

$$H_{10}: \theta < \theta_{10},$$

$$H_{20}: \theta \geq \theta_{20}.$$

We reject  $H_{10}$  at or before look k if

$$Z_{1j} = (\hat{\theta}_j - \theta_{10}) \sqrt{\frac{n_j}{v_{10}}} \ge b_j$$

for some  $j=1,\ldots,k$ , where  $\{b_j:j=1,\ldots,K\}$  are the critical values associated with the specified alpha-spending function, and  $v_{10}$  is the null variance of  $\hat{\theta}$  based on the restricted maximum likelihood (reml) estimate of model parameters subject to the constraint imposed by  $H_{10}$  for one sampling unit drawn from  $H_1$ . For example, for estimating the risk difference  $\theta=\pi_1-\pi_2$ , the asymptotic limits of the reml estimates of  $\pi_1$  and  $\pi_2$  subject to the constraint imposed by  $H_{10}$  are given by

$$(\tilde{\pi}_1, \tilde{\pi}_2) = f(\theta_{10}, r, r\pi_1, 1 - r, (1 - r)\pi_2),$$

where  $f(\theta_0, n_1, y_1, n_2, y_2)$  is the function to obtain the reml of  $\pi_1$  and  $\pi_2$  subject to the constraint that  $\pi_1 - \pi_2 = \theta_0$  with observed data  $(n_1, y_1, n_2, y_2)$  for the number of subjects and number of responses in the active treatment and control groups, r is the randomization probability for the active treatment group, and

$$v_{10} = \frac{\tilde{\pi}_1(1 - \tilde{\pi}_1)}{r} + \frac{\tilde{\pi}_2(1 - \tilde{\pi}_2)}{1 - r}.$$

Let  $I_j = n_j/v_1$  denote the information for  $\theta$  at the jth look, where

$$v_1 = \frac{\pi_1(1-\pi_1)}{r} + \frac{\pi_2(1-\pi_2)}{1-r}$$

denotes the variance of  $\hat{\theta}$  under  $H_1$  for one sampling unit. It follows that

$$(Z_{1j} \ge b_j) = (Z_j \ge w_{10}b_j + (\theta_{10} - \theta)\sqrt{I_j}),$$

where  $Z_j = (\hat{\theta}_j - \theta)\sqrt{I_j}$ , and  $w_{10} = \sqrt{v_{10}/v_1}$ .

Similarly, we reject  $H_{20}$  at or before look k if

$$Z_{2j} = (\hat{\theta}_j - \theta_{20}) \sqrt{\frac{n_j}{v_{20}}} \le -b_j$$

for some  $j=1,\ldots,k$ , where  $v_{20}$  is the null variance of  $\hat{\theta}$  based on the reml estimate of model parameters subject to the constraint imposed by  $H_{20}$  for one sampling unit drawn from  $H_1$ . We have

$$(Z_{2j} \le -b_j) = (Z_j \le -w_{20}b_j + (\theta_{20} - \theta)\sqrt{I_j}),$$

where  $w_{20} = \sqrt{v_{20}/v_1}$ .

Let  $l_j=w_{10}b_j+(\theta_{10}-\theta)\sqrt{I_j}$ , and  $u_j=-w_{20}b_j+(\theta_{20}-\theta)\sqrt{I_j}$ . The cumulative probability to reject  $H_0=H_{10}\cup H_{20}$  at or before look k under the alternative hypothesis  $H_1$  is given by

$$P_{\theta}\left(\bigcup_{j=1}^{k}(Z_{1j} \ge b_j) \cap \bigcup_{j=1}^{k}(Z_{2j} \le -b_j)\right) = p_1 + p_2 + p_{12},$$

where

$$p_1 = P_{\theta} \left( \bigcup_{j=1}^k (Z_{1j} \ge b_j) \right) = P_{\theta} \left( \bigcup_{j=1}^k (Z_j \ge l_j) \right),$$
  
$$p_2 = P_{\theta} \left( \bigcup_{j=1}^k (Z_{2j} \le -b_j) \right) = P_{\theta} \left( \bigcup_{j=1}^k (Z_j \le u_j) \right),$$

and

$$p_{12} = P_{\theta} \left( \bigcup_{j=1}^{k} \{ (Z_j \ge l_j) \cup (Z_j \le u_j) \} \right).$$

Of note, both  $p_1$  and  $p_2$  can be evaluated using one-sided exit probabilities for group sequential designs. If there exists  $j \leq k$  such that  $l_j \leq u_j$ , then  $p_{12} = 1$ . Otherwise,  $p_{12}$  can be evaluated using two-sided exit probabilities for group sequential designs.

To evaluate the type I error of the equivalence trial under  $H_{10}$ , we first match the information under  $H_{10}$  with the information under  $H_{1}$ . For example, for estimating the risk difference for two independent samples, the sample size  $n_{10}$  under  $H_{10}$  must satisfy

$$\frac{1}{n_{10}} \left( \frac{(\pi_2 + \theta_{10})(1 - \pi_2 - \theta_{10})}{r} + \frac{\pi_2(1 - \pi_2)}{1 - r} \right) = \frac{1}{n} \left( \frac{\pi_1(1 - \pi_1)}{r} + \frac{\pi_2(1 - \pi_2)}{1 - r} \right).$$

Then we obtain the reml estimates of  $\pi_1$  and  $\pi_2$  subject to the constraint imposed by  $H_{20}$  for one sampling unit drawn from  $H_{10}$ ,

$$(\tilde{\pi}_{10}, \tilde{\pi}_{20}) = f(\theta_{20}, r, r(\pi_2 + \theta_{10}), 1 - r, (1 - r)\pi_2).$$

Let  $t_i$  denote the information fraction at look j. Define

$$\tilde{v}_1 = \frac{(\pi_2 + \theta_{10})(1 - \pi_2 - \theta_{10})}{r} + \frac{\pi_2(1 - \pi_2)}{1 - r},$$

and

$$\tilde{v}_{20} = \frac{\tilde{\pi}_{10}(1 - \tilde{\pi}_{10})}{r} + \frac{\tilde{\pi}_{20}(1 - \tilde{\pi}_{20})}{1 - r}.$$

The cumulative rejection probability under  $H_{10}$  at or before look k is given by

$$P_{\theta_{10}}\left(\bigcup_{j=1}^{k} \{(\hat{\theta}_{j} - \theta_{10})\sqrt{n_{10}t_{j}/\tilde{v}_{1}} \ge b_{j}\} \cap \bigcup_{j=1}^{k} \{(\hat{\theta}_{j} - \theta_{20})\sqrt{n_{10}t_{j}/\tilde{v}_{20}} \le -b_{j}\}\right) = q_{1} + q_{2} + q_{12},$$

where

$$q_1 = P_{\theta_{10}} \left( \bigcup_{j=1}^k \{ (\hat{\theta}_j - \theta_{10}) \sqrt{n_{10} t_j / \tilde{v}_1} \ge b_j \} \right) = P_{\theta_{10}} \left( \bigcup_{j=1}^k (Z_j \ge b_j) \right),$$

$$q_2 = P_{\theta_{10}} \left( \cup_{j=1}^k \{ (\hat{\theta}_j - \theta_{20}) \sqrt{n_{10} t_j / \tilde{v}_{20}} \le -b_j \} \right) = P_{\theta_{10}} \left( \cup_{j=1}^k (Z_j \le -b_j w_{21} + (\theta_{20} - \theta_{10}) \sqrt{I_j}) \right),$$

and

$$q_{12} = P_{\theta_{10}} \left( \cup_{j=1}^k \{ (Z_j \geq b_j) \cup (Z_j \leq -w_{21}b_j + (\theta_{20} - \theta_{10})\sqrt{I_j}) \} \right).$$

Here  $Z_j=(\hat{\theta}_j-\theta_{10})\sqrt{I_j}$ , and  $w_{21}=\sqrt{\tilde{v}_{20}/\tilde{v}_1}$ . Of note,  $q_1,q_2$ , and  $q_{12}$  can be evaluated using group sequential exit probabilities. Similarly, we can define  $\tilde{v}_2,\,\tilde{v}_{10},\,$  and  $w_{12}=\sqrt{\tilde{v}_{10}/\tilde{v}_2},\,$  and evaluate the type I error under  $H_{20}$ .

The variance ratios correspond to

varianceRatioH10 = 
$$v_{10}/v_1$$
,

varianceRatioH20 = 
$$v_{20}/v_1$$
,

varianceRatioH12 = 
$$\tilde{v}_{10}/\tilde{v}_2$$
,

varianceRatioH21 = 
$$\tilde{v}_{20}/\tilde{v}_1$$
.

If the alternative variance is used, then the variance ratios are all equal to 1.

#### Value

An S3 class designEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - thetaLower: The parameter value at the lower equivalence limit.
  - thetaUpper: The parameter value at the upper equivalence limit.
  - theta: The parameter value under the alternative hypothesis.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.

- expectedInformationH20: The expected information under H20.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative probability for efficacy stopping under H10.
  - cumulativeAttainedAlphaH20: The cumulative probability for efficacy stopping under H20.
  - efficacyThetaLower: The efficacy boundaries on the parameter scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacyThetaUpper: The efficacy boundaries on the parameter scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
- settings: A list containing the following components:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
# Example 1: obtain the maximum information given power
(design1 <- getDesignEquiv(
  beta = 0.2, thetaLower = log(0.8), thetaUpper = log(1.25),
  kMax = 2, informationRates = c(0.5, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: obtain power given the maximum information
(design2 <- getDesignEquiv(
  IMax = 72.5, thetaLower = log(0.7), thetaUpper = -log(0.7),
  kMax = 3, informationRates = c(0.5, 0.75, 1),
  alpha = 0.05, typeAlphaSpending = "sfOF"))</pre>
```

getDesignFisherExact 59

getDesignFisherExact Power and sample size for Fisher's exact test for two proportions

## **Description**

Obtains the power given sample size or obtains the sample size given power for Fisher's exact test for two proportions.

## Usage

```
getDesignFisherExact(
  beta = NA_real_,
  n = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

## **Arguments**

	beta	The type II error.
	n	The total sample size.
	pi1	The assumed probability for the active treatment group.
	pi2	The assumed probability for the control group.
allocationRatioPlanned		
		Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
	alpha	The two-sided significance level. Defaults to 0.05.

## Value

A data frame with the following variables:

- alpha: The two-sided significance level.
- power: The power.
- n: The sample size.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

60 getDesignLogistic

# **Examples**

```
(design1 <- getDesignFisherExact(
  beta = 0.2, pi1 = 0.5, pi2 = 0.2, alpha = 0.05))</pre>
```

 ${\tt getDesignLogistic}$ 

Power and sample size for logistic regression

# **Description**

Obtains the power given sample size or obtains the sample size given power for logistic regression of a binary response given the covariate of interest and other covariates.

# Usage

```
getDesignLogistic(
  beta = NA_real_,
  n = NA_real_,
  ncovariates = NA_integer_,
  nconfigs = NA_integer_,
  x = NA_real_,
  pconfigs = NA_real_,
  corr = 0,
  oddsratios = NA_real_,
  responseprob = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

## **Arguments**

beta	The type II error.
n	The total sample size.
ncovariates	The number of covariates.
nconfigs	The number of configurations of discretized covariate values.
X	The matrix of covariate values.
pconfigs	The vector of probabilities for the configurations.
corr	The multiple correlation between the predictor and other covariates. Defaults to $0$ .
oddsratios	The odds ratios for one unit increase in the covariates.
responseprob	The response probability in the full model when all predictor variables are equal to their means.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

getDesignLogistic 61

#### **Details**

We consider the logistic regression of a binary response variable Y on a set of predictor variables  $x=(x_1,\ldots,x_K)^T$  with  $x_1$  being the covariate of interest:  $\log\frac{P(Y_i=1)}{1-P(Y_i=1)}=\psi_0+x_i^T\psi$ , where  $\psi=(\psi_1,\ldots,\psi_K)^T$ . Similar to Self et al (1992), we assume that all covariates are either inherently discrete or discretized from continuous distributions (e.g. using the quantiles). Let m denote the total number of configurations of the covariate values. Let

$$\pi_i = P(x = x_i), i = 1, \dots, m$$

denote the probabilities for the configurations of the covariates under independence. The likelihood ratio test statistic for testing  $H_0: \psi_1 = 0$  can be approximated by a noncentral chi-square distribution with one degree of freedom and noncentrality parameter

$$\Delta = 2\sum_{i=1}^{m} \pi_i [b'(\theta_i)(\theta_i - \theta_i^*) - \{b(\theta_i) - b(\theta_i^*)\}],$$

where

$$\theta_i = \psi_0 + \sum_{j=1}^k \psi_j x_{ij},$$

$$\theta_i^* = \psi_0^* + \sum_{j=2}^k \psi_j^* x_{ij},$$

for  $\psi_0^* = \psi_0 + \psi_1 \mu_1$ , and  $\psi_j^* = \psi_j$  for j = 2, ..., K. Here  $\mu_1$  is the mean of  $x_1$ , e.g.,  $\mu_1 = \sum_i \pi_i x_{i1}$ . In addition, by formulating the logistic regression in the framework of generalized linear models,

$$b(\theta) = \log(1 + \exp(\theta)),$$

and

$$b'(\theta) = \frac{\exp(\theta)}{1 + \exp(\theta)}.$$

The regression coefficients  $\psi$  can be obtained by taking the log of the odds ratios for the covariates. The intercept  $\psi_0$  can be derived as

$$\psi_0 = \log(\bar{\mu}/(1-\bar{\mu})) - \sum_{j=1}^K \psi_j \mu_j,$$

where  $\bar{\mu}$  denotes the response probability when all predictor variables are equal to their means.

Finally, let  $\rho$  denote the multiple correlation between the predictor and other covariates. The non-centrality parameter of the chi-square test is adjusted downward by multiplying by  $1 - \rho^2$ .

## Value

An S3 class designLogistic object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.

62 getDesignLogistic

- n: The total sample size.
- ncovariates: The number of covariates.
- nconfigs: The number of configurations of discretized covariate values.
- x: The matrix of covariate values.
- pconfigs: The vector of probabilities for the configurations.
- corr: The multiple correlation between the predictor and other covariates.
- oddsratios: The odds ratios for one unit increase in the covariates.
- responseprob: The response probability in the full model when all predictor variables are equal to their means.
- effectsize: The effect size for the chi-square test.
- rounding: Whether to round up sample size.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### References

Steven G. Self, Robert H. Mauritsen and Jill Ohara. Power calculations for likelihood ratio tests in generalized linear models. Biometrics 1992; 48:31-39.

### **Examples**

```
# two ordinal covariates
x1 = c(5, 10, 15, 20)
px1 = c(0.2, 0.3, 0.3, 0.2)
x2 = c(2, 4, 6)
px2 = c(0.4, 0.4, 0.2)
# discretizing a normal distribution with mean 4 and standard deviation 2
nbins = 10
x3 = qnorm(((1:nbins) - 0.5)/nbins)*2 + 4
px3 = rep(1/nbins, nbins)
# combination of covariate values
nconfigs = length(x1)*length(x2)*length(x3)
x = expand.grid(x3 = x3, x2 = x2, x1 = x1)
x = as.matrix(x[, ncol(x):1])
# probabilities for the covariate configurations under independence
pconfigs = as.numeric(px1 %x% px2 %x% px3)
# convert the odds ratio for the predictor variable in 5-unit change
# to the odds ratio in 1-unit change
(design1 <- getDesignLogistic(</pre>
 beta = 0.1, ncovariates = 3,
  nconfigs = nconfigs,
  x = x,
```

getDesignMeanDiff 63

```
pconfigs = pconfigs,
oddsratios = c(1.2^{(1/5)}, 1.4, 1.3),
responseprob = 0.25,
alpha = 0.1))
```

getDesignMeanDiff

Group sequential design for two-sample mean difference

## **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean difference.

# Usage

```
getDesignMeanDiff(
 beta = NA_real_,
 n = NA_real_,
 meanDiffH0 = 0,
 meanDiff = 0.5,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

## **Arguments**

beta The type II error.

n The total sample size.

meanDiffH0 The mean difference under the null hypothesis. Defaults to 0.

meanDiff The mean difference under the alternative hypothesis.

64 getDesignMeanDiff

stDev The standard deviation.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

getDesignMeanDiff 65

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designMeanDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanDiffH0: The mean difference under the null hypothesis.
  - meanDiff: The mean difference under the alternative hypothesis.
  - stDev: The standard deviation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.

- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
- futilityMeanDiff: The futility boundaries on the mean difference scale.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameter Alpha Spending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiff(
  beta = NA, n = 456, meanDiff = 9, stDev = 32,
  kMax = 5, alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: sample size calculation for two-sample t-test
(design2 <- getDesignMeanDiff(
  beta = 0.1, n = NA, meanDiff = 0.3, stDev = 1,
  normalApproximation = FALSE, alpha = 0.025))</pre>
```

getDesignMeanDiffCarryover

Power and sample size for direct treatment effects in crossover trials accounting for carryover effects

### **Description**

Obtains the power and sample size for direct treatment effects in crossover trials accounting for carryover effects.

## Usage

```
getDesignMeanDiffCarryover(
  beta = NA_real_,
  n = NA_real_,
  meanDiffH0 = 0,
  meanDiff = 0.5,
  stDev = 1,
  corr = 0.5,
  design = NA_real_,
  cumdrop = NA_real_,
  allocationRatioPlanned = NA_real_,
  normalApproximation = FALSE,
  rounding = TRUE,
  alpha = 0.025
)
```

# Arguments

	beta	The type II error.
	n	The total sample size.
	meanDiffH0	The mean difference at the last time point under the null hypothesis. Defaults to $0$ .
	meanDiff	The mean difference at the last time point under the alternative hypothesis.
	stDev	The standard deviation for within-subject random error.
	corr	The intra-subject correlation due to subject random effect.
	design	The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.
	cumdrop	The cumulative dropout rate over periods.
allocationRatioPlanned		
		Allocation ratio for the sequences. Defaults to equal randomization if not provided.
normalApproximation		tion
		The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
	rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

## **Details**

alpha

The linear mixed-effects model to assess the direct treatment effect in the presence of carryover treatment effect is given by

The one-sided significance level. Defaults to 0.025.

$$y_{ijk} = \mu + \alpha_i + b_{ij} + \gamma_k + \tau_{d(i,k)} + \lambda_{c(i,k-1)} + e_{ijk},$$
  
$$i = 1, \dots, n; j = 1, \dots, r_i; k = 1, \dots, p; d, c = 1, \dots, t,$$

where  $\mu$  is the general mean,  $\alpha_i$  is the effect of the *i*th treatment sequence,  $b_{ij}$  is the random effect with variance  $\sigma_b^2$  for the *j*the subject of the *i*th treatment sequence,  $\gamma_k$  is the period effect, and  $e_{ijk}$  is the random error with variance  $\sigma^2$  for the subject in period k. The direct effect of the treatment administered in period k of sequence i is  $\tau_{d(i,k)}$ , and  $\lambda_{c(i,k-1)}$  is the carryover effect of the treatment administered in period k-1 of sequence i. The value of the carryover effect for the observed response in the first period is  $\lambda_{c(i,0)} = 0$  since there is no carryover effect in the first period. The intra-subject correlation due to the subject random effect is

$$\rho = \frac{\sigma_b^2}{\sigma_b^2 + sigma^2}.$$

By constructing the design matrix X for the linear model with a compound symmetry covariance matrix for the response vector of a subject, we can obtain

$$Var(\hat{\beta}) = (X'V^{-1}X)^{-1}.$$

The covariance matrix for the direct treatment effects and the carryover treatment effects can be extracted from the appropriate sub-matrices. The covariance matrix for the direct treatment effects without accounting for the carryover treatment effects can be obtained by omitting the carryover effect terms from the model.

The power and relative efficiency are for the direct treatment effect comparing the first treatment to the last treatment accounting for carryover effects.

The degrees of freedom for the t-test can be calculated as the total number of observations minus the number of subjects minus p-1 minus 2(t-1) to account for the subject effect, period effect, and direct and carryover treatment effects.

### Value

An S3 class designMeanDiffCarryover object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The one-sided significance level.
- numberOfSubjects: The maximum number of subjects.
- meanDiffH0: The mean difference under the null hypothesis.
- meanDiff: The mean difference under the alternative hypothesis.
- stDev: The standard deviation for within-subject random error.
- corr: The intra-subject correlation due to subject random effect.
- design: The crossover design represented by a matrix with rows indexing the sequences, columns indexing the periods, and matrix entries indicating the treatments.
- nseq: The number of sequences.
- nprd: The number of periods.
- ntrt: The number of treatments.
- cumdrop: The cumulative dropout rate over periods.
- V\_direct\_only: The covariance matrix for direct treatment effects without accounting for carryover effects.

- V\_direct\_carry: The covariance matrix for direct and carryover treatment effects.
- v\_direct\_only: The variance of direct treatment effects without accounting for carryover effects.
- v\_direct: The variance of direct treatment effects accounting for carryover effects.
- v\_carry: The variance of carryover treatment effects.
- releff\_direct: The relative efficiency of the design for estimating direct treatment effects after accounting for carryover effects with respect to that without accounting for carryover effects. This is equal to v\_direct\_only/v\_direct.
- releff\_carry: The relative efficiency of the design for estimating carryover effects. This is equal to v\_direct\_only/v\_carry.
- allocationRatioPlanned: Allocation ratio for the sequences.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### References

Robert O. Kuehl. Design of Experiments: Statistical Principles of Research Design and Analysis. Brooks/Cole: Pacific Grove, CA. 2000.

## **Examples**

getDesignMeanDiffEquiv

Group sequential design for equivalence in two-sample mean difference

## **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample mean difference.

# Usage

```
getDesignMeanDiffEquiv(
 beta = NA_real_,
 n = NA_real_,
 meanDiffLower = NA_real_,
 meanDiffUpper = NA_real_,
 meanDiff = 0,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

## **Arguments**

beta The type II error.

n The total sample size.

meanDiffLower The lower equivalence limit of mean difference.

meanDiffUpper The upper equivalence limit of mean difference.

meanDiff The mean difference under the alternative hypothesis.

stDev The standard deviation.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

random

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if

left unspecified.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

#### typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designMeanDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlpha: The attained significance level.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanDiffLower: The lower equivalence limit of mean difference.
  - meanDiffUpper: The upper equivalence limit of mean difference.
  - meanDiff: The mean difference under the alternative hypothesis.
  - stDev: The standard deviation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyMeanDiffLower: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the lower equivalence limit.

- efficacyMeanDiffUpper: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the upper equivalence limit.
- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
     The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiffEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sf0F"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanDiffEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

 $\begin{tabular}{ll} {\it getDesignMeanDiffMMRM} & {\it Group sequential design for two-sample mean difference from the} \\ {\it MMRM model} \end{tabular}$ 

# Description

Obtains the power and sample size for two-sample mean difference at the last time point from the mixed-model for repeated measures (MMRM) model.

# Usage

```
getDesignMeanDiffMMRM(
  beta = NA_real_,
 meanDiffH0 = 0,
 meanDiff = 0.5,
  k = 1,
  t = NA_real_,
  covar1 = diag(k),
  covar2 = NA_real_,
  accrualTime = 0,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0,
  gamma1 = 0,
  gamma2 = 0,
  accrualDuration = NA_real_,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

## **Arguments**

beta	The type II error.
meanDiffH0	The mean difference at the last time point under the null hypothesis. Defaults to 0.
meanDiff	The mean difference at the last time point under the alternative hypothesis.
k	The number of postbaseline time points.
t	The postbaseline time points.
covar1	The covariance matrix for the repeated measures given baseline for the active treatment group.
covar2	The covariance matrix for the repeated measures given baseline for the control group. If missing, it will be set equal to the covariance matrix for the active treatment group.

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

gamma1

The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the active treatment group.

gamma2

The hazard rate for exponential dropout, or a vector of hazard rates for piecewise exponential dropout for the control group.

accrualDuration

Duration of the enrollment period.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The degrees of freedom for the t-distribution is the total effective sample size minus 2. The exact calculation using the t distribution is only implemented for the fixed design.

rounding

Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax

The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha

The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

## parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

## userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designMeanDiffMMRM object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - studyDuration: The maximum study duration.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - expectedStudyDurationH1: The expected study duration under H1.
  - expectedStudyDurationH0: The expected study duration under H0.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up time.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - meanDiffH0: The mean difference under H0.

- meanDiff: The mean difference under H1.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
  - futilityMeanDiff: The futility boundaries on the mean difference scale.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: The allocation ratio for the active treatment versus control.
  - accrualTime: A vector that specifies the starting time of piecewise Poisson enrollment time intervals.
  - accrualIntensity: A vector of accrual intensities. One for each accrual time interval.
  - piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals.
  - gamma1: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
  - gamma2: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the control group.
  - k: The number of postbaseline time points.

- t: The postbaseline time points.
- covar1: The covariance matrix for the repeated measures given baseline for the active treatment group.
- covar2: The covariance matrix for the repeated measures given baseline for the control group.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance
  is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
# function to generate the AR(1) correlation matrix
ar1_cor <- function(n, corr) {</pre>
 exponent \leftarrow abs(matrix((1:n) - 1, n, n, byrow = TRUE) - ((1:n) - 1))
 corr^exponent
}
(design1 = getDesignMeanDiffMMRM(
 beta = 0.2,
 meanDiffH0 = 0,
 meanDiff = 0.5,
 k = 4,
 t = c(1,2,3,4),
 covar1 = ar1\_cor(4, 0.7),
 accrualIntensity = 10,
 gamma1 = 0.02634013,
 gamma2 = 0.02634013,
 accrualDuration = NA,
 allocationRatioPlanned = 1,
 kMax = 3,
 alpha = 0.025,
  typeAlphaSpending = "sfOF"))
```

getDesignMeanDiffXO

Group sequential design for mean difference in 2x2 crossover

## Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean difference in 2x2 crossover.

## Usage

```
getDesignMeanDiffXO(
  beta = NA_real_,
  n = NA\_real\_,
 meanDiffH0 = 0,
 meanDiff = 0.5,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

# **Arguments**

beta The type II error.

n The total sample size.

meanDiffH0 The mean difference under the null hypothesis. Defaults to 0.

meanDiff The mean difference under the alternative hypothesis.

stDev The standard deviation for within-subject random error.

allocationRatioPlanned

Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal

randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

79 getDesignMeanDiffXO

### efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

## futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

#### typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

## parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

## userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designMeanDiffXO object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.

- kMax: The number of stages.
- theta: The parameter value.
- information: The maximum information.
- expectedInformationH1: The expected information under H1.
- expectedInformationH0: The expected information under H0.
- drift: The drift parameter, equal to theta\*sqrt(information).
- inflationFactor: The inflation factor (relative to the fixed design).
- numberOfSubjects: The maximum number of subjects.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- meanDiffH0: The mean difference under the null hypothesis.
- meanDiff: The mean difference under the alternative hypothesis.
- stDev: The standard deviation for within-subject random error.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyMeanDiff: The efficacy boundaries on the mean difference scale.
  - futilityMeanDiff: The futility boundaries on the mean difference scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.

- spendingTime: The error spending time at each analysis.
- allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
(design1 <- getDesignMeanDiffXO(
  beta = 0.2, n = NA, meanDiff = 75, stDev = 150,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

getDesignMeanDiffXOEquiv

Group sequential design for equivalence in mean difference in 2x2 crossover

## **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in mean difference in 2x2 crossover.

## Usage

```
getDesignMeanDiffXOEquiv(
 beta = NA_real_,
 n = NA_real_,
 meanDiffLower = NA_real_,
 meanDiffUpper = NA_real_,
 meanDiff = 0,
  stDev = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### **Arguments**

beta The type II error.

n The total sample size.

meanDiffLower The lower equivalence limit of mean difference.

meanDiffUpper The upper equivalence limit of mean difference.

meanDiff The mean difference under the alternative hypothesis.

stDev The standard deviation for within-subject random error.

allocationRatioPlanned

Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal

randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

## Value

An S3 class designMeanDiffX0Equiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level.
  - kMax: The number of stages.

- information: The maximum information.
- expectedInformationH1: The expected information under H1.
- expectedInformationH0: The expected information under H0.
- numberOfSubjects: The maximum number of subjects.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- meanDiffLower: The lower equivalence limit of mean difference.
- meanDiffUpper: The upper equivalence limit of mean difference.
- meanDiff: The mean difference under the alternative hypothesis.
- stDev: The standard deviation for within-subject random error.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyMeanDiffLower: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyMeanDiffUpper: The efficacy boundaries on the mean difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the t distribution.
    The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanDiffXOEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanDiffXOEquiv(
  beta = 0.1, n = NA, meanDiffLower = -1.3, meanDiffUpper = 1.3,
  meanDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

getDesignMeanRatio

Group sequential design for two-sample mean ratio

## **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean ratio.

### Usage

```
getDesignMeanRatio(
 beta = NA_real_,
 n = NA_real_,
 meanRatioH0 = 1,
 meanRatio = 1.25,
 CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

#### **Arguments**

beta The type II error.

n The total sample size.

meanRatioH0 The mean ratio under the null hypothesis. Defaults to 1.

meanRatio The mean ratio under the alternative hypothesis.

CV The coefficient of variation. The standard deviation on the log scale is equal to

 $sqrt(log(1 + CV^2)).$ 

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if

left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true

if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified

if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds

are non-binding for the calculation of critical values.

### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

### userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designMeanRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanRatioH0: The mean ratio under the null hypothesis.
  - meanRatio: The mean ratio under the alternative hypothesis.
  - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.

- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- numberOfSubjects: The number of subjects.
- efficacyMeanRatio: The efficacy boundaries on the mean ratio scale.
- futilityMeanRatio: The futility boundaries on the mean ratio scale.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

```
(design1 <- getDesignMeanRatio(
  beta = 0.1, n = NA, meanRatio = 1.25, CV = 0.25,
  alpha = 0.05, normalApproximation = FALSE))</pre>
```

```
getDesignMeanRatioEquiv
```

Group sequential design for equivalence in two-sample mean ratio

## **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample mean ratio.

## Usage

```
getDesignMeanRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanRatioLower = NA_real_,
 meanRatioUpper = NA_real_,
 meanRatio = 1,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

## **Arguments**

```
beta The type II error.

n The total sample size.

meanRatioLower The lower equivalence limit of mean ratio.

meanRatioUpper The upper equivalence limit of mean ratio.

meanRatio The mean ratio under the alternative hypothesis.

CV The coefficient of variation.

allocationRatioPlanned
```

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

### Value

An S3 class designMeanRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlpha: The attained significance level.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanRatioLower: The lower equivalence limit of mean ratio.
  - meanRatioUpper: The upper equivalence limit of mean ratio.
  - meanRatio: The mean ratio under the alternative hypothesis.
  - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.

- rejectPerStage: The probability for efficacy stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
- cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- numberOfSubjects: The number of subjects.
- efficacyMeanRatioLower: The efficacy boundaries on the mean ratio scale for the onesided null hypothesis on the lower equivalence limit.
- efficacyMeanRatioUpper: The efficacy boundaries on the mean ratio scale for the onesided null hypothesis on the upper equivalence limit.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the t distribution.
    The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanRatioEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanRatioEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

getDesignMeanRatioXO Group sequential design for mean ratio in 2x2 crossover

# **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample mean ratio in 2x2 crossover.

## Usage

```
getDesignMeanRatioXO(
 beta = NA_real_,
  n = NA\_real\_,
 meanRatioH0 = 1,
 meanRatio = 1.25,
 CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

## **Arguments**

beta The type II error.

n The total sample size.

meanRatioH0 The mean ratio under the null hypothesis. Defaults to 1.

meanRatio The mean ratio under the alternative hypothesis.

CV The coefficient of variation. The standard deviation on the log scale is equal to sqrt(log(1 + CV^2)).

allocationRatioPlanned

Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding

Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax

The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designMeanRatioX0 object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanRatioH0: The mean ratio under the null hypothesis.
  - meanRatio: The mean ratio under the alternative hypothesis.
  - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyMeanRatio: The efficacy boundaries on the mean ratio scale.
  - futilityMeanRatio: The futility boundaries on the mean ratio scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
(design1 <- getDesignMeanRatioX0(
  beta = 0.1, n = NA, meanRatio = 1.25, CV = 0.25,
  alpha = 0.05, normalApproximation = FALSE))</pre>
```

getDesignMeanRatioXOEquiv

Group sequential design for equivalence in mean ratio in 2x2 crossover

# **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence mean ratio in 2x2 crossover.

## Usage

```
getDesignMeanRatioXOEquiv(
  beta = NA_real_,
  n = NA_real_,
  meanRatioLower = NA_real_,
  meanRatioUpper = NA_real_,
  meanRatio = 1,
  CV = 1,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
```

```
kMax = 1L,
informationRates = NA_real_,
alpha = 0.05,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
spendingTime = NA_real_
```

## **Arguments**

beta The type II error.

n The total sample size.

meanRatioLower The lower equivalence limit of mean ratio.

meanRatioUpper The upper equivalence limit of mean ratio.

meanRatio The mean ratio under the alternative hypothesis.

CV The coefficient of variation.

allocationRatioPlanned

Allocation ratio for sequence A/B versus sequence B/A. Defaults to 1 for equal randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designMeanRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanRatioLower: The lower equivalence limit of mean ratio.
  - meanRatioUpper: The upper equivalence limit of mean ratio.
  - meanRatio: The mean ratio under the alternative hypothesis.
  - CV: The coefficient of variation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyMeanRatioLower: The efficacy boundaries on the mean ratio scale for the onesided null hypothesis on the lower equivalence limit.
  - efficacyMeanRatioUpper: The efficacy boundaries on the mean ratio scale for the onesided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameter Alpha Spending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for sequence A/B versus sequence B/A.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the t distribution.
    The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignMeanRatioXOEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignMeanRatioXOEquiv(
  beta = 0.1, n = NA, meanRatioLower = 0.8, meanRatioUpper = 1.25,
  meanRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

getDesignOddsRatio

Group sequential design for two-sample odds ratio

## **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample odds ratio.

## Usage

```
getDesignOddsRatio(
  beta = NA_real_,
  n = NA_real_,
  oddsRatioH0 = 1,
  pi1 = NA_real_,
 pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
```

```
parameterBetaSpending = NA_real_,
userBetaSpending = NA_real_,
spendingTime = NA_real_
)
```

#### **Arguments**

beta The type II error.

n The total sample size.

oddsRatioH0 The odds ratio under the null hypothesis. Defaults to 1. pi1 The assumed probability for the active treatment group.

pi2 The assumed probability for the control group.

nullVariance Whether to use the variance under the null or the empirical variance under the

alternative.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if

left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true

if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true

if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds

are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

### userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designOddsRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - oddsRatioH0: The odds ratio under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.

- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacyOdddsRatio: The efficacy boundaries on the odds ratio scale.
- futilityOddsRatio: The futility boundaries on the odds ratio scale.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
(design1 <- getDesignOddsRatio(
  beta = 0.1, n = NA, pi1 = 0.5, pi2 = 0.3,
  alpha = 0.05))</pre>
```

```
getDesignOddsRatioEquiv
```

Group sequential design for equivalence in two-sample odds ratio

# **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample odds ratio.

# Usage

```
getDesignOddsRatioEquiv(
 beta = NA_real_,
  n = NA_real_,
  oddsRatioLower = NA_real_,
  oddsRatioUpper = NA_real_,
  pi1 = NA_real_,
 pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

## **Arguments**

	beta	The type II error.
	n	The total sample size.
	oddsRatioLower	The lower equivalence limit of odds ratio.
	oddsRatioUpper	The upper equivalence limit of odds ratio.
	pi1	The assumed probability for the active treatment group.
	pi2	The assumed probability for the control group.
	nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned		
		Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
	rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designOddsRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.
  - expectedInformationH20: The expected information under H20.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH10: The expected number of subjects under H10.
  - expectedNumberOfSubjectsH20: The expected number of subjects under H20.
  - oddsRatioLower: The lower equivalence limit of odds ratio.
  - oddsRatioUpper: The upper equivalence limit of odds ratio.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
  - oddsRatio: The odds ratio.

- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - efficacyOddsRatioLower: The efficacy boundaries on the odds ratio scale for the onesided null hypothesis on the lower equivalence limit.
  - efficacyOddsRatioUpper: The efficacy boundaries on the odds ratio scale for the onesided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

#### **Examples**

```
(design1 <- getDesignOddsRatioEquiv(
  beta = 0.2, n = NA, oddsRatioLower = 0.8,
  oddsRatioUpper = 1.25, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))</pre>
```

104 getDesignOneMean

getDesignOneMean

Group sequential design for one-sample mean

## **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample mean.

# Usage

```
getDesignOneMean(
 beta = NA_real_,
 n = NA_real_,
 meanH0 = 0,
 mean = 0.5,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

## **Arguments**

beta The type II error.

n The total sample size.

meanH0 The mean under the null hypothesis. Defaults to 0.

mean The mean under the alternative hypothesis.

stDev The standard deviation.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

getDesignOneMean 105

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

## Value

An S3 class designOneMean object with three components:

106 getDesignOneMean

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - meanH0: The mean under the null hypothesis.
  - mean: The mean under the alternative hypothesis.
  - stDev: The standard deviation.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyMean: The efficacy boundaries on the mean scale.
  - futilityMean: The futility boundaries on the mean scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.

- parameterAlphaSpending: The parameter value for alpha spending.
- userAlphaSpending: The user defined alpha spending.
- typeBetaSpending: The type of beta spending.
- parameterBetaSpending: The parameter value for beta spending.
- userBetaSpending: The user defined beta spending.
- spendingTime: The error spending time at each analysis.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance
  is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignOneMean(
  beta = 0.1, n = NA, meanH0 = 7, mean = 6, stDev = 2.5,
  kMax = 5, alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignOneMean(
  beta = 0.1, n = NA, meanH0 = 7, mean = 6, stDev = 2.5,
  normalApproximation = FALSE, alpha = 0.025))</pre>
```

getDesignOneMultinom Power and sample for one-sample multinomial response

# **Description**

Obtains the power given sample size or obtains the sample size given power for one-sample multinomial response.

# Usage

```
getDesignOneMultinom(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  piH0 = NA_real_,
  pi = NA_real_,
  rounding = TRUE,
  alpha = 0.05
)
```

# **Arguments**

beta	The type II error.
n	The total sample size.
ncats	The number of categories of the multinomial response.
piH0	The prevalence of each category under the null hypothesis. Only need to provide the values for the first ncats-1 categories.
pi	The prevalence of each category. Only need to provide the values for the first ncats-1 categories.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

#### Value

An S3 class designOneMultinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ncats: The number of categories of the multinomial response.
- piH0: The prevalence of each category under the null hypothesis.
- pi: The prevalence of each category.
- effectsize: The effect size for the chi-square test.
- rounding: Whether to round up sample size.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
(design1 <- getDesignOneMultinom(
  beta = 0.1, ncats = 3, piH0 = c(0.25, 0.25),
  pi = c(0.3, 0.4), alpha = 0.05))</pre>
```

```
getDesignOneProportion
```

Group sequential design for one-sample proportion

# **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample proportion.

# Usage

```
getDesignOneProportion(
 beta = NA_real_,
  n = NA_real_,
 piH0 = 0.1,
  pi = 0.2,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
 userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### **Arguments**

beta The type II error.

n The total sample size.

piH0 The response probability under the null hypothesis.

pi The response probability under the alternative hypothesis.

normalApproximation

The type of computation of the p-values. If TRUE, the normal approximation will be used, otherwise the calculations are performed with the binomial distribution. The exact calculation using the binomial distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designOneProportion object with three components:

• overallResults: A data frame containing the following variables:

- overallReject: The overall rejection probability.
- alpha: The overall significance level.
- attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping as well as for the binomial exact test in a fixed design.
- kMax: The number of stages.
- theta: The parameter value.
- information: The maximum information.
- expectedInformationH1: The expected information under H1.
- expectedInformationH0: The expected information under H0.
- drift: The drift parameter, equal to theta\*sqrt(information).
- inflationFactor: The inflation factor (relative to the fixed design).
- numberOfSubjects: The maximum number of subjects.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- piH0: The response probability under the null hypothesis.
- pi: The response probability under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyResponses: The efficacy boundaries on the number of responses scale.
  - futilityResponses: The futility boundaries on the number of responses scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.

- typeBetaSpending: The type of beta spending.
- parameterBetaSpending: The parameter value for beta spending.
- userBetaSpending: The user defined beta spending.
- spendingTime: The error spending time at each analysis.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance
  is assumed to be known, otherwise the calculations are performed with the binomial
  distribution.
- rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignOneProportion(
  beta = 0.2, n = NA, piH0 = 0.15, pi = 0.25,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample binomial exact test
(design2 <- getDesignOneProportion(
  beta = 0.2, n = NA, piH0 = 0.15, pi = 0.25,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

# **Description**

Obtains the power given sample size or obtains the sample size given power for one-sample Poisson rate.

### Usage

```
getDesignOneRateExact(
  beta = NA_real_,
  n = NA_real_,
  lambdaH0 = NA_real_,
  lambda = NA_real_,
  D = 1,
  alpha = 0.025
)
```

## **Arguments**

beta	The type II error.
n	The total sample size.
lambdaH0	The Poisson rate under the null hypothesis.
lambda	The Poisson rate under the alternative hypothesis.
D	The average exposure per subject.
alpha	The one-sided significance level. Defaults to 0.025.

### Value

A data frame containing the following variables:

- alpha: The specified significance level.
- attainedAlpha: The attained type I error of the exact test.
- power: The actual power of the exact test.
- n: The sample size.
- lambdaH0: The Poisson rate under the null hypothesis.
- lambda: The Poisson rate under the alternative hypothesis.
- D: The average exposure per subject.
- r: The critical value of the number of events for rejecting the null hypothesis. Reject H0 if Y >= r for upper-tailed test, and reject H0 if Y <= r for lower-tailed test.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# Examples

```
# Example 1: power calculation
(design1 <- getDesignOneRateExact(
    n = 525, lambdaH0 = 0.049, lambda = 0.012,
    D = 0.5, alpha = 0.025))

# Example 2: sample size calculation
(design2 <- getDesignOneRateExact(
    beta = 0.2, lambdaH0 = 0.2, lambda = 0.3,
    D = 1, alpha = 0.05))</pre>
```

114 getDesignOneSlope

getDesignOneSlope Group sequential design for one-sample slope

# Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for one-sample slope.

# Usage

```
getDesignOneSlope(
 beta = NA_real_,
  n = NA_real_,
  slopeH0 = 0,
  slope = 0.5,
  stDev = 1,
  stDevCovariate = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

#### **Arguments**

beta	The type II error.
n	The total sample size.
slopeH0	The slope under the null hypothesis. Defaults to 0.
slope	The slope under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevCovariate	The standard deviation of the covariate.

getDesignOneSlope 115

#### normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding

Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax

The maximum number of stages.

#### informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

#### efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

# futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha

The significance level. Defaults to 0.025.

### typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

# userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

## userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

### spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

116 getDesignOneSlope

#### Value

An S3 class designOneSlope object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - slopeH0: The slope under the null hypothesis.
  - slope: The slope under the alternative hypothesis.
  - stDev: The standard deviation of the residual.
  - stDevCovariate: The standard deviation of the covariate.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacySlope: The efficacy boundaries on the slope scale.
  - futilitySlope: The futility boundaries on the slope scale.

- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

# Examples

```
(design1 <- getDesignOneSlope(
  beta = 0.1, n = NA, slope = 0.5,
  stDev = 15, stDevCovariate = 9,
  normalApproximation = FALSE,
  alpha = 0.025))</pre>
```

getDesignOrderedBinom Power and sample size for Cochran-Armitage trend test for ordered multi-sample binomial response

# Description

Obtains the power given sample size or obtains the sample size given power for the Cochran-Armitage trend test for ordered multi-sample binomial response.

### Usage

```
getDesignOrderedBinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  pi = NA_real_,
  w = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

# **Arguments**

beta The type II error.

n The total sample size.

ngroups The number of treatment groups.

pi The response probabilities for the treatment groups.

The scores assigned to the treatment groups. This should reflect the ordinal

nature of the treatment groups, e.g. dose levels. Defaults to equally spaced

scores.

allocationRatioPlanned

Allocation ratio for the treatment groups.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

alpha The two-sided significance level. Defaults to 0.05.

#### Value

An S3 class designOrderedBinom object with the following components:

• power: The power to reject the null hypothesis.

• alpha: The two-sided significance level.

• n: The maximum number of subjects.

• ngroups: The number of treatment groups.

• pi: The response probabilities for the treatment groups.

• w: The scores assigned to the treatment groups.

• trendstat: The Cochran-Armitage trend test statistic.

• allocationRatioPlanned: Allocation ratio for the treatment groups.

• rounding: Whether to round up sample size.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### **Examples**

```
(design1 <- getDesignOrderedBinom(
  beta = 0.1, ngroups = 3, pi = c(0.1, 0.25, 0.5), alpha = 0.05))</pre>
```

```
getDesignPairedMeanDiff
```

Group sequential design for paired mean difference

### **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for paired mean difference.

# Usage

```
getDesignPairedMeanDiff(
  beta = NA_real_,
  n = NA_real_,
 pairedDiffH0 = 0,
  pairedDiff = 0.5,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### **Arguments**

```
beta The type II error.

n The total sample size.

pairedDiffH0 The paired difference under the null hypothesis. Defaults to 0.

pairedDiff The paired difference under the alternative hypothesis.

stDev The standard deviation for paired difference.

normalApproximation
```

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

### Value

An S3 class designPairedMeanDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedDiffH0: The paired difference under the null hypothesis.
  - pairedDiff: The paired difference under the alternative hypothesis.
  - stDev: The standard deviation for paired difference.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - ${\mbox{-}}$  cumulative RejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyPairedDiff: The efficacy boundaries on the paired difference scale.
  - futilityPairedDiff: The futility boundaries on the paired difference scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.

- parameterAlphaSpending: The parameter value for alpha spending.
- userAlphaSpending: The user defined alpha spending.
- typeBetaSpending: The type of beta spending.
- parameterBetaSpending: The parameter value for beta spending.
- userBetaSpending: The user defined beta spending.
- spendingTime: The error spending time at each analysis.
- normalApproximation: The type of computation of the p-values. If TRUE, the variance
  is assumed to be known, otherwise the calculations are performed with the t distribution.
- rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanDiff(
  beta = 0.1, n = NA, pairedDiffH0 = 0, pairedDiff = -2, stDev = 5,
  kMax = 5, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignPairedMeanDiff(
  beta = 0.1, n = NA, pairedDiffH0 = 0, pairedDiff = -2, stDev = 5,
  normalApproximation = FALSE, alpha = 0.025))</pre>
```

getDesignPairedMeanDiffEquiv

Group sequential design for equivalence in paired mean difference

# **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in paired mean difference.

# Usage

```
getDesignPairedMeanDiffEquiv(
  beta = NA_real_,
  n = NA_real_,
  pairedDiffLower = NA_real_,
  pairedDiffUpper = NA_real_,
  pairedDiff = 0,
  stDev = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
```

```
kMax = 1L,
informationRates = NA_real_,
alpha = 0.05,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
spendingTime = NA_real_
```

# **Arguments**

beta The type II error.

n The total sample size.

pairedDiffLower

The lower equivalence limit of paired difference.

pairedDiffUpper

The upper equivalence limit of paired difference.

pairedDiff The paired difference under the alternative hypothesis.

stDev The standard deviation for paired difference.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Wh

Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax

The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha

The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designPairedMeanDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlpha: The attained significance level under H0.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedDiffLower: The lower equivalence limit of paired difference.
  - pairedDiffUpper: The upper equivalence limit of paired difference.
  - pairedDiff: The paired difference under the alternative hypothesis.
  - stDev: The standard deviation for paired difference.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlpha: The cumulative probability for efficacy stopping under H0.
  - efficacyPairedDiffLower: The efficacy boundaries on the paired difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyPairedDiffUpper: The efficacy boundaries on the paired difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the t distribution.
    The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanDiffEquiv(
  beta = 0.1, n = NA, pairedDiffLower = -1.3, pairedDiffUpper = 1.3,
  pairedDiff = 0, stDev = 2.2,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignPairedMeanDiffEquiv(
  beta = 0.1, n = NA, pairedDiffLower = -1.3, pairedDiffUpper = 1.3,
  pairedDiff = 0, stDev = 2.2,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

getDesignPairedMeanRatio

Group sequential design for paired mean ratio

# Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for paired mean ratio.

### Usage

```
getDesignPairedMeanRatio(
  beta = NA_real_,
  n = NA_real_,
  pairedRatioH0 = 1,
  pairedRatio = 1.2,
  CV = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
```

```
parameterBetaSpending = NA_real_,
userBetaSpending = NA_real_,
spendingTime = NA_real_
)
```

#### **Arguments**

beta The type II error.

n The total sample size.

pairedRatioH0 The paired ratio under the null hypothesis.

pairedRatio The paired ratio under the alternative hypothesis.

CV The coefficient of variation for paired ratio.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds

are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

### userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designPairedMeanRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedRatioH0: The paired ratio under the null hypothesis.
  - pairedRatio: The paired ratio under the alternative hypothesis.
  - CV: The coefficient of variation for paired ratio.
- by StageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.

- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- numberOfSubjects: The number of subjects.
- efficacyPairedRatio: The efficacy boundaries on the paired ratio scale.
- futilityPairedRatio: The futility boundaries on the paired ratio scale.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanRatio(
  beta = 0.1, n = NA, pairedRatio = 1.2, CV = 0.35,
  kMax = 5, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for one-sample t-test
(design2 <- getDesignPairedMeanRatio(
  beta = 0.1, n = NA, pairedRatio = 1.2, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

```
getDesignPairedMeanRatioEquiv
```

Group sequential design for equivalence in paired mean ratio

# Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in paired mean ratio.

# Usage

```
getDesignPairedMeanRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  pairedRatioLower = NA_real_,
  pairedRatioUpper = NA_real_,
  pairedRatio = 1,
  CV = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### **Arguments**

normalApproximation

beta The type II error.

n The total sample size.

pairedRatioLower
The lower equivalence limit of paired ratio.

pairedRatioUpper
The upper equivalence limit of paired ratio.

pairedRatio The paired ratio under the alternative hypothesis.

CV The coefficient of variation for paired ratio.

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

alpha

The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designPairedMeanRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlpha: The attained significance level under H0.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pairedRatioLower: The lower equivalence limit of paired ratio.
  - pairedRatioUpper: The upper equivalence limit of paired ratio.
  - pairedRatio: The paired ratio under the alternative hypothesis.
  - CV: The coefficient of variation for paired ratios.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.

- cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
- cumulativeAttainedAlpha: The cumulative alpha attained under H0.
- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- numberOfSubjects: The number of subjects.
- efficacyPairedRatioLower: The efficacy boundaries on the paired ratio scale for the one-sided null hypothesis on the lower equivalence limit.
- efficacyPairedRatioUpper: The efficacy boundaries on the paired ratio scale for the one-sided null hypothesis on the upper equivalence limit.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the t distribution.
    The exact calculation using the t distribution is only implemented for the fixed design.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

#### **Examples**

```
# Example 1: group sequential trial power calculation
(design1 <- getDesignPairedMeanRatioEquiv(
  beta = 0.1, n = NA, pairedRatioLower = 0.8, pairedRatioUpper = 1.25,
  pairedRatio = 1, CV = 0.35,
  kMax = 4, alpha = 0.05, typeAlphaSpending = "sfOF"))

# Example 2: sample size calculation for t-test
(design2 <- getDesignPairedMeanRatioEquiv(
  beta = 0.1, n = NA, pairedRatioLower = 0.8, pairedRatioUpper = 1.25,
  pairedRatio = 1, CV = 0.35,
  normalApproximation = FALSE, alpha = 0.05))</pre>
```

 ${\tt getDesignPairedPropMcNemar}$ 

Group sequential design for McNemar's test for paired proportions

### **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for McNemar's test for paired proportions.

## Usage

```
getDesignPairedPropMcNemar(
  beta = NA_real_,
  n = NA_real_,
 pDiscordant = NA_real_,
  riskDiff = NA_real_,
  nullVariance = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

# **Arguments**

beta The type II error.

n The total sample size.

pDiscordant The proportion of discordant pairs (xi = pi01 + pi10).

riskDiff The risk difference between the active and control treatments (delta = pi t - pi c

= pi01 - pi10)

nullVariance Whether to use the variance under the null or the variance under the alternative.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if

left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true

if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true

if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

#### typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

# parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

# typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

#### userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

### Value

An S3 class designPairedPropMcNemar object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.

- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- pDiscordant: The proportion of discordant pairs (xi = pi01 + pi10).
- riskDiff: The risk difference between the active and control treatments (delta = pi\_t pi\_c = pi01 pi10)
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - ${\sf -}$  cumulative Rejection H0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyRiskDiff: The efficacy boundaries on the risk difference scale.
  - futilityRiskDiff: The futility boundaries on the risk difference scale.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
# Example 1: fixed design
(design1 <- getDesignPairedPropMcNemar(
  beta = 0.1, n = NA, pDiscordant = 0.16, riskDiff = 0.1,
  alpha = 0.025))

# Example 2: group sequential design
(design2 <- getDesignPairedPropMcNemar(
  beta = 0.1, n = NA, pDiscordant = 0.16, riskDiff = 0.1,
  alpha = 0.025, kMax = 3, typeAlphaSpending = "sf0F"))</pre>
```

getDesignRepeatedANOVA

Power and sample size for repeated-measures ANOVA

# Description

Obtains the power and sample size for one-way repeated measures analysis of variance. Each subject takes all treatments in the longitudinal study.

### Usage

```
getDesignRepeatedANOVA(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  corr = 0,
  rounding = TRUE,
  alpha = 0.05
)
```

# Arguments

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The total standard deviation.
corr	The correlation among the repeated measures.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

#### **Details**

Let  $y_{ij}$  denote the measurement under treatment condition  $j(j=1,\ldots,k)$  for subject  $i(i=1,\ldots,n)$ . Then

$$y_{ij} = \alpha + \beta_j + b_i + e_{ij},$$

where  $b_i$  denotes the subject random effect,  $b_i \sim N(0, \sigma_b^2)$ , and  $e_{ij} \sim N(0, \sigma_e^2)$  denotes the withinsubject residual. If we set  $\beta_k = 0$ , then  $\alpha$  is the mean of the last treatment (control), and  $\beta_j$  is the difference in means between the jth treatment and the control for  $j = 1, \ldots, k-1$ .

The repeated measures have a compound symmetry covariance structure. Let  $\sigma^2 = \sigma_b^2 + \sigma_e^2$ , and  $\rho = \frac{\sigma_b^2}{\sigma_b^2 + \sigma_e^2}$ . Then  $Var(y_i) = \sigma^2 \{ (1 - \rho)I_k + \rho 1_k 1_k^T \}$ . Let  $X_i$  denote the design matrix for subject i. Let  $\theta = (\alpha, \beta_1, \dots, \beta_{k-1})^T$ . It follows that

$$Var(\hat{\theta}) = \left(\sum_{i=1}^{n} X_i^T V_i^{-1} X_i\right)^{-1}.$$

It can be shown that

$$Var(\hat{\beta}) = \frac{\sigma^2(1-\rho)}{n}(I_{k-1} + 1_{k-1}1_{k-1}^T).$$

It follows that  $\hat{\beta}^T \hat{V}_{\hat{\beta}}^{-1} \hat{\beta} \sim F_{k-1,(n-1)(k-1),\lambda}$ , where the noncentrality parameter for the F distribution is

$$\lambda = \beta^T V_{\hat{\beta}}^{-1} \beta = \frac{n \sum_{j=1}^k (\mu_j - \bar{\mu})^2}{\sigma^2 (1 - \rho)}.$$

#### Value

An S3 class designRepeatedANOVA object with the following components:

- power: The power to reject the null hypothesis that there is no difference among the treatment groups.
- alpha: The two-sided significance level.
- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The total standard deviation.
- corr: The correlation among the repeated measures.
- effectsize: The effect size.
- rounding: Whether to round up sample size.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
(design1 <- getDesignRepeatedANOVA(
  beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
  stDev = 5, corr = 0.2, alpha = 0.05))</pre>
```

```
{\tt getDesignRepeatedANOVAContrast}
```

Power and sample size for one-way repeated measures ANOVA contrast

# Description

Obtains the power and sample size for a single contrast in one-way repeated measures analysis of variance.

# Usage

```
getDesignRepeatedANOVAContrast(
  beta = NA_real_,
  n = NA_real_,
  ngroups = 2,
  means = NA_real_,
  stDev = 1,
  corr = 0,
  contrast = NA_real_,
  meanContrastH0 = 0,
  rounding = TRUE,
  alpha = 0.025
)
```

# **Arguments**

beta	The type II error.
n	The total sample size.
ngroups	The number of treatment groups.
means	The treatment group means.
stDev	The total standard deviation.
corr	The correlation among the repeated measures.
contrast	The coefficients for the single contrast.
${\it mean Contrast H0}$	The mean of the contrast under the null hypothesis.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The one-sided significance level. Defaults to 0.025.

# Value

An S3 class designRepeatedANOVAContrast object with the following components:

- power: The power to reject the null hypothesis for the treatment contrast.
- alpha: The one-sided significance level.

- n: The number of subjects.
- ngroups: The number of treatment groups.
- means: The treatment group means.
- stDev: The total standard deviation.
- corr: The correlation among the repeated measures.
- contrast: The coefficients for the single contrast.
- meanContrastH0: The mean of the contrast under the null hypothesis.
- meanContrast: The mean of the contrast under the alternative hypothesis.
- effectsize: The effect size.
- rounding: Whether to round up sample size.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
(design1 <- getDesignRepeatedANOVAContrast(
beta = 0.1, ngroups = 4, means = c(1.5, 2.5, 2, 0),
stDev = 5, corr = 0.2, contrast = c(1, 1, 1, -3)/3,
alpha = 0.025))
```

getDesignRiskDiff

Group sequential design for two-sample risk difference

# **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk difference.

# Usage

```
getDesignRiskDiff(
  beta = NA_real_,
  n = NA_real_,
  riskDiffH0 = 0,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
```

```
futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
```

### **Arguments**

beta The type II error.

n The total sample size.

riskDiffH0 The risk difference under the null hypothesis. Defaults to 0.

pi1 The assumed probability for the active treatment group.

pi2 The assumed probability for the control group.

nullVariance Whether to use the variance under the null or the empirical variance under the

alternative.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if

left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true

if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true

if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

### Value

An S3 class designRiskDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - riskDiffH0: The risk difference under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:

- informationRates: The information rates.
- efficacyBounds: The efficacy boundaries on the Z-scale.
- futilityBounds: The futility boundaries on the Z-scale.
- rejectPerStage: The probability for efficacy stopping.
- futilityPerStage: The probability for futility stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeFutility: The cumulative probability for futility stopping.
- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyRiskDiff: The efficacy boundaries on the risk difference scale.
- futilityRiskDiff: The futility boundaries on the risk difference scale.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
(design1 <- getDesignRiskDiff(
  beta = 0.2, n = NA, pi1 = 0.1, pi2 = 0.15,
  kMax = 3, alpha = 0.025, typeAlphaSpending = "sfOF",
  nullVariance = 0))</pre>
```

```
getDesignRiskDiffEquiv
```

Group sequential design for equivalence in two-sample risk difference

# **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample risk difference.

# Usage

```
getDesignRiskDiffEquiv(
 beta = NA_real_,
 n = NA_real_,
  riskDiffLower = NA_real_,
  riskDiffUpper = NA_real_,
 pi1 = NA_real_,
 pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  spendingTime = NA_real_
)
```

### **Arguments**

	beta	The type II error.
	n	The total sample size.
	riskDiffLower	The lower equivalence limit of risk difference.
	riskDiffUpper	The upper equivalence limit of risk difference.
	pi1	The assumed probability for the active treatment group.
	pi2	The assumed probability for the control group.
	nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.
allocationRatioPlanned		
		Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
	rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designRiskDiffEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.
  - expectedInformationH20: The expected information under H20.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH10: The expected number of subjects under H10.
  - expectedNumberOfSubjectsH20: The expected number of subjects under H20.
  - riskDiffLower: The lower equivalence limit of risk difference.
  - riskDiffUpper: The upper equivalence limit of risk difference.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
  - riskDiff: The risk difference.

- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - efficacyRiskDiffLower: The efficacy boundaries on the risk difference scale for the one-sided null hypothesis on the lower equivalence limit.
  - efficacyRiskDiffUpper: The efficacy boundaries on the risk difference scale for the one-sided null hypothesis on the upper equivalence limit.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - spendingTime: The error spending time at each analysis.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
(design1 <- getDesignRiskDiffEquiv(
  beta = 0.2, n = NA, riskDiffLower = -0.1,
  riskDiffUpper = 0.1, pi1 = 0.12, pi2 = 0.12,
  nullVariance = 1,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))</pre>
```

```
getDesignRiskDiffExact
```

Power and sample size for exact unconditional test for risk difference

#### **Description**

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of risk difference.

# Usage

```
getDesignRiskDiffExact(
  beta = NA_real_,
  n = NA_real_,
  riskDiffH0 = 0,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.025
)
```

#### **Arguments**

```
beta The type II error.

n The total sample size.

riskDiffH0 The risk difference under the null hypothesis. Defaults to 0.

pi1 The assumed probability for the active treatment group.

pi2 The assumed probability for the control group.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

alpha The one-sided significance level. Defaults to 0.025.
```

## Value

A data frame with the following variables:

- alpha: The specified one-sided significance level.
- attainedAlpha: The attained one-sided significance level.
- power: The power.
- n: The sample size.
- riskDiffH0: The risk difference under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.

- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskDiffBound: The critical value on the scale of score test statistic for risk difference.
- pi2star: The response probability in the control group at which the critical value of the test statistic is attained.

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
getDesignRiskDiffExactEquiv
```

Power and sample size for exact unconditional test for equivalence in risk difference

### **Description**

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of equivalence in risk difference.

```
getDesignRiskDiffExactEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskDiffLower = NA_real_,
  riskDiffUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

#### **Arguments**

beta The type II error. The total sample size. riskDiffLower The lower equivalence limit of risk difference. riskDiffUpper The upper equivalence limit of risk difference. pi1 The assumed probability for the active treatment group. pi2 The assumed probability for the control group. allocationRatioPlanned Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization. alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

#### Value

A data frame with the following variables:

- alpha: The specified significance level for each of the two one-sided tests.
- attainedAlpha: The attained significance level.
- power: The power.
- n: The sample size.
- riskDiffLower: The lower equivalence limit of risk difference.
- riskDiffUpper: The upper equivalence limit of risk difference.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- riskDiff: The risk difference.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskDiffLower: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the lower equivalence limit.
- zstatRiskDiffUpper: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the upper equivalence limit.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
getDesignRiskDiffExactEquiv(
  n = 200, riskDiffLower = -0.2, riskDiffUpper = 0.2,
  pi1 = 0.775, pi2 = 0.775, alpha = 0.05)
```

148 getDesignRiskRatio

getDesignRiskRatio Group sequential design for two-sample risk ratio

### **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk ratio.

# Usage

```
getDesignRiskRatio(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

# Arguments

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
nullVariance	Whether to use the variance under the null or the empirical variance under the alternative.

149 getDesignRiskRatio

#### allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

Whether to round up sample size. Defaults to 1 for sample size rounding. rounding

kMax The maximum number of stages.

#### informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

### efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

#### futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

The significance level. Defaults to 0.025. alpha

#### typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

# userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

# typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

#### userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

#### spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

150 getDesignRiskRatio

#### Value

An S3 class designRiskRatio object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - riskRatioH0: The risk ratio under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - ${\mathord{\hspace{1pt}\text{--}}}$  futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyRiskRatio: The efficacy boundaries on the risk ratio scale.
  - futilityRiskRatio: The futility boundaries on the risk ratio scale.
  - numberOfSubjects: The number of subjects.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### **Examples**

```
(design1 <- getDesignRiskRatio(
  beta = 0.1, n = NA, pi1 = 0.5, pi2 = 0.3,
  alpha = 0.05))</pre>
```

getDesignRiskRatioEquiv

Group sequential design for equivalence in two-sample risk ratio

# Description

Obtains the power given sample size or obtains the sample size given power for a group sequential design for equivalence in two-sample risk ratio.

```
getDesignRiskRatioEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskRatioLower = NA_real_,
  riskRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = FALSE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
```

```
kMax = 1L,
informationRates = NA_real_,
criticalValues = NA_real_,
alpha = 0.05,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
spendingTime = NA_real_
```

#### **Arguments**

beta The type II error.

n The total sample size.

riskRatioLower The lower equivalence limit of risk ratio. riskRatioUpper The upper equivalence limit of risk ratio.

pi1 The assumed probability for the active treatment group.

pi2 The assumed probability for the control group.

nullVariance Whether to use the variance under the null or the empirical variance under the

alternative.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if

left unspecified.

critical Values Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

#### Value

An S3 class designRiskRatioEquiv object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The significance level for each of the two one-sided tests. Defaults to 0.05.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - kMax: The number of stages.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH10: The expected information under H10.
  - expectedInformationH20: The expected information under H20.
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH10: The expected number of subjects under H10.
  - expectedNumberOfSubjectsH20: The expected number of subjects under H20.
  - riskRatioLower: The lower equivalence limit of risk ratio.
  - riskRatioUpper: The upper equivalence limit of risk ratio.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
  - riskRatio: The risk ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - efficacyRiskRatioLower: The efficacy boundaries on the risk ratio scale for the onesided null hypothesis on the lower equivalence limit.
  - efficacyRiskRatioUpper: The efficacy boundaries on the risk ratio scale for the onesided null hypothesis on the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
  - numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.

- spendingTime: The error spending time at each analysis.
- nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
- varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
- varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
- varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
- varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
(design1 <- getDesignRiskRatioEquiv(
  beta = 0.2, n = NA, riskRatioLower = 0.8,
  riskRatioUpper = 1.25, pi1 = 0.12, pi2 = 0.12,
  kMax = 3, alpha = 0.05, typeAlphaSpending = "sfOF"))</pre>
```

getDesignRiskRatioExact

Power and sample size for exact unconditional test for risk ratio

# Description

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of risk ratio.

```
getDesignRiskRatioExact(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.025
)
```

#### **Arguments**

beta	The type II error.
n	The total sample size.
riskRatioH0	The risk ratio under the null hypothesis. Defaults to 0.
pi1	The assumed probability for the active treatment group.
pi2	The assumed probability for the control group.
allocationRatioPlanned	
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
alpha	The one-sided significance level. Defaults to 0.025.

#### Value

A data frame with the following variables:

- alpha: The specified one-sided significance level.
- attainedAlpha: The attained one-sided significance level.
- power: The power.
- n: The sample size.
- riskRatioH0: The risk ratio under the null hypothesis.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskRatioBound: The critical value on the scale of score test statistic for risk ratio.
- pi2star: The response probability in the control group at which the critical value of the test statistic is attained.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
getDesignRiskRatioExactEquiv
```

Power and sample size for exact unconditional test for equivalence in risk ratio

# **Description**

Obtains the power given sample size or obtains the sample size given power for exact unconditional test of equivalence in risk ratio.

## Usage

```
getDesignRiskRatioExactEquiv(
  beta = NA_real_,
  n = NA_real_,
  riskRatioLower = NA_real_,
  riskRatioUpper = NA_real_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  alpha = 0.05
)
```

#### **Arguments**

```
beta The type II error.

n The total sample size.

riskRatioLower The lower equivalence limit of risk ratio.

riskRatioUpper The upper equivalence limit of risk ratio.

pi1 The assumed probability for the active treatment group.

pi2 The assumed probability for the control group.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.
```

#### Value

A data frame with the following variables:

- alpha: The specified significance level for each of the two one-sided tests.
- attainedAlpha: The attained significance level.
- power: The power.
- n: The sample size.

- riskRatioLower: The lower equivalence limit of risk ratio.
- riskRatioUpper: The upper equivalence limit of risk ratio.
- pi1: The assumed probability for the active treatment group.
- pi2: The assumed probability for the control group.
- riskRatio: The risk ratio.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- zstatRiskRatioLower: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the lower equivalence limit.
- zstatRiskRatioUpper: The efficacy boundaries on the z-test statistic scale for the one-sided null hypothesis on the upper equivalence limit.

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
getDesignRiskRatioExactEquiv(
  n = 200, riskRatioLower = 0.8, riskRatioUpper = 1.25,
  pi1 = 0.775, pi2 = 0.775, alpha = 0.05)
```

getDesignRiskRatioFM

Group sequential design for two-sample risk ratio based on the Farrington-Manning score test

#### **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample risk ratio based on the Farrington-Manning score test

```
getDesignRiskRatioFM(
  beta = NA_real_,
  n = NA_real_,
  riskRatioH0 = 1,
  pi1 = NA_real_,
  pi2 = NA_real_,
  nullVariance = TRUE,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
```

```
criticalValues = NA_real_,
alpha = 0.025,
typeAlphaSpending = "sfOF",
parameterAlphaSpending = NA_real_,
userAlphaSpending = NA_real_,
futilityBounds = NA_real_,
typeBetaSpending = "none",
parameterBetaSpending = NA_real_,
userBetaSpending = NA_real_,
spendingTime = NA_real_
```

#### **Arguments**

beta The type II error.

n The total sample size.

riskRatioH0 The risk ratio under the null hypothesis. Defaults to 1.

pi1 The assumed probability for the active treatment group.

pi2 The assumed probability for the control group.

nullVariance Whether to use the variance under the null or the empirical variance under the

alternative.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if

left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true

if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true

if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

#### userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designRiskRatioFM object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - riskRatioH0: The risk ratio under the null hypothesis.
  - pi1: The assumed probability for the active treatment group.
  - pi2: The assumed probability for the control group.
- byStageResults: A data frame containing the following variables:

- informationRates: The information rates.
- efficacyBounds: The efficacy boundaries on the Z-scale.
- futilityBounds: The futility boundaries on the Z-scale.
- rejectPerStage: The probability for efficacy stopping.
- futilityPerStage: The probability for futility stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeFutility: The cumulative probability for futility stopping.
- cumulativeAlphaSpent: The cumulative alpha spent.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- rejectPerStageH0: The probability for efficacy stopping under H0.
- futilityPerStageH0: The probability for futility stopping under H0.
- cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacyRiskRatioScore: The efficacy boundaries on the score test pi1 riskRatioH0\*pi2 score.
- futilityRiskRatioScore: The futility boundaries on the score test pi1 riskRatioH0\*pi2 scale.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - varianceRatio: The ratio of the variance under H0 to the variance under H1.
  - nullVariance: Whether to use the variance under the null or the empirical variance under the alternative.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

#### **Examples**

```
(design1 <- getDesignRiskRatioFM(
  beta = 0.2, riskRatioH0 = 1.3, pi1 = 0.125, pi2 = 0.125,
  alpha = 0.05))</pre>
```

getDesignSlopeDiff 161

getDesignSlopeDiff Group sequential design for two-sample slope difference

### **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample slope difference.

# Usage

```
getDesignSlopeDiff(
 beta = NA_real_,
  n = NA_real_,
  slopeDiffH0 = 0,
  slopeDiff = 0.5,
  stDev = 1,
 stDevCovariate = 1,
 allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
 kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

#### **Arguments**

beta	The type II error.
n	The total sample size.
slopeDiffH0	The slope difference under the null hypothesis. Defaults to 0.
slopeDiff	The slope difference under the alternative hypothesis.
stDev	The standard deviation of the residual.
stDevCovariate	The standard deviation of the covariate.

162 getDesignSlopeDiff

#### allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

#### normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The exact calculation using the t distribution is only implemented for the fixed design.

rounding

Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax

The maximum number of stages.

#### informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

# efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

#### futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha

The significance level. Defaults to 0.025.

#### typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

# parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

#### userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

getDesignSlopeDiff 163

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### Value

An S3 class designSlopeDiff object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - slopeDiffH0: The slope difference under the null hypothesis.
  - slopeDiff: The slope difference under the alternative hypothesis.
  - stDev: The standard deviation of the residual.
  - stDevCovariate: The standard deviation of the covariate.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.

- cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
- efficacySlopeDiff: The efficacy boundaries on the slope difference scale.
- futilitySlopeDiff: The futility boundaries on the slope difference scale.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance
    is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
(design1 <- getDesignSlopeDiff(
  beta = 0.1, n = NA, slopeDiff = -0.5,
  stDev = 10, stDevCovariate = 6,
  normalApproximation = FALSE, alpha = 0.025))</pre>
```

getDesignSlopeDiffMMRM

Group sequential design for two-sample slope difference from the MMRM model

# Description

Obtains the power given sample size or obtains the sample size given power for two-sample slope difference from the growth curve MMRM model.

```
getDesignSlopeDiffMMRM(
  beta = NA_real_,
  slopeDiffH0 = 0,
  slopeDiff = 0.5,
```

```
stDev = 1,
  stDevIntercept = 1,
  stDevSlope = 1,
  corrInterceptSlope = 0.5,
 w = NA_real_,
 N = NA_{real}
  accrualTime = 0,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0,
  gamma1 = 0,
  gamma2 = 0,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  allocationRatioPlanned = 1,
  normalApproximation = TRUE,
  rounding = TRUE,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

# **Arguments** beta

The type II error. The slope difference under the null hypothesis. Defaults to 0. slopeDiffH0 The slope difference under the alternative hypothesis. slopeDiff stDev The standard deviation of the residual. stDevIntercept The standard deviation of the random intercept. stDevSlope The standard deviation of the random slope. corrInterceptSlope The correlation between the random intercept and random slope. The number of time units per measurement visit in a period. W The number of measurement visits in a period. accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

gamma1 The hazard rate for exponential dropout, or a vector of hazard rates for piecewise

exponential dropout for the active treatment group.

gamma2 The hazard rate for exponential dropout, or a vector of hazard rates for piecewise

exponential dropout for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

normalApproximation

The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution. The degrees of freedom for the t-distribution for testing the slope difference is calculated using the containment method, and is equal to the total number of observations minus two times the total number of subjects. The exact calculation using the t distribution is only implemented for the fixed design.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime

A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

#### **Details**

We use the following random-effects model to compare two slopes:

$$y_{ij} = \alpha + (\beta + \gamma x_i)t_j + a_i + b_i t_j + e_{ij},$$

where

- $\alpha$ : overall intercept common across treatment groups due to randomization
- $\beta$ : slope for the control group
- $\gamma$ : difference in slopes between the active treatment and control groups
- $x_i$ : treatment indicator for subject i, 1 for the active treatment and 0 for the control
- $t_i$ : time point j for repeated measurements,  $t_1 = 0 < t_2 < \ldots < t_k$
- $(a_i, b_i)$ : random intercept and random slope for subject i,  $Var(a_i) = \sigma_a^2$ ,  $Var(b_i) = \sigma_b^2$ ,  $Corr(a_i, b_i) = \rho$
- $e_{ij}$ : within-subject residual with variance  $\sigma_e^2$

By accounting for randomization, we improve the efficiency for estimating the difference in slopes. We also allow for non-equal spacing of the time points and missing data due to dropouts.

#### Value

An S3 class designSlopeDiffMMRM object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.

- attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping.
- kMax: The number of stages.
- theta: The parameter value.
- information: The maximum information.
- expectedInformationH1: The expected information under H1.
- expectedInformationH0: The expected information under H0.
- drift: The drift parameter, equal to theta\*sqrt(information).
- inflationFactor: The inflation factor (relative to the fixed design).
- numberOfSubjects: The maximum number of subjects.
- studyDuration: The maximum study duration.
- expectedNumberOfSubjectsH1: The expected number of subjects under H1.
- expectedNumberOfSubjectsH0: The expected number of subjects under H0.
- expectedStudyDurationH1: The expected study duration under H1.
- expectedStudyDurationH0: The expected study duration under H0.
- accrualDuration: The accrual duration.
- followupTime: The follow-up time.
- fixedFollowup: Whether a fixed follow-up design is used.
- slopeDiffH0: The slope difference under H0.
- slopeDiff: The slope difference under H1.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacySlopeDiff: The efficacy boundaries on the slope difference scale.
  - futilitySlopeDiff: The futility boundaries on the slope difference scale.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.

- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameter Alpha Spending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: The allocation ratio for the active treatment versus control.
  - accrualTime: A vector that specifies the starting time of piecewise Poisson enrollment time intervals.
  - accrualIntensity: A vector of accrual intensities. One for each accrual time interval.
  - piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals.
  - gamma1: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the active treatment group.
  - gamma2: The hazard rate for exponential dropout or a vector of hazard rates for piecewise exponential dropout for the control group.
  - w: The number of time units per measurement visit in a period.
  - N: The number of measurement visits in a period.
  - stdDev: The standard deviation of the residual.
  - G: The covariance matrix for the random intercept and random slope.
  - normalApproximation: The type of computation of the p-values. If TRUE, the variance is assumed to be known, otherwise the calculations are performed with the t distribution.
  - rounding: Whether to round up sample size.

Kaifeng Lu, <kaifenglu@gmail.com>

#### References

Daniel O. Scharfstein, Anastasios A. Tsiatis, and James M. Robins. Semiparametric efficiency and its implication on the design and analysis of group-sequential studies. Journal of the American Statistical Association 1997; 92:1342-1350.

# **Examples**

```
(design1 <- getDesignSlopeDiffMMRM(
  beta = 0.2, slopeDiff = log(1.15)/52,
  stDev = sqrt(.182),
  stDevIntercept = sqrt(.238960),
  stDevSlope = sqrt(.000057),
  corrInterceptSlope = .003688/sqrt(.238960*.000057),
  w = 8,
  N = 10000,
  accrualIntensity = 15,</pre>
```

```
gamma1 = 1/(4.48*52),
gamma2 = 1/(4.48*52),
accrualDuration = NA,
followupTime = 8,
alpha = 0.025))
```

getDesignTwoMultinom

Power and sample for difference in two-sample multinomial responses

# Description

Obtains the power given sample size or obtains the sample size given power for difference in two-sample multinomial responses.

# Usage

```
getDesignTwoMultinom(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

# Arguments

	beta	The type II error.
	n	The total sample size.
	ncats	The number of categories of the multinomial response.
	pi1	The prevalence of each category for the treatment group. Only need to specify the valued for the first ncats-1 categories.
	pi2	The prevalence of each category for the control group. Only need to specify the valued for the first ncats-1 categories.
allocationRatioPlanned		
		Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.
	rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
	alpha	The two-sided significance level. Defaults to 0.05.

getDesignTwoOrdinal 171

#### Value

An S3 class designTwoMultinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ncats: The number of categories of the multinomial response.
- pi1: The prevalence of each category for the treatment group.
- pi2: The prevalence of each category for the control group.
- effectsize: The effect size for the chi-square test.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- rounding: Whether to round up sample size.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
(design1 <- getDesignTwoMultinom(
  beta = 0.1, ncats = 3, pi1 = c(0.3, 0.35),
  pi2 = c(0.2, 0.3), alpha = 0.05))</pre>
```

getDesignTwoOrdinal

Power and sample size for the Wilcoxon test for two-sample ordinal response

# Description

Obtains the power given sample size or obtains the sample size given power for the Wilcoxon test for two-sample ordinal response.

```
getDesignTwoOrdinal(
  beta = NA_real_,
  n = NA_real_,
  ncats = NA_integer_,
  pi1 = NA_real_,
  pi2 = NA_real_,
  allocationRatioPlanned = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

172 getDesignTwoOrdinal

## **Arguments**

beta	The type II error.	
n	The total sample size.	
ncats	The number of categories of the ordinal response.	
pi1	The prevalence of each category for the treatment group. Only need to specify the valued for the first ncats-1 categories.	
pi2	The prevalence of each category for the control group. Only need to specify the valued for the first ncats-1 categories.	
allocationRatioPlanned		
	Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.	
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.	
alpha	The significance level. Defaults to 0.025.	

#### Value

An S3 class designTwoOrdinal object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ncats: The number of categories of the ordinal response.
- pi1: The prevalence of each category for the treatment group.
- pi2: The prevalence of each category for the control group.
- meanscore1: The mean midrank score for the treatment group.
- meanscore2: The mean midrank score for the control group.
- allocationRatioPlanned: Allocation ratio for the active treatment versus control.
- rounding: Whether to round up sample size.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
(design1 <- getDesignTwoOrdinal(
  beta = 0.1, ncats = 4, pi1 = c(0.55, 0.3, 0.1),
  pi2 = c(0.214, 0.344, 0.251), alpha = 0.025))</pre>
```

getDesignTwoWayANOVA Power and sample size for two-way ANOVA

# **Description**

Obtains the power and sample size for two-way analysis of variance.

# Usage

```
getDesignTwoWayANOVA(
  beta = NA_real_,
  n = NA_real_,
  nlevelsA = 2,
  nlevelsB = 2,
  means = NA_real_,
  stDev = 1,
  rounding = TRUE,
  alpha = 0.05
)
```

# **Arguments**

beta	The type II error.
n	The total sample size.
nlevelsA	The number of groups for Factor A.
nlevelsB	The number of levels for Factor B.
means	The matrix of treatment means for Factors A and B combination.
stDev	The common standard deviation.
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.
alpha	The two-sided significance level. Defaults to 0.05.

#### Value

An S3 class designTwoWayANOVA object with the following components:

- alpha: The two-sided significance level.
- nlevelsA: The number of levels for Factor A.
- nlevelsB: The number of levels for Factor B.
- means: The matrix of treatment group means.
- stDev: The common standard deviation.
- effectsizeA: The effect size for Factor A.
- effectsizeB: The effect size for Factor B.
- effectsizeAB: The effect size for Factor A and Factor B interaction.

- rounding: Whether to round up sample size.
- powerdf: The data frame containing the power and sample size results. It has the following variables:
  - n: The sample size.
  - powerA: The power to reject the null hypothesis that there is no difference among Factor A levels.
  - powerB: The power to reject the null hypothesis that there is no difference among Factor B levels.
  - powerAB: The power to reject the null hypothesis that there is no interaction between Factor A and Factor B.

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
(design1 <- getDesignTwoWayANOVA(
  beta = 0.1, nlevelsA = 2, nlevelsB = 2,
  means = matrix(c(0.5, 4.7, 0.4, 6.9), 2, 2, byrow = TRUE),
  stDev = 2, alpha = 0.05))</pre>
```

getDesignUnorderedBinom

Power and sample size for unordered multi-sample binomial response

#### **Description**

Obtains the power given sample size or obtains the sample size given power for the chi-square test for unordered multi-sample binomial response.

```
getDesignUnorderedBinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  pi = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

## **Arguments**

beta The type II error.

n The total sample size.

ngroups The number of treatment groups.

pi The response probabilities for the treatment groups.

allocationRatioPlanned

Allocation ratio for the treatment groups.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

alpha The two-sided significance level. Defaults to 0.05.

#### Value

An S3 class designUnorderedBinom object with the following components:

• power: The power to reject the null hypothesis.

- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ngroups: The number of treatment groups.
- pi: The response probabilities for the treatment groups.
- effectsize: The effect size for the chi-square test.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### **Examples**

```
(design1 <- getDesignUnorderedBinom( beta = 0.1, ngroups = 3, pi = c(0.1, 0.25, 0.5), alpha = 0.05))
```

getDesignUnorderedMultinom

Power and sample size for unordered multi-sample multinomial response

# Description

Obtains the power given sample size or obtains the sample size given power for the chi-square test for unordered multi-sample multinomial response.

## Usage

```
getDesignUnorderedMultinom(
  beta = NA_real_,
  n = NA_real_,
  ngroups = NA_integer_,
  ncats = NA_integer_,
  pi = NA_real_,
  allocationRatioPlanned = NA_integer_,
  rounding = TRUE,
  alpha = 0.05
)
```

#### **Arguments**

beta	The type II error.	
n	The total sample size.	
ngroups	The number of treatment groups.	
ncats	The number of categories of the multinomial response.	
pi	The matrix of response probabilities for the treatment groups. It should have ngroups rows and ncats-1 or ncats columns.	
allocationRatioPlanned		
	Allocation ratio for the treatment groups.	
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.	
alpha	The two-sided significance level. Defaults to 0.05.	

# Value

An S3 class designUnorderedMultinom object with the following components:

- power: The power to reject the null hypothesis.
- alpha: The two-sided significance level.
- n: The maximum number of subjects.
- ngroups: The number of treatment groups.
- ncats: The number of categories of the multinomial response.
- pi: The response probabilities for the treatment groups.
- effectsize: The effect size for the chi-square test.
- allocationRatioPlanned: Allocation ratio for the treatment groups.
- rounding: Whether to round up sample size.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

getDesignWilcoxon 177

## **Examples**

getDesignWilcoxon

Group sequential design for two-sample Wilcoxon test

#### **Description**

Obtains the power given sample size or obtains the sample size given power for a group sequential design for two-sample Wilcoxon test.

# Usage

```
getDesignWilcoxon(
 beta = NA_real_,
  n = NA_real_,
 pLarger = 0.6,
 allocationRatioPlanned = 1,
  rounding = TRUE,
  kMax = 1L
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_
)
```

# Arguments

```
beta The type II error.

n The total sample size.
```

178 getDesignWilcoxon

pLarger The probability that a randomly chosen sample from the treatment group is

larger than a randomly chosen sample from the control group under the alter-

native hypothesis.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

kMax The maximum number of stages.

informationRates

The information rates. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds

are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

getDesignWilcoxon 179

#### Value

An S3 class designWilcoxon object with three components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlpha: The attained significance level, which is different from the overall significance level in the presence of futility stopping..
  - kMax: The number of stages.
  - theta: The parameter value.
  - information: The maximum information.
  - expectedInformationH1: The expected information under H1.
  - expectedInformationH0: The expected information under H0.
  - drift: The drift parameter, equal to theta\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numberOfSubjects: The maximum number of subjects.
  - expectedNumberOfSubjectsH1: The expected number of subjects under H1.
  - expectedNumberOfSubjectsH0: The expected number of subjects under H0.
  - pLarger: The probability that a randomly chosen sample from the treatment group is larger than a randomly chosen sample from the control group under the alternative hypothesis.
- by StageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
  - rejectPerStageH0: The probability for efficacy stopping under H0.
  - futilityPerStageH0: The probability for futility stopping under H0.
  - cumulativeRejectionH0: The cumulative probability for efficacy stopping under H0.
  - cumulativeFutilityH0: The cumulative probability for futility stopping under H0.
  - efficacyPLarger: The efficacy boundaries on the proportion of pairs of samples from the two treatment groups with the sample from the treatment group greater than that from the control group.

- futilityPLarger: The futility boundaries on the proportion of pairs of samples from the two treatment groups with the sample from the treatment group greater than that from the control group.
- numberOfSubjects: The number of subjects.
- settings: A list containing the following input parameters:
  - typeAlphaSpending: The type of alpha spending.
  - parameterAlphaSpending: The parameter value for alpha spending.
  - userAlphaSpending: The user defined alpha spending.
  - typeBetaSpending: The type of beta spending.
  - parameterBetaSpending: The parameter value for beta spending.
  - userBetaSpending: The user defined beta spending.
  - spendingTime: The error spending time at each analysis.
  - allocationRatioPlanned: Allocation ratio for the active treatment versus control.
  - rounding: Whether to round up sample size.

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
# Example 1: fixed design
(design1 <- getDesignWilcoxon(
  beta = 0.1, n = NA,
  pLarger = pnorm((8 - 2)/sqrt(2*25^2)), alpha = 0.025))
# Example 2: group sequential design
(design2 <- getDesignWilcoxon(
  beta = 0.1, n = NA,
  pLarger = pnorm((8 - 2)/sqrt(2*25^2)), alpha = 0.025,
  kMax = 3, typeAlphaSpending = "sfOF"))</pre>
```

getDurationFromNevents

Range of accrual duration for target number of events

# Description

Obtains a range of accrual duration to reach the target number of events.

## Usage

```
getDurationFromNevents(
  nevents = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  npoints = 23L,
  interval = as.numeric(c(0.001, 240))
)
```

## **Arguments**

nevents The target number of events.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

followupTime	Follow-up time for the last enrolled subjects. Must be provided for fixed follow-up design.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
npoints	The number of accrual duration time points. Defaults to 23.
interval	The interval to search for the solution of accrualDuration. Defaults to c(0.001, 240).

#### Value

A data frame of the following variables:

- nevents: The target number of events.
- fixedFollowup: Whether a fixed follow-up design is used.
- accrualDuration: The accrual duration.
- subjects: The total number of subjects.
- followupTime: The follow-up time for the last enrolled subject.
- studyDuration: The study duration.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

getDurationFromNevents(
   nevents = 80, allocationRatioPlanned = 1,
   accrualTime = seq(0, 8),
   accrualIntensity = 26/9*seq(1, 9),
   piecewiseSurvivalTime = c(0, 6),
   stratumFraction = c(0.2, 0.8),
   lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
   lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
   gamma1 = -log(1-0.05)/12,
   gamma2 = -log(1-0.05)/12,
   fixedFollowup = FALSE)
```

getNeventsFromHazardRatio

Get the required number of events given hazard ratio

## **Description**

Obtains the required number of events given the hazard ratios under the null and alternative hypotheses for a group sequential design.

## Usage

```
getNeventsFromHazardRatio(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  spendingTime = NA_real_,
  hazardRatioH0 = 1,
  hazardRatio = NA_real_,
  allocationRatioPlanned = 1,
  rounding = 1L
)
```

## **Arguments**

beta Type II error. Defaults to 0.2.

kMax The maximum number of stages.

informationRates

The information rates in terms of number of events. Fixed prior to the trial. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

## userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

## userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

hazardRatioH0 Hazard ratio under the null hypothesis for the active treatment versus control.

Defaults to 1 for superiority test.

hazardRatio Hazard ratio under the alternative hypothesis for the active treatment versus control. Defaults to 0.5.

## $allocation {\tt RatioPlanned}$

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

rounding Whether to round up the number of events. Defaults to 1 for rounding.

#### Value

The required number of events.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

getRCI 185

## **Examples**

```
getNeventsFromHazardRatio(
  beta = 0.2, kMax = 2,
  informationRates = c(0.5,1),
  alpha = 0.025, typeAlphaSpending = "sfOF",
  typeBetaSpending = "sfP",
  hazardRatio = 0.673)
```

getRCI

Repeated confidence interval for group sequential design

# **Description**

Obtains the repeated confidence interval for a group sequential trial.

## Usage

```
getRCI(
  L = NA_integer_,
  zL = NA_real_,
  IMax = NA_real_,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sf0F",
  parameterAlphaSpending = NA_real_,
  spendingTime = NA_real_
```

#### **Arguments**

alpha

The significance level. Defaults to 0.025.

186 getRCI

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value of alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

spendingTime

The error spending time up to look L. Defaults to missing, in which case, it is the same as informationRates.

## Value

A data frame with the following components:

- pvalue: Repeated p-value for rejecting the null hypothesis.
- the tahat: Point estimate of the parameter.
- cilevel: Confidence interval level.
- lower: Lower bound of repeated confidence interval.
- upper: Upper bound of repeated confidence interval.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## References

Christopher Jennison and Bruce W. Turnbull. Interim analyses: the repeated confidence interval approach (with discussion). J R Stat Soc Series B. 1989;51:305-361.

## **Examples**

heart 187

```
getRCI(L = L, zL = zL, IMax = n/(4*sigma1^2),
    informationRates = c(1/3, 2/3), alpha = 0.05,
    typeAlphaSpending = "sfHSD", parameterAlphaSpending = -4)
```

heart

Stanford heart transplant data from the survival package

# Description

Survival of patients on the waiting list for the Stanford heart transplant program.

```
start, stop, event entry and exit time and status for the time interval age age-48 years year of acceptance (in years after Nov 1, 1967) surgery prior bypass surgery 1=yes, 0=no transplant received transplant 1=yes, 0=no id patient id
```

# Usage

heart

## **Format**

An object of class data. frame with 172 rows and 8 columns.

hedgesg

Hedges' g effect size

# Description

Obtains Hedges' g estimate and confidence interval of effect size.

# Usage

```
hedgesg(tstat, m, ntilde, cilevel = 0.95)
```

# Arguments

tstat	The value of the t-test statistic for comparing two treatment conditions.
m	The degrees of freedom for the t-test.
ntilde	The normalizing sample size to convert the standardized treatment difference to the t-test statistic, i.e., tstat = sqrt(ntilde)*meanDiff/stDev.
cilevel	The confidence interval level. Defaults to 0.95.

188 hedgesg

## **Details**

Hedges' g is an effect size measure commonly used in meta-analysis to quantify the difference between two groups. It's an improvement over Cohen's d, particularly when dealing with small sample sizes.

The formula for Hedges' g is

$$g = c(m)d$$
,

where d is Cohen's d effect size estimate, and c(m) is the bias correction factor,

$$d = (\hat{\mu}_1 - \hat{\mu}_2)/\hat{\sigma},$$

$$c(m) = 1 - \frac{3}{4m - 1}.$$

Since c(m) < 1, Cohen's d overestimates the true effect size.  $\delta = (\mu_1 - \mu_2)/\sigma$ . Since

$$t = \sqrt{\tilde{n}}d.$$

we have

$$g = \frac{c(m)}{\sqrt{\tilde{n}}}t,$$

where t has a noncentral t distribution with m degrees of freedom and noncentrality parameter  $\sqrt{\tilde{n}}\delta$ .

The asymptotic variance of g can be approximated by

$$Var(g) = \frac{1}{\tilde{n}} + \frac{g^2}{2m}.$$

The confidence interval for  $\delta$  can be constructed using normal approximation.

For two-sample mean difference with sample size  $n_1$  for the treatment group and  $n_2$  for the control group, we have  $\tilde{n} = \frac{n_1 n_2}{n_1 + n_2}$  and  $m = n_1 + n_2 - 2$  for pooled variance estimate.

## Value

A data frame with the following variables:

- tstat: The value of the t test statistic.
- m: The degrees of freedom for the t-test.
- ntilde: The normalizing sample size to convert the standardized treatment difference to the t-test statistic.
- g: Hedges' g effect size estimate.
- varg: Variance of g.
- lower: The lower confidence limit for effect size.
- upper: The upper confidence limit for effect size.
- cilevel: The confidence interval level.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

kmdiff 189

## References

Larry V. Hedges. Distribution theory for Glass's estimator of effect size and related estimators. Journal of Educational Statistics 1981; 6:107-128.

## **Examples**

```
n1 = 7
n2 = 8
meanDiff = 0.444
stDev = 1.201
m = n1+n2-2
ntilde = n1*n2/(n1+n2)
tstat = sqrt(ntilde)*meanDiff/stDev
hedgesg(tstat, m, ntilde)
```

kmdiff

Estimate of milestone survival difference

## **Description**

Obtains the estimate of milestone survival difference between two treatment groups.

## Usage

```
kmdiff(
  data,
  rep = "rep",
  stratum = "stratum",
  treat = "treat",
  time = "time",
  event = "event",
  milestone = NA_real_,
  survDiffH0 = 0,
  confint = 0.95
)
```

## **Arguments**

data

The input data frame that contains the following variables:

- rep: The replication for by-group processing.
- stratum: The stratum.
- treat: The treatment.
- time: The possibly right-censored survival time.
- event: The event indicator.

190 kmdiff

rep The name of the replication variable in the input data.

stratum The name of the stratum variable in the input data.

treat The name of the treatment variable in the input data.

time The name of the time variable in the input data.

event The name of the event variable in the input data.

milestone The milestone time at which to calculate the survival probability.

survDiffH0 The difference in milestone survival probabilities under the null hypothesis. De-

faults to 0 for superiority test.

confint The level of the two-sided confidence interval for the difference in milestone

survival probabilities. Defaults to 0.95.

#### Value

A data frame with the following variables:

- rep: The replication.
- milestone: The milestone time relative to randomization.
- survDiffH0: The difference in milestone survival probabilities under the null hypothesis.
- surv1: The estimated milestone survival probability for the treatment group.
- surv2: The estimated milestone survival probability for the control group.
- survDiff: The estimated difference in milestone survival probabilities.
- vsurv1: The variance for surv1.
- vsurv2: The variance for surv2.
- vsurvDiff: The variance for survDiff.
- survDiffZ: The Z-statistic value.
- survDiffPValue: The one-sided p-value.
- lower: The lower bound of confidence interval.
- upper: The upper bound of confidence interval.
- confint: The level of confidence interval.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

kmest 191

kmest

Kaplan-Meier estimates of the survival curve

## **Description**

Obtains the Kaplan-Meier estimates of the survival curve.

## Usage

```
kmest(
  data,
  rep = "rep",
  stratum = "stratum",
  time = "time",
  event = "event",
  conftype = "log-log",
  confint = 0.95
)
```

# **Arguments**

data The input data frame that contains the following variables:

• rep: The replication for by-group processing.

• stratum: The stratum.

• time: The possibly right-censored survival time.

• event: The event indicator.

rep The name of the replication variable in the input data.

stratum The name of the stratum variable in the input data.

time The name of the time variable in the input data.

event The name of the event variable in the input data.

conftype The type of confidence interval. One of "none", "plain", "log", "log-log" (the de-

fault), or "arcsin". The arcsin option bases the intervals on asin(sqrt(survival)).

The level of the two-sided confidence interval for the survival probabilities. De-

faults to 0.95.

#### Value

confint

A data frame with the following variables:

- rep: The replication.
- stratum: The stratum.
- size: The number of subjects in the stratum.
- time: The event time.
- nrisk: The number of subjects at risk.

- nevent: The number of subjects having the event.
- survival: The Kaplan-Meier estimate of the survival probability.
- stderr: The standard error of the estimated survival probability based on the Greendwood formula.
- lower: The lower bound of confidence interval if requested.
- upper: The upper bound of confidence interval if requested.
- confint: The level of confidence interval if requested.
- conftype: The type of confidence interval if requested.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

kmpower

Power for difference in milestone survival probabilities

## **Description**

Estimates the power for testing the difference in milestone survival probabilities in a two-sample survival design.

## Usage

```
kmpower(
 kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
 milestone = NA_real_,
  survDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
```

```
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
spendingTime = NA_real_,
studyDuration = NA_real_
```

## **Arguments**

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha

The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and

gamma for "sfHSD".

milestone The milestone time at which to calculate the survival probability.

survDiffH0 The difference in milestone survival probabilities under the null hypothesis. De-

faults to 0 for superiority test.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event

intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambdal A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and

followupTime.

#### Value

An S3 class kmpower object with 3 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - drift: The drift parameter, equal to (survDiff survDiffH0)\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numbeOfSubjects: The total number of subjects.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up duration.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - kMax: The number of stages.
  - milestone: The milestone time relative to randomization.
  - survDiffH0: The difference in milestone survival probabilities under the null hypothesis.
  - surv1: The milestone survival probability for the treatment group.
  - surv2: The milestone survival probability for the control group.
  - survDiff: The difference in milestone survival probabilities, equal to surv1 surv2.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacySurvDiff: The efficacy boundaries on the survival difference scale.
  - futilitySurvDiff: The futility boundaries on the survival difference scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

kmpower1s

Power for one-sample milestone survival probability

## Description

Estimates the power, stopping probabilities, and expected sample size in a one-group survival design.

## Usage

```
kmpower1s(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
 milestone = NA_real_,
  survH0 = NA_real_,
  accrualTime = 0L,
```

```
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda = NA_real_,
gamma = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
spendingTime = NA_real_,
studyDuration = NA_real_
```

## Arguments

kMax The ma

The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha

The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and

gamma for "sfHSD".

milestone The milestone time at which to calculate the survival probability.

The milestone survival probability under the null hypothesis.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event

intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda A vector of hazard rates for the event in each analysis time interval by stratum

under the alternative hypothesis.

gamma The hazard rate for exponential dropout or a vector of hazard rates for piecewise

exponential dropout. Defaults to 0 for no dropout.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and

followupTime.

### Value

An S3 class kmpower1s object with 3 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - drift: The drift parameter, equal to (surv survH0)\*sqrt(information).
  - inflationFactor: The inflation factor (relative to the fixed design).
  - numbeOfSubjects: The total number of subjects.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfSubjects: The expected number of subjects.

- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- kMax: The number of stages.
- milestone: The milestone time to calculate the survival probability.
- survH0: The milestone survival probability under the null hypothesis.
- surv: The milestone survival probability under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacySurv: The efficacy boundaries on the milestone survival probability scale.
  - futilitySurv: The futility boundaries on the milestone survival probability scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda, gamma, and spendingTime.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## See Also

kmstat

## **Examples**

200 kmpowerequiv

```
accrualIntensity = 26/9*seq(1, 9),
piecewiseSurvivalTime = c(0, 6),
stratumFraction = c(0.2, 0.8),
lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
gamma = -log(1-0.05)/12, accrualDuration = 22,
followupTime = 18, fixedFollowup = FALSE)
```

kmpowerequiv

Power for equivalence in milestone survival probability difference

## **Description**

Obtains the power for equivalence in milestone survival probability difference.

## Usage

```
kmpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
 milestone = NA_real_,
  survDiffLower = NA_real_,
  survDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
 piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

## **Arguments**

kMax

The maximum number of stages.

kmpowerequiv 201

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

milestone The milestone time at which to calculate the survival probability.

survDiffLower 
The lower equivalence limit of milestone survival probability difference.

survDiffUpper The upper equivalence limit of milestone survival probability difference.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime A vector

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

202 kmpowerequiv

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrual $\mathsf{Duration}$  and followup $\mathsf{Time}$ . If provided, the value is allowed to be less than the sum of accrual $\mathsf{Duration}$  and

followupTime.

#### Value

An S3 class kmpowerequiv object with 3 components:

• overallResults: A data frame containing the following variables:

- overallReject: The overall rejection probability.
- alpha: The overall significance level.
- attainedAlphaH10: The attained significance level under H10.
- attainedAlphaH20: The attained significance level under H20.
- numbeOfSubjects: The total number of subjects.
- studyDuration: The total study duration.
- information: The maximum information.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- kMax: The number of stages.
- milestone: The milestone time relative to randomization.
- survDiffLower: The lower equivalence limit of milestone survival probability difference.
- survDiffUpper: The upper equivalence limit of milestone survival probability difference.
- surv1: The milestone survival probability for the treatment group.
- surv2: The milestone survival probability for the control group.
- survDiff: The milestone survival probability difference.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.

- cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
- cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
- cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
- numberOfSubjects: The number of subjects.
- analysisTime: The average time since trial start.
- efficacySurvDiffLower: The efficacy boundaries on the milestone survival probability difference scale for the one-sided null hypothesis at the lower equivalence limit.
- efficacySurvDiffUpper: The efficacy boundaries on the milestone survival probability difference scale for the one-sided null hypothesis at the upper equivalence limit.
- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### See Also

kmstat

## **Examples**

```
kmpowerequiv(kMax = 2, informationRates = c(0.5, 1), alpha = 0.05, typeAlphaSpending = "sf0F", milestone = 18, survDiffLower = -0.13, survDiffUpper = 0.13, allocationRatioPlanned = 1, accrualTime = seq(0, 8), accrualIntensity = 26/9*seq(1, 9), piecewiseSurvivalTime = c(0, 6), stratumFraction = c(0.2, 0.8), lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12, accrualDuration = 22, followupTime = 18, fixedFollowup = FALSE)
```

kmsamplesize

Sample size for difference in milestone survival probabilities

## **Description**

Obtains the needed accrual duration given power, accrual intensity, and follow-up time, the needed follow-up time given power, accrual intensity, and accrual duration, or the needed absolute accrual intensity given power, relative accrual intensity, accrual duration, and follow-up time in a two-group survival design.

## Usage

```
kmsamplesize(
 beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
 efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
 milestone = NA_real_,
  survDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
 piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

## **Arguments**

beta Type II error. Defaults to 0.2. kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

## typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

## parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

## userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

milestone The milestone time at which to calculate the survival probability.

SurvDiffH0 The difference in milestone survival probabilities under the null hypothesis. Defaults to 0 for superiority test.

## allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

#### accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

## piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

## stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1	A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.			
lambda2	A vector of hazard rates for the event in each analysis time interval by stratum for the control group.			
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.			
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.			
accrualDuration				
	Duration of the enrollment period.			
followupTime	Follow-up time for the last enrolled subject.			
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.			
interval	The interval to search for the solution of accrualDuration, followupTime, or the proportionality constant of accrualIntensity. Defaults to $c(0.001, 240)$ .			
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.			
rounding	Whether to round up sample size. Defaults to 1 for sample size rounding.			

## Value

A list of two components:

- resultsUnderH1: An S3 class kmpower object under the alternative hypothesis.
- resultsUnderH0: An S3 class kmpower object under the null hypothesis.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## See Also

kmpower

## **Examples**

```
stratumFraction = c(0.2, 0.8),
            lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
            lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
            gamma1 = -log(1-0.05)/12,
            gamma2 = -\log(1-0.05)/12, accrualDuration = 22,
            followupTime = NA, fixedFollowup = FALSE)
# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up time for variable follow-up
kmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
            alpha = 0.025, typeAlphaSpending = "sfOF",
            milestone = 18,
            allocationRatioPlanned = 1, accrualTime = seq(0, 8),
            accrualIntensity = 26/9*seq(1, 9),
            piecewiseSurvivalTime = c(0, 6),
            stratumFraction = c(0.2, 0.8),
            lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
            lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
            gamma1 = -log(1-0.05)/12,
            gamma2 = -\log(1-0.05)/12, accrualDuration = 22,
            followupTime = 18, fixedFollowup = FALSE)
# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up time for fixed follow-up
kmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
            alpha = 0.025, typeAlphaSpending = "sfOF",
            milestone = 18,
            allocationRatioPlanned = 1, accrualTime = seq(0, 8),
            accrualIntensity = 26/9*seq(1, 9),
            piecewiseSurvivalTime = c(0, 6),
            stratumFraction = c(0.2, 0.8),
            lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
            lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
            gamma1 = -log(1-0.05)/12,
            gamma2 = -log(1-0.05)/12, accrualDuration = NA,
            followupTime = 18, fixedFollowup = TRUE)
```

kmsamplesize1s

Sample size for one-sample milestone survival probability

## **Description**

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group survival design.

## Usage

```
kmsamplesize1s(
 beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
 efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
 milestone = NA_real_,
  survH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

# Arguments

beta Type II error. Defaults to 0.2.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

critical Values Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

#### typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

## userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

## userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

milestone The milestone time at which to calculate the survival probability.

SurvH0 The milestone survival probability under the null hypothesis.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

## accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

## piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

#### stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda A vector of hazard rates for the event in each analysis time interval by stratum

under the alternative hypothesis.

gamma The hazard rate for exponential dropout or a vector of hazard rates for piecewise

exponential dropout. Defaults to 0 for no dropout.

### accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

The interval to search for the solution of accrualDuration, followupDuration, or the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

## Value

A list of two components:

- resultsUnderH1: An S3 class kmpower1s object under the alternative hypothesis.
- resultsUnderH0: An S3 class kmpower1s object under the null hypothesis.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### See Also

kmpower1s

## **Examples**

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up
kmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
              milestone = 18, survH0 = 0.30,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -\log(1-0.05)/12, accrualDuration = 22,
               followupTime = NA, fixedFollowup = FALSE)
# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up
kmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
              milestone = 18, survH0 = 0.30,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
```

kmsamplesizeequiv 211

```
stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -\log(1-0.05)/12, accrualDuration = 22,
               followupTime = 18, fixedFollowup = FALSE)
# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up
kmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               milestone = 18, survH0 = 0.30,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -\log(1-0.05)/12, accrualDuration = NA,
               followupTime = 18, fixedFollowup = TRUE)
```

kmsamplesizeequiv

Sample size for equivalence in milestone survival probability difference

## Description

Obtains the sample size for equivalence in milestone survival probability difference.

## Usage

```
kmsamplesizeequiv(
 beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
 milestone = NA_real_,
  survDiffLower = NA_real_,
  survDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
```

212 kmsamplesizeequiv

```
lambda1 = NA_real_,
lambda2 = NA_real_,
gamma1 = 0L,
gamma2 = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
interval = as.numeric(c(0.001, 240)),
spendingTime = NA_real_,
rounding = 1L
```

## Arguments

beta The type II error.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

milestone The milestone time at which to calculate the survival probability.

survDiffLower The lower equivalence limit of milestone survival probability difference.

survDiffUpper The upper equivalence limit of milestone survival probability difference.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval. piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

kmsamplesizeequiv 213

c+	rati	ım⊢	rac	٠+٦	nn
3 L	ıaı	ullil	ıav	. L.I	OI

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval The interval to search for the solution of accrualDuration, followupDuration, or

the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

#### Value

An S3 class kmpowerequiv object

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### See Also

kmpowerequiv

## **Examples**

```
kmsamplesizeequiv(beta = 0.1, kMax = 2, informationRates = c(0.5, 1), alpha = 0.05, typeAlphaSpending = "sfOF", milestone = 18, survDiffLower = -0.13, survDiffUpper = 0.13, allocationRatioPlanned = 1, accrualTime = seq(0, 8), accrualIntensity = 26/9*seq(1, 9), piecewiseSurvivalTime = c(0, 6), stratumFraction = c(0.2, 0.8), lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
```

214 kmstat

```
gamma1 = -\log(1-0.05)/12,
gamma2 = -\log(1-0.05)/12, accrualDuration = NA,
followupTime = 18, fixedFollowup = FALSE)
```

kmstat

Stratified difference in milestone survival probabilities

# Description

Obtains the stratified milestone survival probabilities and difference in milestone survival probabilities at given calendar times.

## Usage

```
kmstat(
  time = NA_real_,
  milestone = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L
)
```

### **Arguments**

time A vector of calendar times for data cut.

milestone The milestone time at which to calculate the survival probability.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

kmstat 215

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

#### Value

A data frame containing the following variables:

- time: The calendar time since trial start.
- subjects: The number of enrolled subjects.
- milestone: The milestone time relative to randomization.
- surv1: The milestone survival probability for the treatment group.
- surv2: The milestone survival probability for the control group.
- survDiff: The difference in milestone survival probabilities, i.e., surv1 surv2.
- vsurv1: The variance for surv1.
- vsurv2: The variance for surv2.
- vsurvDiff: The variance for survDiff.
- information: The information for survDiff, equal to 1/vsurvDiff.
- survDiffZ: The Z-statistic value, i.e., survDiff/sqrt(vsurvDiff).

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

216 liferegr

## **Examples**

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

kmstat(time = c(22, 40),
    milestone = 18,
    allocationRatioPlanned = 1,
    accrualTime = seq(0, 8),
    accrualIntensity = 26/9*seq(1, 9),
    piecewiseSurvivalTime = c(0, 6),
    stratumFraction = c(0.2, 0.8),
    lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
    lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
    gamma1 = -log(1-0.05)/12,
    gamma2 = -log(1-0.05)/12,
    accrualDuration = 22,
    followupTime = 18, fixedFollowup = FALSE)
```

liferegr

Parametric regression models for failure time data

## **Description**

Obtains the parameter estimates from parametric regression models with uncensored, right censored, left censored, or interval censored data.

## Usage

```
liferegr(
  data,
  rep = "rep",
  stratum = "stratum",
  time = "time",
  time2 = "time2",
  event = "event",
  covariates = "treat",
  weight = "weight",
  id = "id",
  dist = "weibull",
  robust = 0L
)
```

# **Arguments**

data

The input data frame that contains the following variables:

- rep: The replication for by-group processing.
- stratum: The stratum.

liferegr 217

 time: The follow-up time for right censored data, or the left end of each interval for interval censored data.

- time2: The right end of each interval for interval censored data.
- event: The event indicator, normally 1=event, 0=no event.
- covariates: The values of baseline covariates. This is the full-rank design matrix (excluding the intercept) for the regression model, assuming that factor variables have already been expanded into dummy variables. The intercept will be added automatically.
- weight: The weight for each observation.

• id: The optional subject ID to group the score residuals in computing the robust sandwich variance.

rep The name of the replication variable in the input data.

stratum The name of the stratum variable in the input data.

time The name of the time variable or the left end of each interval for interval cen-

sored data in the input data.

time2 The name of the right end of each interval for interval censored data in the input

data.

event The name of the event variable in the input data for right censored data.

covariates The vector of names of baseline covariates in the input data.

weight The name of the weighting variable in the input data.

id The name of the id variable in the input data.

dist The assumed distribution for time to event. Options include "exponential",

"weibull", "lognormal", and "loglogistic" to be modeled on the log-scale, and

"normal" and "logistic" to be modeled on the original scale.

robust Whether a robust sandwich variance estimate should be computed. The default

is TRUE if there are fractional weights or there is at least 1 id with >1 event. In the presence of the id variable, the score residual will be aggregated for each id

when computing the robust sandwich variance estimate.

# **Details**

There are two ways to specify the model, one for right censored data through the time and event variables, and the other for interval censored data through the time and time2 variables. For the second form, we follow the convention used in SAS PROC LIFEREG:

- If lower is not missing, upper is not missing, and lower is equal to upper, then there is no censoring and the event occurred at time lower.
- If lower is not missing, upper is not missing, and lower < upper, then the event time is censored within the interval (lower, upper).
- If lower is missing, but upper is not missing, then upper will be used as the left censoring value.
- If lower is not missing, but upper is missing, then lower will be used as the right censoring value.
- If lower is not missing, upper is not missing, but lower > upper, or if both lower and upper are missing, then the observation will not be used.

#### Value

A list with the following components:

- sumstat: The data frame of summary statistics of model fit with the following variables:
  - rep: The replication.
  - n: The number of observations.
  - nevents: The number of events.
  - loglik0: The log-likelihood under null.
  - loglik1: The maximum log-likelihood.
  - scoretest: The score test statistic.
- parest: The data frame of parameter estimates with the following variables:
  - rep: The replication.
  - param: The name of the covariate for the parameter estimate.
  - beta: The parameter estimate.
  - sebeta: The standard error of parameter estimate.
  - z: The Wald test statistic.
  - expbeta: The exponentiated parameter.
  - vbeta: The covariance matrix for parameter estimates.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

lrpower

Log-rank test power

### **Description**

Estimates the power, stopping probabilities, and expected sample size in a two-group survival design.

lrpower 219

# Usage

```
lrpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  numSubintervals = 300L,
  estimateHazardRatio = 1L,
  typeOfComputation = "direct",
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

# **Arguments**

kMax The maximum number of stages.

information Rates

The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to (1:kMax) / kMax if left unspecified.

 ${\it efficacyStopping}$ 

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true

if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

hazardRatioH0 Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

# allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g.,  $c(\emptyset, 3)$  breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

## accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

## piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

#### stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test.

Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank

test. Defaults to 0 for conventional log-rank test.

numSubintervals

Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better

approximation.

estimateHazardRatio

Whether to estimate the hazard ratio from weighted Cox regression model and

report the stopping boundaries on the hazard ratio scale.

typeOfComputation

The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoen-

feld" under proportional hazards and conventional log-rank test.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and

followupTime.

#### Value

An S3 class 1rpower object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.

- studyDuration: The total study duration.
- information: The maximum information.
- expectedNumberOfEvents: The expected number of events.
- expectedNumberOfDropouts: The expected number of dropouts.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- accrualDuration: The accrual duration.
- followupTime: The follow-up time.
- fixedFollowup: Whether a fixed follow-up design is used.
- rho1: The first parameter of the Fleming-Harrington family of weighted log-rank test.
- rho2: The second parameter of the Fleming-Harrington family of weighted log-rank test.
- kMax: The number of stages.
- hazardRatioH0: The hazard ratio under the null hypothesis.
- typeOfComputation: The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - ${\tt -}$  efficacyHR: The efficacy boundaries on the hazard ratio scale if estimateHazardRatio.
  - futilityHR: The futility boundaries on the hazard ratio scale if estimateHazardRatio.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - HR: The average hazard ratio.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, estimateHazardRatio, and spendingTime.
- byTreatmentCounts: A list containing the following counts by treatment group:

- numberOfEvents1: The number of events by stage for the treatment group.
- numberOfDropouts1: The number of dropouts by stage for the treatment group.
- number Of Subjects 1: The number of subjects by stage for the treatment group.
- numberOfEvents2: The number of events by stage for the control group.
- numberOfDropouts2: The number of dropouts by stage for the control group.
- numberOfSubjects2: The number of subjects by stage for the control group.
- expectedNumberOfEvents1: The expected number of events for the treatment group.
- expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
- expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
- expectedNumberOfEvents2: The expected number of events for control group.
- expectedNumberOfDropouts2: The expected number of dropouts for the control group.
- expectedNumberOfSubjects2: The expected number of subjects for the control group.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

lrpower(kMax = 2, informationRates = c(0.8, 1),
    alpha = 0.025, typeAlphaSpending = "sfOF",
    allocationRatioPlanned = 1, accrualTime = seq(0, 8),
    accrualIntensity = 26/9*seq(1, 9),
    piecewiseSurvivalTime = c(0, 6),
    stratumFraction = c(0.2, 0.8),
    lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
    lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
    gamma1 = -log(1-0.05)/12,
    gamma2 = -log(1-0.05)/12, accrualDuration = 22,
    followupTime = 18, fixedFollowup = FALSE)
```

lrpowerequiv

Power for equivalence in hazard ratio

### Description

Obtains the power for equivalence in hazard ratio.

# Usage

```
lrpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  hazardRatioLower = NA_real_,
  hazardRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  typeOfComputation = "direct",
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

#### **Arguments**

kMax The maximum number of stages.

information Rates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05. typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

hazardRatioLower

The lower equivalence limit of hazard ratio.

hazardRatioUpper

The upper equivalence limit of hazard ratio.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

Tandonnzado

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

accrualTime

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

typeOfComputation

The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoen-

feld" under proportional hazards and conventional log-rank test.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and

followupTime.

#### Value

An S3 class 1rpowerequiv object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - attainedAlphaH10: The attained significance level under H10.
  - attainedAlphaH20: The attained significance level under H20.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - expectedNumberOfEvents: The expected number of events.
  - expectedNumberOfDropouts: The expected number of dropouts.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedStudyDuration: The expected study duration.
  - expectedInformation: The expected information.
  - kMax: The number of stages.
  - hazardRatioLower: The lower equivalence limit of hazard ratio.
  - hazardRatioUpper: The upper equivalence limit of hazard ratio.
  - accrualDuration: The accrual duration.
  - followupTime: The follow-up time.
  - fixedFollowup: Whether a fixed follow-up design is used.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacyHRLower: The efficacy boundaries on the hazard ratio scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacyHRUpper: The efficacy boundaries on the hazard ratio scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.

- information: The cumulative information.
- HR: The average hazard ratio.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, typeOfComputation, and spendingTime.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
  - expectedNumberOfEvents2: The expected number of events for control group.
  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
  - expectedNumberOfSubjects2: The expected number of subjects for the control group.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### See Also

rmstat

#### **Examples**

```
lrpowerequiv(kMax = 2, informationRates = c(0.5, 1), alpha = 0.05, typeAlphaSpending = "sfOF", hazardRatioLower = 0.71, hazardRatioUpper = 1.4, allocationRatioPlanned = 1, accrualTime = seq(0, 8), accrualIntensity = 100/9*seq(1, 9), piecewiseSurvivalTime = c(0, 6), stratumFraction = c(0.2, 0.8), lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12, accrualDuration = 22, followupTime = 18, fixedFollowup = FALSE)
```

lrsamplesize

Log-rank test sample size

### **Description**

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up time, and relative accrual rates in a two-group survival design.

# Usage

```
lrsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  numSubintervals = 300L,
  estimateHazardRatio = 1L,
  typeOfComputation = "direct",
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
```

### **Arguments**

beta Type II error. Defaults to 0.2.

The maximum number of stages. kMax

informationRates

The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

hazardRatioH0 Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test.

Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank

test. Defaults to 0 for conventional log-rank test.

numSubintervals

Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better

approximation.

estimateHazardRatio

Whether to estimate the hazard ratio from weighted Cox regression model and report the stopping boundaries on the hazard ratio scale.

typeOfComputation

The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoenfeld" under proportional hazards and conventional log-rank test.

The interval to search for the solution of accrualDuration, followupTime, or the proportionality constant of accrualIntensity. Defaults to c(0.001, 240). Adjustment may be needed for non-monotone relationship with study power.

SpendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

Tounding Whether to round up sample size and events. Defaults to 1 for sample size

rounding.

#### Value

A list of two components:

- resultsUnderH1: An S3 class 1rpower object under the alternative hypothesis.
- resultsUnderH0: An S3 class 1rpower object under the null hypothesis.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### See Also

**1rpower** 

# **Examples**

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.
# Example 1: Obtains accrual duration given power and follow-up time
lrsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12,
             accrualDuration = NA,
             followupTime = 18, fixedFollowup = FALSE)
# Example 2: Obtains follow-up time given power and accrual duration
lrsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualTime = seq(0, 8),
```

232 Irsamplesizeequiv

```
accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12,
             accrualDuration = 22,
             followupTime = NA, fixedFollowup = FALSE)
# Example 3: Obtains absolute accrual intensity given power,
# accrual duration, follow-up time, and relative accrual intensity
lrsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualTime = seq(0, 8),
             accrualIntensity = 26/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -log(1-0.05)/12,
             accrualDuration = 22,
             followupTime = 18, fixedFollowup = FALSE)
```

lrsamplesizeequiv

Sample size for equivalence in hazard ratio

# **Description**

Obtains the sample size for equivalence in hazard ratio.

### Usage

```
lrsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  hazardRatioLower = NA_real_,
  hazardRatioUpper = NA_real_,
```

Irsamplesizeequiv 233

```
allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  typeOfComputation = "direct",
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

#### **Arguments**

beta The type II error.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

hazardRatioLower

The lower equivalence limit of hazard ratio.

hazardRatioUpper

The upper equivalence limit of hazard ratio.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

234 Irsamplesizeequiv

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

typeOfComputation

The type of computation, either "direct" for the direct approximation method, or "schoenfeld" for the Schoenfeld method. Defaults to "direct". Can use "Schoen-

feld" under proportional hazards and conventional log-rank test.

interval The interval to search for the solution of accrualDuration, followupDuration, or

the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

### Value

An S3 class 1rpowerequiv object

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### See Also

lrpowerequiv

### **Examples**

```
lrsamplesizeequiv(kMax = 2, informationRates = c(0.5, 1), alpha = 0.05, typeAlphaSpending = "sfOF", hazardRatioLower = 0.71, hazardRatioUpper = 1.4, allocationRatioPlanned = 1, accrualTime = seq(0, 8), accrualIntensity = 26/9*seq(1, 9), piecewiseSurvivalTime = c(0, 6), stratumFraction = c(0.2, 0.8), lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12, accrualDuration = NA, followupTime = 18, fixedFollowup = FALSE)
```

lrsim

Log-rank test simulation

#### **Description**

Performs simulation for two-arm group sequential trials based on weighted log-rank test.

# Usage

```
lrsim(
  kMax = NA_integer_,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  futilityBounds = NA_real_,
  hazardRatioH0 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
```

```
maxNumberOfIterations = 1000L,
maxNumberOfRawDatasetsPerStage = 0L,
seed = NA_integer_
)
```

#### **Arguments**

kMax

The maximum number of stages.

informationRates

The information rates in terms of number of events for the conventional log-rank test and in terms of the actual information for weighted log-rank tests. Fixed prior to the trial. If left unspecified, it defaults to plannedEvents / plannedEvents[kMax] when plannedEvents is provided and to plannedTime / plannedTime[kMax] otherwise.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1,

..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds

are non-binding for the calculation of critical values.

hazardRatioH0 Hazard ratio under the null hypothesis for the active treatment versus control.

Defaults to 1 for superiority test.

allocation1 Number of subjects in the active treatment group in a randomization block. De-

faults to 1 for equal randomization.

allocation2 Number of subjects in the control group in a randomization block. Defaults to 1

for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test.

Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank

test. Defaults to 0 for conventional log-rank test.

plannedEvents The planned cumulative total number of events at each stage.

plannedTime The calendar times for the analyses. To use calendar time to plan the analyses,

plannedEvents should be missing.

maxNumberOfIterations

The number of simulation iterations. Defaults to 1000.

 ${\tt maxNumberOfRawDatasetsPerStage}$ 

The number of raw datasets per stage to extract. Defaults to 1.

seed The seed to reproduce the simulation results. The seed from the environment

will be used if left unspecified,

#### Value

An S3 class 1rsim object with 3 components:

- overview: A list containing the following information:
  - rejectPerStage: The efficacy stopping probability by stage.
  - futilityPerStage: The futility stopping probability by stage.
  - cumulativeRejection: Cumulative efficacy stopping probability by stage.
  - cumulativeFutility: The cumulative futility stopping probability by stage.
  - numberOfEvents: The average number of events by stage.
  - numberOfDropouts: The average number of dropouts by stage.
  - numberOfSubjects: The average number of subjects by stage.
  - analysisTime: The average analysis time by stage.
  - overallReject: The overall rejection probability.
  - expectedNumberOfEvents: The expected number of events for the overall study.
  - expectedNumberOfDropouts: The expected number of dropouts for the overall study.
  - expectedNumberOfSubjects: The expected number of subjects for the overall study.
  - expectedStudyDuration: The expected study duration.
  - hazardRatioH0: Hazard ratio under the null hypothesis for the active treatment versus control.
  - useEvents: whether the analyses are planned based on the number of events or calendar time
  - accrualDuration: Duration of the enrollment period.
  - fixedFollowup: Whether a fixed follow-up design is used.
  - rho1: The first parameter of the Fleming-Harrington family of weighted log-rank test.
     Defaults to 0 for conventional log-rank test.

rho2: The second parameter of the Fleming-Harrington family of weighted log-rank test.
 Defaults to 0 for conventional log-rank test.

- kMax: The maximum number of stages.
- sumdata: A data frame of summary data by iteration and stage:
  - iterationNumber: The iteration number.
  - stopStage: The stage at which the trial stops.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
  - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the treatment group.
  - accruals2: The number of subjects enrolled at the stage for the control group.
  - totalAccruals: The total number of subjects enrolled at the stage.
  - events1: The number of events at the stage for the treatment group.
  - events2: The number of events at the stage for the control group.
  - totalEvents: The total number of events at the stage.
  - dropouts1: The number of dropouts at the stage for the treatment group.
  - dropouts2: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - uscore: The numerator of the log-rank test statistic.
  - vscore: The variance of the log-rank test statistic.
  - logRankStatistic: The log-rank test Z-statistic.
  - rejectPerStage: Whether to reject the null hypothesis at the stage.
  - futilityPerStage: Whether to stop the trial for futility at the stage.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - iterationNumber: The iteration number.
  - stopStage: The stage at which the trial stops.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.
  - treatmentGroup: The treatment group (1 or 2) for the subject.
  - survivalTime: The underlying survival time for the subject.
  - dropoutTime: The underlying dropout time for the subject.
  - timeUnderObservation: The time under observation since randomization.
  - event: Whether the subject experienced the event.
  - dropoutEvent: Whether the subject dropped out.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
# Example 1: analyses based on number of events
sim1 = lrsim(kMax = 2, informationRates = c(0.5, 1),
             critical Values = c(2.797, 1.977),
             accrualIntensity = 11,
             lambda1 = 0.018, lambda2 = 0.030,
             accrualDuration = 12,
             plannedEvents = c(60, 120),
             maxNumberOfIterations = 1000,
             maxNumberOfRawDatasetsPerStage = 1,
             seed = 314159)
# summary statistics
sim1
# summary for each simulated data set
head(sim1$sumdata)
# raw data for selected replication
head(sim1$rawdata)
# Example 2: analyses based on calendar time have similar power
sim2 = 1rsim(kMax = 2, informationRates = c(0.5, 1),
             criticalValues = c(2.797, 1.977),
             accrualIntensity = 11,
             lambda1 = 0.018, lambda2 = 0.030,
             accrualDuration = 12,
             plannedTime = c(31.9, 113.2),
             maxNumberOfIterations = 1000,
             maxNumberOfRawDatasetsPerStage = 1,
             seed = 314159)
# summary statistics
sim2
# summary for each simulated data set
head(sim2$sumdata)
```

1rsim2e

Log-rank test simulation for two endpoints

### **Description**

Performs simulation for two-endpoint two-arm group sequential trials based on weighted log-rank test. The first kMaxe1 looks are driven by the total number of PFS events in two arms combined, and the subsequent looks are driven by the total number of OS events in two arms combined. Alternatively, the analyses can be planned to occur at specified calendar times.

# Usage

```
lrsim2e(
  kMax = NA_integer_,
  kMaxe1 = NA_integer_,
 hazardRatioH0e1 = 1,
 hazardRatioH0e2 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  rho = 0,
  lambda1e1 = NA_real_,
  lambda2e1 = NA_real_,
  lambda1e2 = NA_real_,
  lambda2e2 = NA_real_,
  gamma1e1 = 0L,
  gamma2e1 = 0L,
  gamma1e2 = 0L,
  gamma2e2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
 maxNumberOfIterations = 1000L,
 maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

### **Arguments**

kMax The maximum number of stages.

kMaxe1 Number of stages with timing determined by PFS events. Ranges from 0 (none)

to kMax.

hazardRatioH0e1

Hazard ratio under the null hypothesis for the active treatment vs control for

endpoint 1 (PFS). Defaults to 1 for superiority test.

hazardRatioH0e2

Hazard ratio under the null hypothesis for the active treatment vs control for

endpoint 2 (OS). Defaults to 1 for superiority test.

allocation1 Number of subjects in the treatment group in a randomization block. Defaults

to 1 for equal randomization.

allocation2 Number of subjects in the control group in a randomization block. Defaults to 1

for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

intervals. [0, 3) and [3, mi

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

rho The correlation coefficient for the standard bivariate normal random variables used to generate time to disease progression and time to death using the inverse

CDF method.

lambda1e1 A vector of hazard rates for the event in each analysis time interval by stratum

for the treatment group and endpoint 1 (PFS).

lambda2e1 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group and endpoint 1 (PFS).

lambda1e2 A vector of hazard rates for the event in each analysis time interval by stratum

for the treatment group and endpoint 2 (OS).

lambda2e2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group and endpoint 2 (OS).

gamma1e1 The hazard rate for exponential dropout, a vector of hazard rates for piecewise

exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group and

endpoint 1 (PFS).

gamma2e1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group and

endpoint 1 (PFS).

gamma1e2 The hazard rate for exponential dropout, a vector of hazard rates for piecewise

exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the treatment group and

endpoint 2 (OS).

gamma2e2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group and

endpoint 2 (OS).

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test.

Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank

test. Defaults to 0 for conventional log-rank test.

plannedEvents The planned cumulative total number of PFS events at Look 1 to Look kMaxe1

and the planned cumulative total number of OS events at Look kMaxe1+1 to

Look kMax.

plannedTime The calendar times for the analyses. To use calendar time to plan the analyses,

plannedEvents should be missing.

maxNumberOfIterations

The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage

The number of raw datasets per stage to extract. Defaults to 1.

seed The seed to reproduce the simulation results. The seed from the environment

will be used if left unspecified,

#### Value

### A list with 2 components:

• sumdata: A data frame of summary data by iteration and stage:

- iterationNumber: The iteration number.
- eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
- stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
- analysisTime: The time for the stage since trial start.
- accruals1: The number of subjects enrolled at the stage for the treatment group.
- accruals2: The number of subjects enrolled at the stage for the control group.
- totalAccruals: The total number of subjects enrolled at the stage.
- endpoint: The endpoint (1 or 2) under consideration.
- events1: The number of events at the stage for the treatment group.
- events2: The number of events at the stage for the control group.
- totalEvents: The total number of events at the stage.
- dropouts1: The number of dropouts at the stage for the treatment group.
- dropouts 2: The number of dropouts at the stage for the control group.
- totalDropouts: The total number of dropouts at the stage.
- logRankStatistic: The log-rank test Z-statistic for the endpoint.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - iterationNumber: The iteration number.
  - stageNumber: The stage under consideration.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.

- treatmentGroup: The treatment group (1 or 2) for the subject.
- survivalTime1: The underlying survival time for event endpoint 1 for the subject.
- dropoutTime1: The underlying dropout time for event endpoint 1 for the subject.
- timeUnderObservation1: The time under observation since randomization for event endpoint 1 for the subject.
- event1: Whether the subject experienced event endpoint 1.
- dropoutEvent1: Whether the subject dropped out for endpoint 1.
- survivalTime2: The underlying survival time for event endpoint 2 for the subject.
- dropoutTime2: The underlying dropout time for event endpoint 2 for the subject.
- timeUnderObservation2: The time under observation since randomization for event endpoint 2 for the subject.
- event2: Whether the subject experienced event endpoint 2.
- dropoutEvent2: Whether the subject dropped out for endpoint 2.

# Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
sim1 = lrsim2e(
  kMax = 3,
  kMaxe1 = 2,
  allocation1 = 2,
  allocation2 = 1,
  accrualTime = c(0, 8),
  accrualIntensity = c(10, 28),
  piecewiseSurvivalTime = 0,
  rho = 0,
  lambda1e1 = log(2)/12*0.60,
  lambda2e1 = log(2)/12,
  lambda1e2 = log(2)/30*0.65,
  lambda2e2 = log(2)/30,
  accrualDuration = 20.143,
  plannedEvents = c(186, 259, 183),
  maxNumberOfIterations = 1000,
  maxNumberOfRawDatasetsPerStage = 1,
  seed = 314159)
head(sim1$sumdata)
head(sim1$rawdata)
```

# **Description**

Performs simulation for two-endpoint three-arm group sequential trials based on weighted log-rank test. The first kMaxe1 looks are driven by the total number of PFS events in Arm A and Arm C combined, and the subsequent looks are driven by the total number of OS events in Arm A and Arm C combined. Alternatively, the analyses can be planned to occur at specified calendar times.

# Usage

```
lrsim2e3a(
  kMax = NA_integer_,
  kMaxe1 = NA_integer_,
  hazardRatioH013e1 = 1,
  hazardRatioH023e1 = 1,
  hazardRatioH012e1 = 1,
  hazardRatioH013e2 = 1,
  hazardRatioH023e2 = 1,
  hazardRatioH012e2 = 1,
  allocation1 = 1L,
  allocation2 = 1L,
  allocation3 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  rho = 0,
  lambda1e1 = NA_real_,
  lambda2e1 = NA_real_,
  lambda3e1 = NA_real_,
  lambda1e2 = NA_real_,
  lambda2e2 = NA_real_,
  lambda3e2 = NA_real_,
  gamma1e1 = 0L,
  gamma2e1 = 0L,
  gamma3e1 = 0L,
  gamma1e2 = 0L,
  gamma2e2 = 0L,
  gamma3e2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
 maxNumberOfIterations = 1000L,
 maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

#### **Arguments**

kMax The maximum number of stages.

kMaxe1 Number of stages with timing determined by PFS events. Ranges from 0 (none)

to kMax.

hazardRatioH013e1

Hazard ratio under the null hypothesis for arm 1 vs arm 3 for endpoint 1 (PFS).

Defaults to 1 for superiority test.

hazardRatioH023e1

Hazard ratio under the null hypothesis for arm 2 vs arm 3 for endpoint 1 (PFS). Defaults to 1 for superiority test.

hazardRatioH012e1

Hazard ratio under the null hypothesis for arm 1 vs arm 2 for endpoint 1 (PFS). Defaults to 1 for superiority test.

hazardRatioH013e2

Hazard ratio under the null hypothesis for arm 1 vs arm 3 for endpoint 2 (OS). Defaults to 1 for superiority test.

hazardRatioH023e2

Hazard ratio under the null hypothesis for arm 2 vs arm 3 for endpoint 2 (OS). Defaults to 1 for superiority test.

hazardRatioH012e2

Hazard ratio under the null hypothesis for arm 1 vs arm 2 for endpoint 2 (OS). Defaults to 1 for superiority test.

allocation1 Number of subjects in Arm A in a randomization block. Defaults to 1 for equal

randomization.

allocation2 Number of subjects in Arm B in a randomization block. Defaults to 1 for equal

randomization.

allocation3 Number of subjects in Arm C in a randomization block. Defaults to 1 for equal

randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

rho The correlation coefficient for the standard bivariate normal random variables used to generate time to disease progression and time to death using the inverse

CDF method.

lambda1e1 A vector of hazard rates for the event in each analysis time interval by stratum

for arm 1 and endpoint 1 (PFS).

lambda2e1	A vector of hazard rates for the event in each analysis time interval by stratum for arm 2 and endpoint 1 (PFS).
lambda3e1	A vector of hazard rates for the event in each analysis time interval by stratum for arm 3 and endpoint 1 (PFS).
lambda1e2	A vector of hazard rates for the event in each analysis time interval by stratum for arm 1 and endpoint 2 (OS).
lambda2e2	A vector of hazard rates for the event in each analysis time interval by stratum for arm 2 and endpoint 2 (OS).
lambda3e2	A vector of hazard rates for the event in each analysis time interval by stratum for arm 3 and endpoint 2 (OS).
gamma1e1	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1 and endpoint 1 (PFS).
gamma2e1	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2 and endpoint 1 (PFS).
gamma3e1	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3 and endpoint 1 (PFS).
gamma1e2	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 1 and endpoint 2 (OS).
gamma2e2	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 2 and endpoint 2 (OS).
gamma3e2	The hazard rate for exponential dropout. A vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for arm 3 and endpoint 2 (OS).
accrualDuration	
	Duration of the enrollment period.
followupTime	Follow-up time for the last enrolled subject.
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.
rho1	The first parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
rho2	The second parameter of the Fleming-Harrington family of weighted log-rank test. Defaults to 0 for conventional log-rank test.
plannedEvents	The planned cumulative total number of PFS events at Look 1 to Look kMaxe1 for Arms A and C combined and the planned cumulative total number of OS events at Look kMaxe1+1 to Look kMax for Arms A and C combined.
plannedTime	The calendar times for the analyses. To use calendar time to plan the analyses, plannedEvents should be missing.

maxNumberOfIterations

The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage

The number of raw datasets per stage to extract. Defaults to 1.

The seed to reproduce the simulation results. The seed from the environment will be used if left unspecified,

#### Value

### A list with 2 components:

- sumdata: A data frame of summary data by iteration and stage:
  - iterationNumber: The iteration number.
  - eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
  - stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
  - analysisTime: The time for the stage since trial start.
  - accruals1: The number of subjects enrolled at the stage for the active treatment 1 group.
  - accruals2: The number of subjects enrolled at the stage for the active treatment 2 group.
  - accruals3: The number of subjects enrolled at the stage for the control group.
  - totalAccruals: The total number of subjects enrolled at the stage.
  - endpoint: The endpoint (1 or 2) under consideration.
  - events1: The number of events at the stage for the active treatment 1 group.
  - events2: The number of events at the stage for the active treatment 2 group.
  - events3: The number of events at the stage for the control group.
  - totalEvents: The total number of events at the stage.
  - dropouts1: The number of dropouts at the stage for the active treatment 1 group.
  - dropouts2: The number of dropouts at the stage for the active treatment 2 group.
  - dropouts3: The number of dropouts at the stage for the control group.
  - totalDropouts: The total number of dropouts at the stage.
  - logRankStatistic13: The log-rank test Z-statistic comparing the active treatment 1 to the control for the endpoint.
  - logRankStatistic23: The log-rank test Z-statistic comparing the active treatment 2 to the control for the endpoint.
  - logRankStatistic12: The log-rank test Z-statistic comparing the active treatment 1 to the active treatment 2 for the endpoint.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:
  - iterationNumber: The iteration number.
  - stageNumber: The stage under consideration.
  - analysisTime: The time for the stage since trial start.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.

- stratum: The stratum for the subject.
- treatmentGroup: The treatment group (1, 2, or 3) for the subject.
- survivalTime1: The underlying survival time for event endpoint 1 for the subject.
- dropoutTime1: The underlying dropout time for event endpoint 1 for the subject.
- timeUnderObservation1: The time under observation since randomization for event endpoint 1 for the subject.
- event1: Whether the subject experienced event endpoint 1.
- dropoutEvent1: Whether the subject dropped out for endpoint 1.
- survivalTime2: The underlying survival time for event endpoint 2 for the subject.
- dropoutTime2: The underlying dropout time for event endpoint 2 for the subject.
- timeUnderObservation2: The time under observation since randomization for event endpoint 2 for the subject.
- event2: Whether the subject experienced event endpoint 2.
- dropoutEvent2: Whether the subject dropped out for endpoint 2.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# **Examples**

```
sim1 = 1rsim2e3a(
 kMax = 3,
 kMaxe1 = 2,
 allocation1 = 2,
 allocation2 = 2,
 allocation3 = 1,
 accrualTime = c(0, 8),
 accrualIntensity = c(10, 28),
 piecewiseSurvivalTime = 0,
 rho = 0,
 lambda1e1 = log(2)/12*0.60,
 lambda2e1 = log(2)/12*0.70,
 lambda3e1 = log(2)/12,
 lambda1e2 = log(2)/30*0.65,
 lambda2e2 = log(2)/30*0.75,
 lambda3e2 = log(2)/30,
 accrualDuration = 30.143,
 plannedEvents = c(186, 259, 183),
 maxNumberOfIterations = 1000,
 maxNumberOfRawDatasetsPerStage = 1,
 seed = 314159)
head(sim1$sumdata)
head(sim1$rawdata)
```

Irsim3a 249

lrsim3a

Log-rank test simulation for three arms

### **Description**

Performs simulation for three-arm group sequential trials based on weighted log-rank test. The looks are driven by the total number of events in Arm A and Arm C combined. Alternatively, the analyses can be planned to occur at specified calendar times.

### Usage

```
lrsim3a(
  kMax = NA_integer_,
  hazardRatioH013 = 1,
 hazardRatioH023 = 1,
  hazardRatioH012 = 1,
 allocation1 = 1L,
  allocation2 = 1L,
  allocation3 = 1L,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  lambda3 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  gamma3 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  plannedEvents = NA_integer_,
  plannedTime = NA_real_,
 maxNumberOfIterations = 1000L,
 maxNumberOfRawDatasetsPerStage = 0L,
  seed = NA_integer_
)
```

# **Arguments**

kMax

The maximum number of stages.

hazardRatioH013

Hazard ratio under the null hypothesis for arm 1 versus arm 3. Defaults to 1 for superiority test.

250 Irsim3a

hazardRatioH023

Hazard ratio under the null hypothesis for arm 2 versus arm 3. Defaults to 1 for superiority test.

hazardRatioH012

Hazard ratio under the null hypothesis for arm 1 versus arm 2. Defaults to 1 for superiority test.

allocation 1 Number of subjects in Arm A in a randomization block. Defaults to 1 for equal randomization.

allocation2 Number of subjects in Arm B in a randomization block. Defaults to 1 for equal randomization.

allocation3 Number of subjects in Arm C in a randomization block. Defaults to 1 for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, 1].

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for arm 1.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for arm 2.

lambda3 A vector of hazard rates for the event in each analysis time interval by stratum

for arm 3.

gamma1 The hazard rate for exponential dropout. A vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for

dropout in each analysis time interval by stratum for arm 1.

gamma2 The hazard rate for exponential dropout. A vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for

dropout in each analysis time interval by stratum for arm 2.

gamma3 The hazard rate for exponential dropout. A vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for

dropout in each analysis time interval by stratum for arm 3.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test.

Defaults to 0 for conventional log-rank test.

Irsim3a 251

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank

test. Defaults to 0 for conventional log-rank test.

plannedEvents The planned cumulative total number of events at Look 1 to Look kMax for Arms

A and C combined.

plannedTime The calendar times for the analyses. To use calendar time to plan the analyses,

plannedEvents should be missing.

maxNumberOfIterations

The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasetsPerStage

The number of raw datasets per stage to extract. Defaults to 1.

seed The seed to reproduce the simulation results. The seed from the environment

will be used if left unspecified,

### Value

#### A list with 2 components:

• sumdata: A data frame of summary data by iteration and stage:

- iterationNumber: The iteration number.
- eventsNotAchieved: Whether the target number of events is not achieved for the iteration.
- stageNumber: The stage number, covering all stages even if the trial stops at an interim look.
- analysisTime: The time for the stage since trial start.
- accruals1: The number of subjects enrolled at the stage for the active treatment 1 group.
- accruals2: The number of subjects enrolled at the stage for the active treatment 2 group.
- accruals3: The number of subjects enrolled at the stage for the control group.
- totalAccruals: The total number of subjects enrolled at the stage.
- events1: The number of events at the stage for the active treatment 1 group.
- events2: The number of events at the stage for the active treatment 2 group.
- events3: The number of events at the stage for the control group.
- totalEvents: The total number of events at the stage.
- dropouts1: The number of dropouts at the stage for the active treatment 1 group.
- dropouts2: The number of dropouts at the stage for the active treatment 2 group.
- dropouts3: The number of dropouts at the stage for the control group.
- totalDropouts: The total number of dropouts at the stage.
- logRankStatistic13: The log-rank test Z-statistic comparing the active treatment 1 to the control.
- logRankStatistic23: The log-rank test Z-statistic comparing the active treatment 2 to the control
- logRankStatistic12: The log-rank test Z-statistic comparing the active treatment 1 to the active treatment 2.
- rawdata (exists if maxNumberOfRawDatasetsPerStage is a positive integer): A data frame for subject-level data for selected replications, containing the following variables:

252 Irstat

- iterationNumber: The iteration number.
- stageNumber: The stage under consideration.
- analysisTime: The time for the stage since trial start.
- subjectId: The subject ID.
- arrivalTime: The enrollment time for the subject.
- stratum: The stratum for the subject.
- treatmentGroup: The treatment group (1, 2, or 3) for the subject.
- survivalTime: The underlying survival time for the subject.
- dropoutTime: The underlying dropout time for the subject.
- timeUnderObservation: The time under observation since randomization for the subject.
- event: Whether the subject experienced the event.
- dropoutEvent: Whether the subject dropped out.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
sim1 = lrsim3a(
 kMax = 3,
 allocation1 = 2,
 allocation2 = 2,
 allocation3 = 1,
 accrualTime = c(0, 8),
 accrualIntensity = c(10, 28),
 piecewiseSurvivalTime = 0,
 lambda1 = log(2)/12*0.60,
 lambda2 = log(2)/12*0.70,
 lambda3 = log(2)/12,
 accrualDuration = 30.143,
 plannedEvents = c(186, 259, 295),
 maxNumberOfIterations = 1000,
 maxNumberOfRawDatasetsPerStage = 1,
 seed = 314159)
head(sim1$sumdata)
head(sim1$rawdata)
```

Irstat 253

## **Description**

Obtains the number of subjects accrued, number of events, number of dropouts, and number of subjects reaching the maximum follow-up in each group, mean and variance of weighted log-rank score statistic, estimated hazard ratio from weighted Cox regression and variance of log hazard ratio estimate at given calendar times.

# Usage

```
lrstat(
  time = NA_real_,
  hazardRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  rho1 = 0,
  rho2 = 0,
  numSubintervals = 300L,
  predictTarget = 2L
)
```

## Arguments

time

A vector of calendar times at which to calculate the number of events and the mean and variance of log-rank test score statistic.

hazardRatioH0

Hazard ratio under the null hypothesis for the active treatment versus control. Defaults to 1 for superiority test.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g.,  $c(\emptyset, 3)$  breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

254 Irstat

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test.

Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank

test. Defaults to 0 for conventional log-rank test.

numSubintervals

Number of sub-intervals to approximate the mean and variance of the weighted log-rank test score statistic. Defaults to 300. Specify a larger number for better

approximation.

predictTarget The target of prediction. Set predictTarget = 1 to predict the number of events

only. Set predictTarget = 2 (default) to predict the number of events and log-rank score statistic mean and variance. Set predictTarget = 3 to predict the number of events, log-rank score statistic mean and variance, and hazard ratio

and variance of log hazard ratio.

#### Value

A data frame containing the following variables if predictTarget = 1:

- time: The analysis time since trial start.
- subjects: The number of enrolled subjects.
- nevents: The total number of events.
- nevents1: The number of events in the active treatment group.
- nevents2: The number of events in the control group.
- ndropouts: The total number of dropouts.
- ndropouts1: The number of dropouts in the active treatment group.
- ndropouts2: The number of dropouts in the control group.
- nfmax: The total number of subjects reaching maximum follow-up.

Irtest 255

- nfmax1: The number of subjects reaching maximum follow-up in the active treatment group.
- nfmax2: The number of subjects reaching maximum follow-up in the control group.

If predictTarget = 2, the following variables will also be included:

- uscore: The numerator of the log-rank test statistic.
- vscore: The variance of the log-rank score test statistic.
- logRankZ: The log-rank test statistic on the Z-scale.
- hazardRatioH0: The hazard ratio under the null hypothesis.

Furthermore, if predictTarget = 3, the following additional variables will also be included:

- HR: The average hazard ratio from weighted Cox regression.
- vlogHR: The variance of log hazard ratio.
- zlogHR: The Z-statistic for log hazard ratio.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### **Examples**

**1rtest** 

Log-rank test of survival curve difference

### Description

Obtains the log-rank test using the Fleming-Harrington family of weights.

256 Irtest

### Usage

```
lrtest(
   data,
   rep = "rep",
   stratum = "stratum",
   treat = "treat",
   time = "time",
   event = "event",
   rho1 = 0,
   rho2 = 0
)
```

## **Arguments**

data The input data frame that contains the following variables:

• rep: The replication for by-group processing.

• stratum: The stratum.

• treat: The treatment.

• time: The possibly right-censored survival time.

• event: The event indicator.

rep The name of the replication variable in the input data.

stratum The name of the stratum variable in the input data.

treat The name of the treatment variable in the input data.

time The name of the time variable in the input data.

event The name of the event variable in the input data.

rho1 The first parameter of the Fleming-Harrington family of weighted log-rank test.

Defaults to 0 for conventional log-rank test.

rho2 The second parameter of the Fleming-Harrington family of weighted log-rank

test. Defaults to 0 for conventional log-rank test.

#### Value

A data frame with the following variables:

- rep: The replication.
- uscore: The numerator of the log-rank test statistic.
- vscore: The variance of the log-rank score test statistic.
- logRankZ: The Z-statistic value.
- logRankPValue: The one-sided p-value.
- rho1: The first parameter of the Fleming-Harrington weights.
- rho2: The second parameter of the Fleming-Harrington weights.

# Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

mnOddsRatioCI 257

## **Examples**

mnOddsRatioCI

Miettinen-Nurminen score confidence interval for two-sample odds ratio

# Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample odds ratio possibly with stratification.

## Usage

```
mnOddsRatioCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

# **Arguments**

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

### **Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

### Value

A list with two components:

- data A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - n1: The sample size for the active treatment group.

258 mnRateDiffCI

- y1: The number of responses for the active treatment group.
- n2: The sample size for the control group.
- y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for odds ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
mnOddsRatioCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

mnRateDiffCI

Miettinen-Nurminen score confidence interval for two-sample rate difference

# **Description**

Obtains the Miettinen-Nurminen score confidence interval for two-sample rate difference possibly with stratification.

#### Usage

```
mnRateDiffCI(
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

### **Arguments**

tl	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

cilevel The confidence interval level.

mnRateRatioCI 259

#### **Details**

The Mantel-Haenszel weights are used for stratified samples.

### Value

A list with two components:

- data A data frame containing the input exposure and number of events for each treatment group. It has the following variables:
  - t1: The exposure for the active treatment group.
  - y1: The number of events for the active treatment group.
  - t2: The exposure for the control group.
  - y2: The number of events for the control group.
- estimates: A data frame containing the point estimate and confidence interval for rate difference. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

### **Examples**

```
mnRateDiffCI(t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

mnRateRatioCI

Miettinen-Nurminen score confidence interval for two-sample rate ratio

# **Description**

Obtains the Miettinen-Nurminen score confidence interval for two-sample rate ratio possibly with stratification.

### Usage

```
mnRateRatioCI(t1, y1, t2, y2, cilevel = 0.95)
```

260 mnRateRatioCI

### **Arguments**

t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.
cilevel	The confidence interval level.

#### **Details**

The Mantel-Haenszel weights are used for stratified samples.

#### Value

A list with two components:

- data A data frame containing the input exposure and number of events for each treatment group. It has the following variables:
  - t1: The exposure for the active treatment group.
  - y1: The number of events for the active treatment group.
  - t2: The exposure for the control group.
  - y2: The number of events for the control group.
- estimates: A data frame containing the point estimate and confidence interval for rate ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
mnRateRatioCI(t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

mnRiskDiffCI 261

jerenee	mnRiskDiffCI	Miettinen-Nurminen score confidence interval for two-sample risk difference
---------	--------------	---

# **Description**

Obtains the Miettinen-Nurminen score confidence interval for two-sample risk difference possibly with stratification.

# Usage

```
mnRiskDiffCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

# Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

# **Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

# Value

A list with two components:

- data A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:
  - n1: The sample size for the active treatment group.
  - y1: The number of responses for the active treatment group.
  - n2: The sample size for the control group.
  - y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for risk difference. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.

262 mnRiskRatioCI

```
lower: The lower limit of the confidence interval.
upper: The upper limit of the confidence interval.
cilevel: The confidence interval level.
```

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
mnRiskDiffCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

mnRiskRatioCI

Miettinen-Nurminen score confidence interval for two-sample risk ratio

# Description

Obtains the Miettinen-Nurminen score confidence interval for two-sample risk ratio possibly with stratification.

# Usage

```
mnRiskRatioCI(
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_,
  cilevel = 0.95
)
```

# Arguments

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

### **Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

mTPI2Table 263

### Value

A list with two components:

• data A data frame containing the input sample size and number of responses for each treatment group. It has the following variables:

- n1: The sample size for the active treatment group.
- y1: The number of responses for the active treatment group.
- n2: The sample size for the control group.
- y2: The number of responses for the control group.
- estimates: A data frame containing the point estimate and confidence interval for risk ratio. It has the following variables:
  - scale: The scale of treatment effect.
  - estimate: The point estimate.
  - lower: The lower limit of the confidence interval.
  - upper: The upper limit of the confidence interval.
  - cilevel: The confidence interval level.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### **Examples**

```
mnRiskRatioCI(n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

mTPI2Table

mTPI-2 decision table

# Description

Obtains the decision table for the modified toxicity probability interval-2 (mTPI-2) design.

## Usage

```
mTPI2Table(
  nMax = NA_integer_,
  pT = 0.3,
  epsilon1 = 0.05,
  epsilon2 = 0.05,
  a = 1,
  b = 1,
  pExcessTox = 0.95
)
```

264 mTPI2Table

#### **Arguments**

nMax The maximum number of subjects in a dose cohort. The target toxicity probability. Defaults to 0.3. Τα epsilon1 The lower equivalence margin from the target. Defaults to 0.05. epsilon2 The upper equivalence margin from the target. Defaults to 0.05. The prior toxicity parameter for the beta prior. а b The prior non-toxicity parameter for the beta prior. pExcessTox The threshold for excessive toxicity, i.e., if  $Prob(p > pT \mid Data) > pExcessTox$ , then the current and all higher doses will be excluded and never be used again in the remainder of the trial to avoid any other subjects receiving treatment at those doses. Defaults to 0.95.

#### Value

An S3 class mTPI2Table object with the following components:

- settings: The input settings data frame with the following variables:
  - nMax: The maximum number of subjects in a dose cohort.
  - pT: The target toxicity probability.
  - epsilon1: The lower equivalence margin from the target.
  - epsilon2: The upper equivalence margin from the target.
  - a: The prior toxicity parameter for the beta prior.
  - b: The prior non-toxicity parameter for the beta prior.
  - pExcessTox: The threshold for excessive toxicity.
- subintervals: The subintervals of equal length in the mTPI-2 design. It includes the following variables:
  - lower: The lower bound of the subinterval.
  - upper: The upper bound of the subinterval.
  - decision: The dosing decision for the subinterval.
- decisionDataFrame: The decision data frame for the mTPI-2 design. It includes the following variables:
  - n: The sample size.
  - y: The number of toxicities.
  - decision: The dosing decision.
- decisionMatrix: The decision matrix corresponding to the decision data frame.

### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

```
mTPI2Table(nMax = 18, pT = 0.3, epsilon1 = 0.05, epsilon2 = 0.05)
```

nbpower

Power for negative binomial rate ratio

# Description

Estimates the power for negative binomial rate ratio test.

# Usage

```
nbpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_,
  nullVariance = 0L
)
```

# **Arguments**

kMax The maximum number of stages. informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

rateRatioH0 Rate ratio under the null hypothesis.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, 1].

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa1	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.	
kappa2	The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.	
lambda1	The rate parameter of the negative binomial distribution for the active treatment group by stratum.	
lambda2	The rate parameter of the negative binomial distribution for the control group by stratum.	
gamma1	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.	
gamma2	The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.	
accrualDuration		
	Duration of the enrollment period.	
followupTime	Follow-up time for the last enrolled subject.	
fixedFollowup	Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.	
spendingTime	A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.	
studyDuration	Study duration for fixed follow-up design. Defaults to missing, which is to be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and followupTime.	
nullVariance	Whether to calculate the variance for log rate ratio under the null hypothesis.	

#### Value

An S3 class nbpower object with 4 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.
  - alpha: The overall significance level.
  - numberOfEvents: The total number of events.
  - numberOfDropouts: The total number of dropouts.
  - numbeOfSubjects: The total number of subjects.
  - exposure: The total exposure.
  - studyDuration: The total study duration.
  - information: The maximum information.
  - ${\color{blue}\textbf{-}}$  expected Number Of Events: The expected number of events.
  - expectedNumberOfDropouts: The expected number of dropouts.
  - expectedNumberOfSubjects: The expected number of subjects.
  - expectedExposure: The expected exposure.

- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- kMax: The number of stages.
- rateRatioH0: The rate ratio under the null hypothesis.
- rateRatio: The rate ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfEvents: The number of events.
  - numberOfDropouts: The number of dropouts.
  - numberOfSubjects: The number of subjects.
  - exposure: The exposure.
  - analysisTime: The average time since trial start.
  - efficacyRateRatio: The efficacy boundaries on the rate ratio scale.
  - futilityRateRatio: The futility boundaries on the rate ratio scale.
  - efficacyP: The efficacy boundaries on the p-value scale.
  - futilityP: The futility boundaries on the p-value scale.
  - information: The cumulative information.
  - efficacyStopping: Whether to allow efficacy stopping.
  - futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, kappa1, kappa2, lambda1, lambda2, gamma1, gamma2, spendingTime, and nullVariance.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - exposure1: The exposure by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - exposure2: The exposure by stage for the control group.

- expectedNumberOfEvents1: The expected number of events for the treatment group.
- expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
- expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
- expectedExposure1: The expected exposure for the treatment group.
- expectedNumberOfEvents2: The expected number of events for control group.
- expectedNumberOfDropouts2: The expected number of dropouts for the control group.
- expectedNumberOfSubjects2: The expected number of subjects for the control group.
- expectedExposure2: The expected exposure for the control group.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### See Also

nbstat

# Examples

```
# Example 1: Variable follow-up design
nbpower(kMax = 2, informationRates = c(0.5, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        accrualIntensity = 1956/1.25,
        stratumFraction = c(0.2, 0.8),
        kappa1 = 5, kappa2 = 5,
        lambda1 = c(0.7*0.125, 0.75*0.25),
        lambda2 = c(0.125, 0.25),
        gamma1 = 0, gamma2 = 0,
        accrualDuration = 1.25,
        followupTime = 2.75, fixedFollowup = FALSE,
        nullVariance = 1)
# Example 2: Fixed follow-up design
nbpower(kMax = 2, informationRates = c(0.5, 1),
        alpha = 0.025, typeAlphaSpending = "sfOF",
        accrualIntensity = 220/1.5,
        kappa1 = 3, kappa2 = 3,
        lambda1 = 0.5*8.4, lambda2 = 8.4,
        gamma1 = 0, gamma2 = 0,
        accrualDuration = 1.5,
        followupTime = 0.5, fixedFollowup = TRUE)
```

nbpower1s

Power for one-sample negative binomial rate

### **Description**

Estimates the power, stopping probabilities, and expected sample size in a one-group negative binomial design.

# Usage

```
nbpower1s(
  kMax = 1L,
  informationRates = NA_real_,
 efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  lambdaH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa = NA_real_,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

#### **Arguments**

```
kMax The maximum number of stages.
```

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

lambdaH0 The rate parameter of the negative binomial distribution under the null hypothe-

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

The dispersion parameter (reciprocal of the shape parameter of the gamma mixkappa ing distribution) of the negative binomial distribution by stratum.

lambda The rate parameter of the negative binomial distribution under the alternative

hypothesis by stratum.

gamma The hazard rate for exponential dropout or a vector of hazard rates for piecewise

exponential dropout by stratum. Defaults to 0 for no dropout.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and

followupTime.

#### Value

An S3 class nbpower1s object with 3 components:

• overallResults: A data frame containing the following variables:

- overallReject: The overall rejection probability.
- alpha: The overall significance level.
- numberOfEvents: The total number of events.
- numberOfDropouts: The total number of dropouts.
- numbeOfSubjects: The total number of subjects.
- exposure: The total exposure.
- studyDuration: The total study duration.
- information: The maximum information.
- expectedNumberOfEvents: The expected number of events.
- expectedNumberOfDropouts: The expected number of dropouts.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedExposure: The expected exposure.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- kMax: The number of stages.
- lambdaH0: The rate parameter of the negative binomial distribution under the null hypothesis.
- lambda: The overall rate parameter of the negative binomial distribution under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.

- futilityBounds: The futility boundaries on the Z-scale.
- rejectPerStage: The probability for efficacy stopping.
- futilityPerStage: The probability for futility stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeFutility: The cumulative probability for futility stopping.
- cumulativeAlphaSpent: The cumulative alpha spent.
- numberOfEvents: The number of events.
- numberOfDropouts: The number of dropouts.
- numberOfSubjects: The number of subjects.
- exposure: The exposure.
- analysisTime: The average time since trial start.
- efficacyRate: The efficacy boundaries on the rate scale.
- futilityRate: The futility boundaries on the rate scale.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, kappa, lambda, gamma, and spendingTime.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### See Also

nbstat

### **Examples**

```
kappa = 3, lambda = 0.5*8.4,
gamma = 0, accrualDuration = 1.5,
followupTime = 0.5, fixedFollowup = TRUE)
```

nbpowerequiv

Power for equivalence in negative binomial rate ratio

# Description

Obtains the power for equivalence in negative binomial rate ratio.

# Usage

```
nbpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  rateRatioLower = NA_real_,
  rateRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_{real}
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_,
  nullVariance = 0L
)
```

# **Arguments**

kMax The maximum number of stages. informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

rateRatioLower The lower equivalence limit of rate ratio.

rateRatioUpper The upper equivalence limit of rate ratio.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa1 The dispersion parameter (reciprocal of the shape parameter of the gamma mix-

ing distribution) for the active treatment group by stratum.

kappa2 The dispersion parameter (reciprocal of the shape parameter of the gamma mix-

ing distribution) for the control group by stratum.

lambda1 The rate parameter of the negative binomial distribution for the active treatment

group by stratum.

lambda2 The rate parameter of the negative binomial distribution for the control group by

stratum.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and  $\frac{1}{2}$ 

followupTime.

nullVariance Whether to calculate the variance for log rate ratio under the null hypothesis.

#### Value

An S3 class nbpowerequiv object with 4 components:

• overallResults: A data frame containing the following variables:

- overallReject: The overall rejection probability.
- alpha: The overall significance level.
- attainedAlphaH10: The attained significance level under H10.
- attainedAlphaH20: The attained significance level under H20.
- numberOfEvents: The total number of events.
- numberOfDropouts: The total number of dropouts.
- numbeOfSubjects: The total number of subjects.
- exposure: The total exposure.
- studyDuration: The total study duration.
- information: The maximum information.
- ${\mbox{-}}$  expected NumberOfEvents: The expected number of events.
- expectedNumberOfDropouts: The expected number of dropouts.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedExposure: The expected exposure.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- kMax: The number of stages.
- rateRatioLower: The lower equivalence limit of rate ratio.
- rateRatioUpper: The upper equivalence limit of rate ratio.
- rateRatio: The rate ratio.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.

- cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
- cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
- cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
- numberOfEvents: The number of events.
- numberOfDropouts: The number of dropouts.
- numberOfSubjects: The number of subjects.
- exposure: The exposure.
- analysisTime: The average time since trial start.
- efficacyRateRatioLower: The efficacy boundaries on the rate ratio scale for the onesided null hypothesis at the lower equivalence limit.
- efficacyRateRatioUpper: The efficacy boundaries on the rate ratio scale for the onesided null hypothesis at the upper equivalence limit.
- efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
- information: The cumulative information.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, kappa1, kappa2, lambda1, lambda2, gamma1, gamma2, accrualDuration, followupTime, fixedFollowup, spendingTime, nullVariance, and varianceRatios. The varianceRatios is a data frame with the following variables:
  - varianceRatioH10: The ratio of the variance under H10 to the variance under H1.
  - varianceRatioH20: The ratio of the variance under H20 to the variance under H1.
  - varianceRatioH12: The ratio of the variance under H10 to the variance under H20.
  - varianceRatioH21: The ratio of the variance under H20 to the variance under H10.
- byTreatmentCounts: A list containing the following counts by treatment group:
  - numberOfEvents1: The number of events by stage for the treatment group.
  - numberOfDropouts1: The number of dropouts by stage for the treatment group.
  - numberOfSubjects1: The number of subjects by stage for the treatment group.
  - exposure1: The exposure by stage for the treatment group.
  - numberOfEvents2: The number of events by stage for the control group.
  - numberOfDropouts2: The number of dropouts by stage for the control group.
  - numberOfSubjects2: The number of subjects by stage for the control group.
  - exposure2: The exposure by stage for the control group.
  - expectedNumberOfEvents1: The expected number of events for the treatment group.
  - expectedNumberOfDropouts1: The expected number of dropouts for the treatment group.
  - expectedNumberOfSubjects1: The expected number of subjects for the treatment group.
  - expectedExposure1: The expected exposure for the treatment group.
  - expectedNumberOfEvents2: The expected number of events for control group.
  - expectedNumberOfDropouts2: The expected number of dropouts for the control group.
  - expectedNumberOfSubjects2: The expected number of subjects for the control group.
  - expectedExposure2: The expected exposure for the control group.

### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## See Also

nbstat

### **Examples**

```
# Example 1: Variable follow-up design
nbpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             rateRatioLower = 2/3, rateRatioUpper = 3/2,
             accrualIntensity = 1956/1.25,
             kappa1 = 5, kappa2 = 5,
             lambda1 = 0.125, lambda2 = 0.125,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.25,
             followupTime = 2.75, fixedFollowup = FALSE,
             nullVariance = 1)
# Example 2: Fixed follow-up design
nbpowerequiv(kMax = 2, informationRates = c(0.5, 1),
             alpha = 0.05, typeAlphaSpending = "sfOF",
             rateRatioLower = 0.5, rateRatioUpper = 2,
             accrualIntensity = 220/1.5,
             stratumFraction = c(0.2, 0.8),
             kappa1 = 3, kappa2 = 3,
             lambda1 = c(8.4, 10.2),
             lambda2 = c(8.0, 11.5),
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.5,
             followupTime = 0.5, fixedFollowup = TRUE)
```

nbsamplesize

Sample size for negative binomial rate ratio

### **Description**

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a two-group negative binomial design.

# Usage

```
nbsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
```

```
alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA\_real\_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L,
  nullVariance = 0L
)
```

## **Arguments**

beta Type II error. Defaults to 0.2.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries,

"sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

#### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

#### userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

rateRatioH0 Rate ratio under the null hypothesis.

#### allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

#### accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

#### piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

#### stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

Kappa1 The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the active treatment group by stratum.

kappa2 The dispersion parameter (reciprocal of the shape parameter of the gamma mixing distribution) for the control group by stratum.

lambda1 The rate parameter of the negative binomial distribution for the active treatment group by stratum.

lambda2	The rate parameter of the negative binomial	distribution for the control group	by
---------	---	------------------------------------	----

stratum.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval The interval to search for the solution of accrualDuration, followupDuration, or

the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

nullVariance Whether to calculate the variance for log rate ratio under the null hypothesis.

#### Value

A list of two components:

- resultsUnderH1: An S3 class nbpower object under the alternative hypothesis.
- resultsUnderH0: An S3 class nbpower object under the null hypothesis.

# Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### See Also

nbpower

# **Examples**

```
followupTime = NA, fixedFollowup = FALSE)
# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up
nbsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.5, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualIntensity = 100,
             kappa1 = 5, kappa2 = 5,
             lambda1 = 0.0875, lambda2 = 0.125,
             gamma1 = 0, gamma2 = 0,
             accrualDuration = 1.25,
             followupTime = 2.25, fixedFollowup = FALSE)
# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up
nbsamplesize(beta = 0.2, kMax = 2,
             informationRates = c(0.5, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             accrualIntensity = 1667,
             stratumFraction = c(0.2, 0.8),
             kappa1 = 5, kappa2 = 5,
             lambda1 = c(0.7*0.125, 0.75*0.25),
             lambda2 = c(0.125, 0.25),
             gamma1 = 0, gamma2 = 0,
             accrualDuration = NA,
             followupTime = 0.5, fixedFollowup = TRUE)
```

nbsamplesize1s

Sample size for one-sample negative binomial rate

# Description

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group negative binomial design.

# Usage

```
nbsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
```

```
criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
 userBetaSpending = NA_real_,
  lambdaH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa = NA_real_,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

# Arguments

beta Type II error. Defaults to 0.2.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

lambdaH0 The rate parameter of the negative binomial distribution under the null hypothe-

sis.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

The dispersion parameter (reciprocal of the shape parameter of the gamma mixkappa

ing distribution) of the negative binomial distribution by stratum.

lambda The rate parameter of the negative binomial distribution under the alternative

hypothesis by stratum.

The hazard rate for exponential dropout or a vector of hazard rates for piecewise gamma

exponential dropout by stratum. Defaults to 0 for no dropout.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval The interval to search for the solution of accrualDuration, followupDuration, or

the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

#### Value

A list of two components:

- resultsUnderH1: An S3 class nbpower1s object under the alternative hypothesis.
- resultsUnderH0: An S3 class nbpower1s object under the null hypothesis.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

### See Also

nbpower1s

# **Examples**

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up
nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               lambdaH0 = 0.125, accrualIntensity = 500,
               stratumFraction = c(0.2, 0.8),
               kappa = c(3, 5), lambda = c(0.0875, 0.085),
               gamma = 0, accrualDuration = 1.25,
               followupTime = NA, fixedFollowup = FALSE)
# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up
nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               lambdaH0 = 0.125, accrualIntensity = 100,
               kappa = 5, lambda = 0.0875,
               gamma = 0, accrualDuration = 1.25,
               followupTime = 2.25, fixedFollowup = FALSE)
# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up
nbsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.5, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
               lambdaH0 = 8.4, accrualIntensity = 40,
```

286 nbsamplesizeequiv

```
kappa = 3, lambda = 4.2,
gamma = 0, accrualDuration = NA,
followupTime = 0.5, fixedFollowup = TRUE)
```

nbsamplesizeequiv

Sample size for equivalence in negative binomial rate ratio

### **Description**

Obtains the sample size for equivalence in negative binomial rate ratio.

## Usage

```
nbsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  rateRatioLower = NA_real_,
  rateRatioUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L,
  nullVariance = 0L
)
```

nbsamplesizeequiv 287

#### **Arguments**

beta The type II error.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

rateRatioLower The lower equivalence limit of rate ratio.

rateRatioUpper The upper equivalence limit of rate ratio.

 $\hbox{allocation} \hbox{RatioPlanned}$ 

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

randomization

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa1 The dispersion parameter (reciprocal of the shape parameter of the gamma mix-

ing distribution) for the active treatment group by stratum.

kappa2 The dispersion parameter (reciprocal of the shape parameter of the gamma mix-

ing distribution) for the control group by stratum.

lambda1 The rate parameter of the negative binomial distribution for the active treatment

group by stratum.

lambda2 The rate parameter of the negative binomial distribution for the control group by

stratum.

288 nbsamplesizeequiv

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

interval The interval to search for the solution of accrualDuration, followupDuration, or

the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

nullVariance Whether to calculate the variance for log rate ratio under the null hypothesis.

#### Value

An S3 class nbpowerequiv object

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# See Also

nbpowerequiv

# **Examples**

nbstat

Negative binomial rate ratio

### **Description**

Obtains the number of subjects accrued, number of events, number of dropouts, number of subjects reaching the maximum follow-up, total exposure, and variance for log rate in each group, rate ratio, variance, and Wald test statistic of log rate ratio at given calendar times.

## Usage

```
nbstat(
  time = NA_real_,
  rateRatioH0 = 1,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  kappa1 = NA_real_,
  kappa2 = NA_real_,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  nullVariance = 0L
)
```

### **Arguments**

time A vector of calendar times for data cut. rateRatioH0 Rate ratio under the null hypothesis.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

kappa1 The dispersion parameter (reciprocal of the shape parameter of the gamma mix-

ing distribution) for the active treatment group by stratum.

kappa2 The dispersion parameter (reciprocal of the shape parameter of the gamma mix-

ing distribution) for the control group by stratum.

lambda1 The rate parameter of the negative binomial distribution for the active treatment

group by stratum.

lambda2 The rate parameter of the negative binomial distribution for the control group by

stratum.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

nullVariance Whether to calculate the variance for log rate ratio under the null hypothesis.

#### **Details**

The probability mass function for a negative binomial distribution with dispersion parameter  $\kappa_i$  and rate parameter  $\lambda_i$  is given by

$$P(Y_{ij} = y) = \frac{\Gamma(y + 1/\kappa_i)}{\Gamma(1/\kappa_i)y!} \left(\frac{1}{1 + \kappa_i \lambda_i t_{ij}}\right)^{1/\kappa_i} \left(\frac{\kappa_i \lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right)^y,$$

where  $Y_{ij}$  is the event count for subject j in treatment group i, and  $t_{ij}$  is the exposure time for the subject. If  $\kappa_i = 0$ , the negative binomial distribution reduces to the Poisson distribution.

For treatment group i, let  $\beta_i = \log(\lambda_i)$ . The likelihood for  $\{(\kappa_i, \beta_i) : i = 1, 2\}$  can be written as

$$l = \sum_{i=1}^{2} \sum_{j=1}^{n_i} \{ \log \Gamma(y_{ij} + 1/\kappa_i) - \log \Gamma(1/\kappa_i) + y_{ij} (\log(\kappa_i) + \beta_i) - (y_{ij} + 1/\kappa_i) \log(1 + \kappa_i \exp(\beta_i) t_{ij}) \}.$$

It follows that

$$\frac{\partial l}{\partial \beta_i} = \sum_{j=1}^{n_i} \left\{ y_{ij} - (y_{ij} + 1/\kappa_i) \frac{\kappa_i \exp(\beta_i) t_{ij}}{1 + \kappa_i \exp(\beta_i) t_{ij}} \right\},\,$$

and

$$-\frac{\partial^2 l}{\partial \beta_i^2} = \sum_{i=1}^{n_i} (y_{ij} + 1/\kappa_i) \frac{\kappa_i \lambda_i t_{ij}}{(1 + \kappa_i \lambda_i t_{ij})^2}.$$

The Fisher information for  $\beta_i$  is

$$E\left(-\frac{\partial^2 l}{\partial \beta_i^2}\right) = n_i E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right).$$

In addition, we can show that

$$E\left(-\frac{\partial^2 l}{\partial \beta_i \partial \kappa_i}\right) = 0.$$

Therefore, the variance of  $\hat{\beta}_i$  is

$$Var(\hat{\beta}_i) = \frac{1}{n_i} \left\{ E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right) \right\}^{-1}.$$

To evaluate the integral, we need to obtain the distribution of the exposure time,

$$t_{ij} = \min(\tau - W_{ij}, C_{ij}, T_{fmax}),$$

where  $\tau$  denotes the calendar time since trial start,  $W_{ij}$  denotes the enrollment time for subject j in treatment group i,  $C_{ij}$  denotes the time to dropout after enrollment for subject j in treatment group i, and  $T_{fmax}$  denotes the maximum follow-up time for all subjects. Therefore,

$$P(t_{ij} \ge t) = P(W_{ij} \le \tau - t)P(C_{ij} \ge t)I(t \le T_{fmax}).$$

Let H denote the distribution function of the enrollment time, and  $G_i$  denote the survival function of the dropout time for treatment group i. By the change of variables, we have

$$E\left(\frac{\lambda_i t_{ij}}{1 + \kappa_i \lambda_i t_{ij}}\right) = \int_0^{\tau \wedge T_{fmax}} \frac{\lambda_i}{(1 + \kappa_i \lambda_i t)^2} H(\tau - t) G_i(t) dt.$$

A numerical integration algorithm for a univariate function can be used to evaluate the above integral.

For the restricted maximum likelihood (reml) estimate of  $(\beta_1, \beta_2)$  subject to the constraint that  $\beta_1 - \beta_2 = \Delta$ , we express the log-likelihood in terms of  $(\beta_2, \Delta, \kappa_1, \kappa_2)$ , and takes the derivative of the log-likelihood function with respect to  $\beta_2$ . The resulting score equation has asymptotic limit

$$E\left(\frac{\partial l}{\partial \beta_2}\right) = s_1 + s_2,$$

where

$$s_1 = nrE\left\{\lambda 1_1 t_{1j} - \left(\lambda_1 t_{1j} + \frac{1}{\kappa_1}\right) \frac{\kappa_1 e^{\tilde{\beta}_2 + \Delta} t_{1j}}{1 + \kappa_1 e^{\tilde{\beta}_2 + \Delta} t_{1j}}\right\},\,$$

and

$$s_2 = n(1 - r)E\left\{\lambda_2 t_{2j} - \left(\lambda_2 t_{2j} + \frac{1}{\kappa_2}\right) \frac{\kappa_2 e^{\tilde{\beta}_2} t_{2j}}{1 + \kappa_2 e^{\tilde{\beta}_2} t_{2j}}\right\}.$$

Here r is the randomization probability for the active treatment group. The asymptotic limit of the reml of  $\beta_2$  is the solution  $\tilde{\beta}_2$  to  $E\left(\frac{\partial l}{\partial \beta_2}\right)=0$ .

#### Value

A list with two components:

- resultsUnderH1: A data frame containing the following variables:
  - time: The analysis time since trial start.
  - subjects: The number of enrolled subjects.
  - nevents: The total number of events.
  - nevents1: The number of events in the active treatment group.
  - nevents2: The number of events in the control group.
  - ndropouts: The total number of dropouts.
  - ndropouts1: The number of dropouts in the active treatment group.
  - ndropouts2: The number of dropouts in the control group.
  - nfmax: The total number of subjects reaching maximum follow-up.
  - nfmax1: The number of subjects reaching maximum follow-up in the active treatment group.
  - nfmax2: The number of subjects reaching maximum follow-up in the control group.
  - exposure: The total exposure time.
  - exposure1: The exposure time for the active treatment group.
  - exposure2: The exposure time for the control group.
  - rateRatio: The rate ratio of the active treatment group versus the control group.
  - vlogRate1: The variance for the log rate parameter for the active treatment group.
  - vlogRate2: The variance for the log rate parameter for the control group.
  - vlogRR: The variance of log rate ratio.
  - information: The information of log rate ratio.
  - zlogRR: The Z-statistic for log rate ratio.
- resultsUnderH0 when nullVariance = TRUE: A data frame with the following variables:
  - time: The analysis time since trial start.
  - lambda1H0: The restricted maximum likelihood estimate of the event rate for the active treatment group.
  - lambda2H0: The restricted maximum likelihood estimate of the event rate for the control group.
  - rateRatioH0: The rate ratio under H0.

 vlogRate1H0: The variance for the log rate parameter for the active treatment group under H0.

- vlogRate2H0: The variance for the log rate parameter for the control group under H0.
- vlogRRH0: The variance of log rate ratio under H0.
- informationH0: The information of log rate ratio under H0.
- zlogRRH0: The Z-statistic for log rate ratio with variance evaluated under H0.
- varianceRatio: The ratio of the variance under H0 versus the variance under H1.
- lambda1: The true event rate for the active treatment group.
- lambda2: The true event rate for the control group.
- rateRatio: The true rate ratio.
- resultsUnderH0 when nullVariance = FALSE: A data frame with the following variables:
  - time: The analysis time since trial start.
  - rateRatioH0: The rate ratio under H0.
  - varianceRatio: Equal to 1.
  - lambda1: The true event rate for the active treatment group.
  - lambda2: The true event rate for the control group.
  - rateRatio: The true rate ratio.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

```
# Example 1: Variable follow-up design
nbstat(time = c(1, 1.25, 2, 3, 4),
       accrualIntensity = 1956/1.25,
       kappa1 = 5,
       kappa2 = 5,
       lambda1 = 0.7*0.125,
       lambda2 = 0.125,
       gamma1 = 0,
       gamma2 = 0,
       accrualDuration = 1.25,
       followupTime = 2.75)
# Example 2: Fixed follow-up design
nbstat(time = c(0.5, 1, 1.5, 2),
       accrualIntensity = 220/1.5,
       stratumFraction = c(0.2, 0.8),
       kappa1 = 3,
       kappa2 = 3,
       lambda1 = c(0.5*8.4, 0.6*10.5),
       lambda2 = c(8.4, 10.5),
       gamma1 = 0,
       gamma2 = 0,
```

294 phregr

```
accrualDuration = 1.5,
followupTime = 0.5,
fixedFollowup = 1,
nullVariance = 1)
```

phregr

Proportional hazards regression model

## **Description**

Obtains the hazard ratio estimates from the proportional hazards regression model with right censored or counting process data.

## Usage

```
phregr(
  data,
  rep = "rep",
  stratum = "stratum",
  time = "time",
  time2 = "time2",
  event = "event",
  covariates = "treat",
  weight = "weight",
  id = "id",
  ties = "efron",
  robust = 0L
)
```

#### **Arguments**

data

The input data frame that contains the following variables:

- rep: The replication for by-group processing.
- stratum: The stratum.
- time: The follow-up time for right censored data, or the left end of each interval for counting process data.
- time2: The right end of each interval for counting process data only. Intervals are assumed to be open on the left and closed on the right, and event indicates whether an event occurred at the right end of each interval.
- event: The event indicator, normally 1=event, 0=no event.
- covariates: The values of baseline covariates (and time-dependent covariates in each interval for counting process data). This is the full-rank design matrix for the Cox model, assuming that factor variables have already been expanded into dummy variables.
- weight: The weight for each observation.

phregr 295

 id: The optional subject ID for counting process data with time-dependent covariates.

rep The name of the replication variable in the input data.

stratum The name of the stratum variable in the input data.

time The name of the time variable or the left end of each interval for counting process

data in the input data.

time2 The name of the right end of each interval for counting process data in the input

data.

event The name of the event variable in the input data.

covariates The vector of names of baseline and time-dependent covariates in the input data.

weight The name of the weighting variable in the input data.

id The name of the id variable in the input data.

ties The method for handling ties with options including "breslow" and "efron" (de-

fault).

robust Whether a robust sandwich variance estimate should be computed. The default

is TRUE if there are fractional weights or there is at least 1 id with >1 event. In the presence of the id variable, the score residual will be aggregated for each id

when computing the robust sandwich variance estimate.

#### Value

A list with the following components:

- sumstat: The data frame of summary statistics of model fit with the following variables:
  - rep: The replication.
  - n: The number of observations.
  - nevents: The number of events.
  - loglik0: The log-likelihood under null.
  - loglik1: The maximum log-likelihood.
  - scoretest: The score test statistic.
- parest: The data frame of parameter estimates with the following variables:
  - rep: The replication.
  - param: The name of the covariate for the parameter estimate.
  - beta: The log hazard ratio estimate.
  - sebeta: The standard error of log hazard ratio estimate.
  - rsebeta: The robust standard error of log hazard ratio estimate if robust variance is requested.
  - z: The Wald test statistic for log hazard ratio. The rsebeta will be used if robust variance is requested.
  - hazardRatio: The hazard ratio estimate.
  - vbeta: The covariance matrix for parameter estimates.
  - rvbeta: The robust covariance matrix for parameter estimates if robust variance is requested.

296 ptpwexp

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### **Examples**

ptpwexp

Distribution function of truncated piecewise exponential distribution

#### **Description**

Obtains the probability of a truncated piecewise exponential distribution.

### Usage

```
ptpwexp(
   q,
   piecewiseSurvivalTime = 0,
   lambda = 0.0578,
   lowerBound = 0,
   lower.tail = TRUE,
   log.p = FALSE
)
```

#### **Arguments**

```
q The vector of quantiles.
```

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda A vector of hazard rates for the event. One for each analysis time interval.

lowerBound The left truncation time point for the survival time. Defaults to 0 for no trunca-

tion.

lower.tail Logical; if TRUE (default), probabilities are  $P(X \le x)$ , otherwise, P(X > x).

log.p Logical; if TRUE, probabilities p are given as log(p).

pwexpcuts 297

#### Value

The probability p such that  $P(X > q \mid X > lowerBound) = 1 - p$ .

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

```
ptpwexp(q = c(8, 18), piecewiseSurvivalTime = c(0, 6, 9, 15), lambda = c(0.025, 0.04, 0.015, 0.007))
```

pwexpcuts

Piecewise exponential approximation to a survival distribution

## **Description**

Obtains the piecewise exponential distribution that approximates a survival distribution.

#### Usage

```
pwexpcuts(S, ...)
```

#### **Arguments**

- S The survival function of a univariate survival time.
- ... Additional arguments to be passed to S.

#### Value

A list with three components:

- piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf).
- lambda: A vector of hazard rates for the event. One for each analysis time interval.
- loglik: The sequence of the asymptotic limit of the piecewise exponential log-likelihood for an increasing number of change points.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

298 pwexploglik

### **Examples**

pwexploglik

Profile log-likelihood function for the change points in piecewise exponential approximation

# Description

Obtains the profile log-likelihood function for the change points in the piecewise exponential approximation to a survival function.

### Usage

```
pwexploglik(tau, S, ...)
```

#### **Arguments**

tau The numeric vector of change points.

S The survival function of a univariate survival time.

... Additional arguments to be passed to S.

### Value

A list with the following three components:

- piecewiseSurvivalTime: A vector that specifies the starting time of piecewise exponential survival time intervals.
- lambda: A vector of hazard rates for the event. One for each analysis time interval.
- loglik: The value of the profile log-likelihood.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
pwexploglik(tau = c(0.5, 1.2, 2.8), pweibull,
shape = 1.37, scale = 1/0.818, lower.tail = FALSE)
```

qtpwexp 299

qtpwexp

Quantile function of truncated piecewise exponential distribution

#### **Description**

Obtains the quantile of a truncated piecewise exponential distribution.

## Usage

```
qtpwexp(
   p,
   piecewiseSurvivalTime = 0,
   lambda = 0.0578,
   lowerBound = 0,
   lower.tail = TRUE,
   log.p = FALSE
)
```

## **Arguments**

The vector of probabilities.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda A vector of hazard rates for the event. One for each analysis time interval.

lowerBound The left truncation time point for the survival time. Defaults to 0 for no trunca-

tion.

lower.tail Logical; if TRUE (default), probabilities are  $P(X \le x)$ , otherwise, P(X > x).

log.p Logical; if TRUE, probabilities p are given as log(p).

#### Value

The quantile q such that  $P(X > q \mid X > lowerBound) = 1 - p$ .

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
qtpwexp(p = c(0.205, 0.317), piecewiseSurvivalTime = c(0, 6, 9, 15), lambda = c(0.025, 0.04, 0.015, 0.007))
```

300 remlOddsRatio

rawdata

A simulated time-to-event data set with 10 replications

## **Description**

A simulated data set with stratification and delayed treatment effect:

```
iterationNumber The iteration number
arrivalTime The enrollment time for the subject
stratum The stratum for the subject
treatmentGroup The treatment group for the subject
timeUnderObservation The time under observation since randomization
event Whether the subject experienced the event
dropoutEvent Whether the subject dropped out
```

## Usage

rawdata

# **Format**

An object of class data. frame with 4910 rows and 7 columns.

remlOddsRatio

REML estimates of individual proportions with specified odds ratio

# Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified odds ratio.

#### Usage

```
remlOddsRatio(
  oddsRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

remlRateDiff 301

## **Arguments**

oddsRatioH0	The specified odds ratio.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

#### Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
remlOddsRatio(oddsRatioH0 = 1.25, n1 = 10, y1 = 4, n2 = 20, y2 = 2)
```

remlRateDiff

REML estimates of individual rates with specified rate difference

# Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified rate difference.

## Usage

```
remlRateDiff(
  rateDiffH0 = 0,
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_
```

rateDiffH0	The specified rate difference.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

302 remlRateRatio

## Value

A vector of the restricted maximum likelihood estimates of the incidence rates for the two treatment groups.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

```
remlRateDiff(rateDiffH0 = 0.1, t1 = 10, y1 = 4, t2 = 20, y2 = 2)
```

remlRateRatio

REML estimates of individual rates with specified rate ratio

# Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified rate ratio.

### Usage

```
remlRateRatio(
  rateRatioH0 = 1,
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_
```

# Arguments

rateRatioH0	The specified rate ratio.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

#### Value

A vector of the restricted maximum likelihood estimates of the incidence rates for the two treatment groups.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

remlRiskDiff 303

## **Examples**

```
remlRateRatio(rateRatioH0 = 1.1, t1 = 10, y1 = 4, t2 = 20, y2 = 2)
```

 $\begin{tabular}{ll} \it REML \ estimates \ of \ individual \ proportions \ with \ specified \ risk \ difference \\ \hline \end{tabular}$ 

# Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified risk difference.

# Usage

```
remlRiskDiff(
  riskDiffH0 = 0,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
```

## **Arguments**

riskDiffH0	The specified risk difference.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

#### Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

```
remlRiskDiff(riskDiffH0 = 0.1, n1 = 10, y1 = 4, n2 = 20, y2 = 0)
```

304 remlRiskRatio

remlRiskRatio

REML estimates of individual proportions with specified risk ratio

# Description

Obtains the restricted maximum likelihood estimates of individual proportions with specified risk ratio

## Usage

```
remlRiskRatio(
  riskRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
```

## **Arguments**

riskRatioH0	The specified risk ratio.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

#### Value

A vector of the restricted maximum likelihood estimates of the response probabilities for the two treatment groups.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
remlRiskRatio(riskRatioH0 = 1.2, \ n1 = 10, \ y1 = 4, \ n2 = 20, \ y2 = 2)
```

repeatedPValue 305

repeatedPValue

Repeated p-values for group sequential design

#### **Description**

Obtains the repeated p-values for a group sequential design.

## Usage

```
repeatedPValue(
  kMax,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA,
  maxInformation = 1,
  p,
  information,
  spendingTime = NULL
)
```

## **Arguments**

kMax

The maximum number of stages.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT",

rho for "sfKD", and gamma for "sfHSD".

maxInformation The target maximum information. Defaults to 1, in which case, information

represents informationRates.

p The raw p-values at look 1 to look k. It can be a matrix with k columns for k <=

kMax.

information The observed information by look. It can be a matrix with k columns.

spendingTime The error spending time at each analysis, must be increasing and less than or

equal to 1. Defaults to NULL, in which case, it is the same as informationRates derived from information and maxInformation. It can be a matrix with  ${\sf k}$ 

columns.

#### Value

The repeated p-values at look 1 to look k.

306 riskDiffExactCI

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## **Examples**

riskDiffExactCI

Exact unconditional confidence interval for risk difference

## **Description**

Obtains the exact unconditional confidence interval for risk difference based on the standardized score statistic.

## Usage

```
riskDiffExactCI(
  n1 = NA_integer_,
  y1 = NA_integer_,
  n2 = NA_integer_,
  y2 = NA_integer_,
  cilevel = 0.95
)
```

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

riskDiffExactPValue 307

# Value

A data frame containing the following variables:

- scale: The scale of treatment effect.
- estimate: The point estimate.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# Examples

```
riskDiffExactCI(n1 = 68, y1 = 2, n2 = 65, y2 = 1, cilevel = 0.95)
```

riskDiffExactPValue

P-value for exact unconditional test of risk difference

# Description

Obtains the p-value for exact unconditional test of risk difference.

## Usage

```
riskDiffExactPValue(
  riskDiffH0 = 0,
  directionUpper = 1L,
  n1 = NA_integer_,
  y1 = NA_integer_,
  n2 = NA_integer_,
  y2 = NA_integer_
```

riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
${\it direction Upper}$	Whether larger values represent better responses.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

308 riskRatioExactCI

#### Value

A data frame containing the following variables:

- riskDiffH0: The risk difference under the null hypothesis.
- directionUpper: Whether larger values represent better responses.
- riskDiff: The observed risk difference.
- zstat: The observed value of the Z test statistic.
- pvalue: The one-sided p-value for the unconditional exact test.
- pi2star: The value of pi2 that yields the p-value.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### **Examples**

```
riskDiffExactPValue(riskDiffH0 = 0, directionUpper = 1,

n1 = 68, y1 = 2, n2 = 65, y2 = 1)
```

riskRatioExactCI

Exact unconditional confidence interval for risk ratio

#### **Description**

Obtains the exact unconditional confidence interval for risk ratio based on the standardized score statistic.

# Usage

```
riskRatioExactCI(
  n1 = NA_integer_,
  y1 = NA_integer_,
  n2 = NA_integer_,
  y2 = NA_integer_,
  cilevel = 0.95
)
```

n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.
cilevel	The confidence interval level.

riskRatioExactPValue 309

## Value

A data frame containing the following variables:

- scale: The scale of treatment effect.
- estimate: The point estimate.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

```
riskRatioExactCI(n1 = 68, y1 = 2, n2 = 65, y2 = 1, cilevel = 0.95)
```

# Description

Obtains the p-value for exact unconditional test of risk ratio.

## Usage

```
riskRatioExactPValue(
  riskRatioH0 = 1,
  directionUpper = 1L,
  n1 = NA_integer_,
  y1 = NA_integer_,
  n2 = NA_integer_,
  y2 = NA_integer_
```

riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
${\it direction Upper}$	Whether larger values represent better responses.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

310 rmdiff

## Value

A data frame containing the following variables:

- riskRatioH0: The risk ratio under the null hypothesis.
- directionUpper: Whether larger values represent better responses.
- riskRatio: The observed risk ratio.
- zstat: The observed value of the Z test statistic.
- pvalue: The one-sided p-value for the unconditional exact test.
- pi2star: The value of pi2 that yields the p-value.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

```
riskRatioExactPValue(riskRatioH0 = 1, directionUpper = 1, n1 = 68, y1 = 2, n2 = 65, y2 = 1)
```

rmdiff

Estimate of restricted mean survival time difference

# Description

Obtains the estimate of restricted mean survival time difference between two treatment groups.

## Usage

```
rmdiff(
  data,
  rep = "rep",
  stratum = "stratum",
  treat = "treat",
  time = "time",
  event = "event",
  milestone = NA_real_,
  rmstDiffH0 = 0,
  confint = 0.95,
  biascorrection = 0L
)
```

rmdiff 311

### **Arguments**

data The input data frame that contains the following variables:

• rep: The replication for by-group processing.

• stratum: The stratum.

• treat: The treatment.

• time: The possibly right-censored survival time.

• event: The event indicator.

rep The name of the replication variable in the input data.

stratum The name of the stratum variable in the input data.

treat The name of the treatment variable in the input data.

time The name of the time variable in the input data.

event The name of the event variable in the input data.

milestone The milestone time at which to calculate the restricted mean survival time.

rmstDiffH0 The difference in restricted mean survival times under the null hypothesis. De-

faults to 0 for superiority test.

confint The level of the two-sided confidence interval for the difference in restricted

mean survival times. Defaults to 0.95.

biascorrection Whether to apply bias correction for the variance estimate of individual re-

stricted mean survival times. Defaults to no bias correction.

## Value

A data frame with the following variables:

- rep: The replication number.
- milestone: The milestone time relative to randomization.
- rmstDiffH0: The difference in restricted mean survival times under the null hypothesis.
- rmst1: The estimated restricted mean survival time for the treatment group.
- rmst2: The estimated restricted mean survival time for the control group.
- rmstDiff: The estimated difference in restricted mean survival times.
- vrmst1: The variance for rmst1.
- vrmst2: The variance for rmst2.
- vrmstDiff: The variance for rmstDiff.
- rmstDiffZ: The Z-statistic value.
- rmstDiffPValue: The one-sided p-value.
- lower: The lower bound of confidence interval.
- upper: The upper bound of confidence interval.
- confint: The level of confidence interval.
- biascorrection: Whether to apply bias correction for the variance estimate of individual restricted mean survival times.

312 rmest

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## Examples

rmest

Estimate of restricted mean survival time

## **Description**

Obtains the estimate of restricted means survival time for each stratum.

### Usage

```
rmest(
  data,
  rep = "rep",
  stratum = "stratum",
  time = "time",
  event = "event",
  milestone = NA_real_,
  confint = 0.95,
  biascorrection = 0L
)
```

# Arguments

data The input data frame that contains the following variables:

- rep: The replication for by-group processing.
- stratum: The stratum.
- time: The possibly right-censored survival time.
- event: The event indicator.

rep The name of the replication variable in the input data.

stratum The name of the stratum variable in the input data.

time The name of the time variable in the input data.

event The name of the event variable in the input data.

milestone The milestone time at which to calculate the restricted mean survival time.

confint The level of the two-sided confidence interval for the survival probabilities. De-

faults to 0.95.

biascorrection Whether to apply bias correction for the variance estimate. Defaults to no bias

correction.

## Value

A data frame with the following variables:

- rep: The replication.
- stratum: The stratum variable.
- size: The number of subjects in the stratum.
- milestone: The milestone time relative to randomization.
- rmst: The estimate of restricted mean survival time.
- stderr: The standard error of the estimated rmst.
- lower: The lower bound of confidence interval if requested.
- upper: The upper bound of confidence interval if requested.
- confint: The level of confidence interval if requested.
- biascorrection: Whether to apply bias correction for the variance estimate.

## Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

## **Examples**

rmpower

Power for difference in restricted mean survival times

## **Description**

Estimates the power for testing the difference in restricted mean survival times in a two-sample survival design.

## Usage

```
rmpower(
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
 milestone = NA_real_,
  rmstDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

### Arguments

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming

boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

#### userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

### typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

#### parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

milestone The milestone time at which to calculate the restricted mean survival time.

rmstDiffH0 The difference in restricted mean survival times under the null hypothesis. Defaults to 0 for superiority test.

## allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

#### accrualIntensity

A vector of accrual intensities. One for each accrual time interval. piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

### stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piecewise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and  $\frac{1}{2}$ 

followupTime.

#### Value

An S3 class rmpower object with 3 components:

• overallResults: A data frame containing the following variables:

- overallReject: The overall rejection probability.
- alpha: The overall significance level.
- drift: The drift parameter, equal to (rmstDiff rmstDiffH0)\*sqrt(information).
- inflationFactor: The inflation factor (relative to the fixed design).
- numbeOfSubjects: The total number of subjects.
- studyDuration: The total study duration.
- information: The maximum information.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- kMax: The number of stages.
- milestone: The milestone time relative to randomization.
- rmstDiffH0: The difference in restricted mean survival times under the null hypothesis.
- rmst1: The restricted mean survival time for the treatment group.
- rmst2: The restricted mean survival time for the control group.
- rmstDiff: The difference in restricted mean survival times, equal to rmst1 rmst2.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.

- futilityPerStage: The probability for futility stopping.
- cumulativeRejection: The cumulative probability for efficacy stopping.
- cumulativeFutility: The cumulative probability for futility stopping.
- cumulativeAlphaSpent: The cumulative alpha spent.
- numberOfSubjects: The number of subjects.
- analysisTime: The average time since trial start.
- efficacyRmstDiff: The efficacy boundaries on the restricted mean survival time difference scale.
- futilityRmstDiff: The futility boundaries on the restricted mean survival time difference scale.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### **Examples**

```
# Piecewise accrual, piecewise exponential survival, and 5% dropout by
# the end of 1 year.

rmpower(kMax = 2, informationRates = c(0.8, 1),
    alpha = 0.025, typeAlphaSpending = "sfOF",
    milestone = 18,
    allocationRatioPlanned = 1, accrualTime = seq(0, 8),
    accrualIntensity = 100/9*seq(1, 9),
    piecewiseSurvivalTime = c(0, 6),
    stratumFraction = c(0.2, 0.8),
    lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
    lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
    gamma1 = -log(1-0.05)/12,
    gamma2 = -log(1-0.05)/12, accrualDuration = 22,
    followupTime = 18, fixedFollowup = FALSE)
```

318 rmpower1s

rmpower1s

Power for one-sample restricted mean survival time

## **Description**

Estimates the power, stopping probabilities, and expected sample size in a one-group survival design.

## Usage

```
rmpower1s(
  kMax = 1L,
  informationRates = NA_real_,
 efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
 milestone = NA_real_,
  rmstH0 = NA_real_,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
 piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

#### **Arguments**

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

rmpower1s 319

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds

are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and

gamma for "sfHSD".

milestone The milestone time at which to calculate the restricted mean survival time.

rmstH0 The restricted mean survival time under the null hypothesis.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda A vector of hazard rates for the event in each analysis time interval by stratum

under the alternative hypothesis.

The hazard rate for exponential dropout or a vector of hazard rates for piecewise gamma

exponential dropout. Defaults to 0 for no dropout.

320 rmpower1s

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and

followupTime.

#### Value

An S3 class rmpower1s object with 3 components:

• overallResults: A data frame containing the following variables:

- overallReject: The overall rejection probability.
- alpha: The overall significance level.
- drift: The drift parameter, equal to (rmst rmstH0)\*sqrt(information).
- inflationFactor: The inflation factor (relative to the fixed design).
- numbeOfSubjects: The total number of subjects.
- studyDuration: The total study duration.
- information: The maximum information.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- kMax: The number of stages.
- milestone: The milestone time relative to randomization.
- rmstH0: The restricted mean survival time under the null hypothesis.
- rmst: The restricted mean survival time under the alternative hypothesis.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale.
  - futilityBounds: The futility boundaries on the Z-scale.
  - rejectPerStage: The probability for efficacy stopping.
  - futilityPerStage: The probability for futility stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeFutility: The cumulative probability for futility stopping.
  - cumulativeAlphaSpent: The cumulative alpha spent.
  - numberOfSubjects: The number of subjects.

- analysisTime: The average time since trial start.
- efficacyRmst: The efficacy boundaries on the restricted mean survival time.
- futilityRmst: The futility boundaries on the restricted mean survival time.
- efficacyP: The efficacy boundaries on the p-value scale.
- futilityP: The futility boundaries on the p-value scale.
- information: The cumulative information.
- efficacyStopping: Whether to allow efficacy stopping.
- futilityStopping: Whether to allow futility stopping.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, typeBetaSpending, parameterBetaSpending, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda, gamma, and spendingTime.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### See Also

rmstat

# **Examples**

rmpowerequiv

Power for equivalence in restricted mean survival time difference

## Description

Obtains the power for equivalence in restricted mean survival time difference.

#### Usage

```
rmpowerequiv(
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
 milestone = NA_real_,
  rmstDiffLower = NA_real_,
  rmstDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  spendingTime = NA_real_,
  studyDuration = NA_real_
)
```

#### **Arguments**

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05. typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

milestone The milestone time at which to calculate the restricted mean survival time.

rmstDiffLower The lower equivalence limit of restricted mean survival time difference.

The upper equivalence limit of restricted mean survival time difference.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime

A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g.,  $c(\emptyset, 3)$  breaks the time axis into 2 accrual intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

studyDuration Study duration for fixed follow-up design. Defaults to missing, which is to

be replaced with the sum of accrualDuration and followupTime. If provided, the value is allowed to be less than the sum of accrualDuration and  $\,$ 

followupTime.

#### Value

An S3 class rmpowerequiv object with 3 components:

- overallResults: A data frame containing the following variables:
  - overallReject: The overall rejection probability.

- alpha: The overall significance level.
- attainedAlphaH10: The attained significance level under H10.
- attainedAlphaH20: The attained significance level under H20.
- numbeOfSubjects: The total number of subjects.
- studyDuration: The total study duration.
- information: The maximum information.
- expectedNumberOfSubjects: The expected number of subjects.
- expectedStudyDuration: The expected study duration.
- expectedInformation: The expected information.
- kMax: The number of stages.
- milestone: The milestone time relative to randomization.
- rmstDiffLower: The lower equivalence limit of restricted mean survival time difference.
- rmstDiffUpper: The upper equivalence limit of restricted mean survival time difference.
- rmst1: The restricted mean survival time for the treatment group.
- rmst2: The restricted mean survival time for the control group.
- rmstDiff: The restricted mean survival time difference.
- accrualDuration: The accrual duration.
- followupTime: The follow-up duration.
- fixedFollowup: Whether a fixed follow-up design is used.
- byStageResults: A data frame containing the following variables:
  - informationRates: The information rates.
  - efficacyBounds: The efficacy boundaries on the Z-scale for each of the two one-sided tests.
  - rejectPerStage: The probability for efficacy stopping.
  - cumulativeRejection: The cumulative probability for efficacy stopping.
  - cumulativeAlphaSpent: The cumulative alpha for each of the two one-sided tests.
  - cumulativeAttainedAlphaH10: The cumulative alpha attained under H10.
  - cumulativeAttainedAlphaH20: The cumulative alpha attained under H20.
  - numberOfSubjects: The number of subjects.
  - analysisTime: The average time since trial start.
  - efficacyRmstDiffLower: The efficacy boundaries on the restricted mean survival time difference scale for the one-sided null hypothesis at the lower equivalence limit.
  - efficacyRmstDiffUpper: The efficacy boundaries on the restricted mean survival time difference scale for the one-sided null hypothesis at the upper equivalence limit.
  - efficacyP: The efficacy bounds on the p-value scale for each of the two one-sided tests.
  - information: The cumulative information.
- settings: A list containing the following input parameters: typeAlphaSpending, parameterAlphaSpending, userAlphaSpending, allocationRatioPlanned, accrualTime, accuralIntensity, piecewiseSurvivalTime, stratumFraction, lambda1, lambda2, gamma1, gamma2, and spendingTime.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## See Also

rmstat

#### **Examples**

```
rmpowerequiv(kMax = 2, informationRates = c(0.5, 1), alpha = 0.05, typeAlphaSpending = "sfOF", milestone = 18, rmstDiffLower = -2, rmstDiffUpper = 2, allocationRatioPlanned = 1, accrualTime = seq(0, 8), accrualIntensity = 100/9*seq(1, 9), piecewiseSurvivalTime = c(0, 6), stratumFraction = c(0.2, 0.8), lambda1 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533), gamma1 = -log(1-0.05)/12, gamma2 = -log(1-0.05)/12, accrualDuration = 22, followupTime = 18, fixedFollowup = FALSE)
```

rmsamplesize

Sample size for difference in restricted mean survival times

## Description

Obtains the needed accrual duration given power, accrual intensity, and follow-up time, the needed follow-up time given power, accrual intensity, and accrual duration, or the needed absolute accrual intensity given power, relative accrual intensity, accrual duration, and follow-up time in a two-group survival design.

```
rmsamplesize(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
 milestone = NA_real_,
```

```
rmstDiffH0 = 0,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

#### Arguments

beta Type II error. Defaults to 0.2.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

milestone The milestone time at which to calculate the restricted mean survival time.

rmstDiffH0 The difference in restricted mean survival times under the null hypothesis. Defaults to 0 for superiority test.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates

for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

The interval to search for the solution of accrualDuration, followupTime, or the

proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

#### Value

A list of two components:

- resultsUnderH1: An S3 class rmpower object under the alternative hypothesis.
- resultsUnderH0: An S3 class rmpower object under the null hypothesis.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### See Also

rmpower

# **Examples**

```
# Example 1: Obtains follow-up time given power, accrual intensity,
# and accrual duration for variable follow-up. Of note, the power
# reaches the maximum when the follow-up time equals milestone.
rmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             milestone = 18,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -\log(1-0.05)/12, accrualDuration = 22,
             followupTime = NA, fixedFollowup = FALSE)
# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up time for variable follow-up
rmsamplesize(beta = 0.2, kMax = 2, informationRates = c(0.8, 1),
             alpha = 0.025, typeAlphaSpending = "sfOF",
             milestone = 18,
             allocationRatioPlanned = 1, accrualTime = seq(0, 8),
             accrualIntensity = 100/9*seq(1, 9),
             piecewiseSurvivalTime = c(0, 6),
             stratumFraction = c(0.2, 0.8),
             lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
             lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
             gamma1 = -log(1-0.05)/12,
             gamma2 = -\log(1-0.05)/12, accrualDuration = 22,
```

rmsamplesize1s

Sample size for one-sample restricted mean survival time

#### **Description**

Obtains the needed accrual duration given power and follow-up time, the needed follow-up time given power and accrual duration, or the needed absolute accrual rates given power, accrual duration, follow-up duration, and relative accrual rates in a one-group survival design.

```
rmsamplesize1s(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  efficacyStopping = NA_integer_,
  futilityStopping = NA_integer_,
  criticalValues = NA_real_,
  alpha = 0.025,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
  futilityBounds = NA_real_,
  typeBetaSpending = "none",
  parameterBetaSpending = NA_real_,
  userBetaSpending = NA_real_,
  milestone = NA_real_,
  rmstH0 = NA_real_,
```

```
accrualTime = 0L,
accrualIntensity = NA_real_,
piecewiseSurvivalTime = 0L,
stratumFraction = 1L,
lambda = NA_real_,
gamma = 0L,
accrualDuration = NA_real_,
followupTime = NA_real_,
fixedFollowup = 0L,
interval = as.numeric(c(0.001, 240)),
spendingTime = NA_real_,
rounding = 1L
```

# Arguments

beta Type II error. Defaults to 0.2.

kMax The maximum number of stages.

informationRates

The information rates. Defaults to (1:kMax) / kMax if left unspecified.

efficacyStopping

Indicators of whether efficacy stopping is allowed at each stage. Defaults to true if left unspecified.

futilityStopping

Indicators of whether futility stopping is allowed at each stage. Defaults to true if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level. Defaults to 0.025.

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

#### parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

futilityBounds Lower boundaries on the z-test statistic scale for stopping for futility at stages 1, ..., kMax-1. Defaults to rep(-6, kMax-1) if left unspecified. The futility bounds are non-binding for the calculation of critical values.

typeBetaSpending

The type of beta spending. One of the following: "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for

Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early futility stopping. Defaults to "none".

parameterBetaSpending

The parameter value for the beta spending. Corresponds to rho for "sfKD", and gamma for "sfHSD".

userBetaSpending

The user defined beta spending. Cumulative beta spent up to each stage.

milestone The milestone time at which to calculate the restricted survival time.

rmstH0 The restricted mean survival time under the null hypothesis.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda A vector of hazard rates for the event in each analysis time interval by stratum

under the alternative hypothesis.

gamma The hazard rate for exponential dropout or a vector of hazard rates for piecewise

exponential dropout. Defaults to 0 for no dropout.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

 ${\tt fixedFollowup} \quad \text{Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.}$ 

interval The interval to search for the solution of accrualDuration, followupDuration, or

the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

## Value

A list of two components:

- resultsUnderH1: An S3 class rmpower1s object under the alternative hypothesis.
- resultsUnderH0: An S3 class rmpower1s object under the null hypothesis.

## Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

## See Also

rmpower1s

#### **Examples**

```
# Example 1: Obtains follow-up duration given power, accrual intensity,
# and accrual duration for variable follow-up
rmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
              milestone = 18, rmstH0 = 10,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
              piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -\log(1-0.05)/12, accrualDuration = 22,
               followupTime = NA, fixedFollowup = FALSE)
# Example 2: Obtains accrual intensity given power, accrual duration, and
# follow-up duration for variable follow-up
rmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
              milestone = 18, rmstH0 = 10,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
              piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -\log(1-0.05)/12, accrualDuration = 22,
               followupTime = 18, fixedFollowup = FALSE)
# Example 3: Obtains accrual duration given power, accrual intensity, and
# follow-up duration for fixed follow-up
rmsamplesize1s(beta = 0.2, kMax = 2,
               informationRates = c(0.8, 1),
               alpha = 0.025, typeAlphaSpending = "sfOF",
              milestone = 18, rmstH0 = 10,
               accrualTime = seq(0, 8),
               accrualIntensity = 26/9*seq(1, 9),
               piecewiseSurvivalTime = c(0, 6),
               stratumFraction = c(0.2, 0.8),
               lambda = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
               gamma = -\log(1-0.05)/12, accrualDuration = NA,
               followupTime = 18, fixedFollowup = TRUE)
```

rmsamplesizeequiv 333

rmsamplesizeequiv

Sample size for equivalence in restricted mean survival time difference

#### **Description**

Obtains the sample size for equivalence in restricted mean survival time difference.

#### Usage

```
rmsamplesizeequiv(
  beta = 0.2,
  kMax = 1L,
  informationRates = NA_real_,
  criticalValues = NA_real_,
  alpha = 0.05,
  typeAlphaSpending = "sfOF",
  parameterAlphaSpending = NA_real_,
  userAlphaSpending = NA_real_,
 milestone = NA_real_,
  rmstDiffLower = NA_real_,
  rmstDiffUpper = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
 piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
  followupTime = NA_real_,
  fixedFollowup = 0L,
  interval = as.numeric(c(0.001, 240)),
  spendingTime = NA_real_,
  rounding = 1L
)
```

## **Arguments**

beta The type II error.

kMax The maximum number of stages.

informationRates
The information rates. Defaults to (1:kMax) / kMax if left unspecified.

criticalValues Upper boundaries on the z-test statistic scale for stopping for efficacy.

alpha The significance level for each of the two one-sided tests. Defaults to 0.05.

334 rmsamplesizeequiv

typeAlphaSpending

The type of alpha spending. One of the following: "OF" for O'Brien-Fleming boundaries, "P" for Pocock boundaries, "WT" for Wang & Tsiatis boundaries, "sfOF" for O'Brien-Fleming type spending function, "sfP" for Pocock type spending function, "sfKD" for Kim & DeMets spending function, "sfHSD" for Hwang, Shi & DeCani spending function, "user" for user defined spending, and "none" for no early efficacy stopping. Defaults to "sfOF".

parameterAlphaSpending

The parameter value for the alpha spending. Corresponds to Delta for "WT", rho for "sfKD", and gamma for "sfHSD".

userAlphaSpending

The user defined alpha spending. Cumulative alpha spent up to each stage.

milestone The milestone time at which to calculate the restricted mean survival time.

rmstDiffLower The lower equivalence limit of restricted mean survival time difference.

rmstDiffUpper The upper equivalence limit of restricted mean survival time difference.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

rmst 335

The interval to search for the solution of accrualDuration, followupDuration, or

the proportionality constant of accrualIntensity. Defaults to c(0.001, 240).

spendingTime A vector of length kMax for the error spending time at each analysis. Defaults to

missing, in which case, it is the same as informationRates.

rounding Whether to round up sample size. Defaults to 1 for sample size rounding.

#### Value

An S3 class rmpowerequiv object

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

#### See Also

```
rmpowerequiv
```

## **Examples**

rmst

Restricted mean survival time

#### **Description**

Obtains the restricted mean survival time over an interval.

```
rmst(t1 = 0, t2 = NA_real_, piecewiseSurvivalTime = 0L, lambda = NA_real_)
```

336 rmstat

# **Arguments**

t1 Lower bound of the analysis time interval.

t2 Upper bound of the analysis time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda

A vector of hazard rates for the event. One for each analysis time interval.

#### Value

The integral of the survival function from t1 to t2

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
rmst(t1 = 0, t2 = 7, piecewiseSurvivalTime = c(0, 6), lambda = c(0.0533, 0.0309))
```

rmstat

Stratified difference in restricted mean survival times

# **Description**

Obtains the stratified restricted mean survival times and difference in restricted mean survival times at given calendar times.

```
rmstat(
  time = NA_real_,
  milestone = NA_real_,
  allocationRatioPlanned = 1,
  accrualTime = 0L,
  accrualIntensity = NA_real_,
  piecewiseSurvivalTime = 0L,
  stratumFraction = 1L,
  lambda1 = NA_real_,
  lambda2 = NA_real_,
  gamma1 = 0L,
  gamma2 = 0L,
  accrualDuration = NA_real_,
```

rmstat 337

```
followupTime = NA_real_,
fixedFollowup = 0L
)
```

#### Arguments

time A vector of calendar times at which to calculate the restricted mean survival

time.

milestone The milestone time at which to calculate the restricted mean survival time.

allocationRatioPlanned

Allocation ratio for the active treatment versus control. Defaults to 1 for equal

randomization.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda1 A vector of hazard rates for the event in each analysis time interval by stratum

for the active treatment group.

lambda2 A vector of hazard rates for the event in each analysis time interval by stratum

for the control group.

gamma1 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the active treatment

group.

gamma2 The hazard rate for exponential dropout, a vector of hazard rates for piece-

wise exponential dropout applicable for all strata, or a vector of hazard rates for dropout in each analysis time interval by stratum for the control group.

accrualDuration

Duration of the enrollment period.

followupTime Follow-up time for the last enrolled subject.

fixedFollowup Whether a fixed follow-up design is used. Defaults to 0 for variable follow-up.

#### Value

A data frame containing the following variables:

- time: The calendar time at which to calculate the restricted mean survival time.
- subjects: The number of enrolled subjects.
- milestone: The milestone time relative to randomization.

338 rtpwexp

- rmst1: The restricted mean survival time for the treatment group.
- rmst2: The restricted mean survival time for the control group.
- rmstDiff: The difference in restricted mean survival times, i.e., rmst1 rmst2.
- vrmst1: The variance for rmst1.
- vrmst2: The variance for rmst2.
- vrmstDiff: The variance for rmstDiff.
- information: The information for rmstDiff, equal to 1/vrmstDiff.
- rmstDiffZ: The Z-statistic value, i.e., rmstDiff/sqrt(vrmstDiff).

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

# Examples

```
# Piecewise accrual, piecewise exponential survivals, and 5% dropout by
# the end of 1 year.

rmstat(time = c(22, 40),
    milestone = 18,
    allocationRatioPlanned = 1,
    accrualTime = seq(0, 8),
    accrualIntensity = 26/9*seq(1, 9),
    piecewiseSurvivalTime = c(0, 6),
    stratumFraction = c(0.2, 0.8),
    lambda1 = c(0.0533, 0.0309, 1.5*0.0533, 1.5*0.0309),
    lambda2 = c(0.0533, 0.0533, 1.5*0.0533, 1.5*0.0533),
    gamma1 = -log(1-0.05)/12,
    gamma2 = -log(1-0.05)/12,
    accrualDuration = 22,
    followupTime = 18, fixedFollowup = FALSE)
```

rtpwexp

Random number generation function of truncated piecewise exponential distribution

# **Description**

Obtains random samples from a truncated piecewise exponential distribution.

```
rtpwexp(n, piecewiseSurvivalTime = 0, lambda = 0.0578, lowerBound = 0)
```

runShinyApp 339

#### **Arguments**

The number of observations.

piecewiseSurvivalTime

A vector that specifies the starting time of piecewise exponential survival time intervals. Must start with 0, e.g., c(0, 6) breaks the time axis into 2 event intervals: [0, 6) and [6, Inf.]. Defaults to 0 for exponential distribution.

intervals: [0, 6) and [6, Inf). Defaults to 0 for exponential distribution.

lambda A vector of hazard rates for the event. One for each analysis time interval.

lowerBound The left truncation time point for the survival time. Defaults to 0 for no trunca-

tion.

#### Value

The random numbers from truncated piecewise exponential distribution.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
rtpwexp(n = 10, piecewiseSurvivalTime = c(0, 6, 9, 15), lambda = c(0.025, 0.04, 0.015, 0.007))
```

runShinyApp

Run Shiny app

# **Description**

Runs the log-rank test power and sample size calculation Shiny app.

# Usage

runShinyApp()

#### Value

No return value, called for side effects.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

340 simon2stage

simon2stage

Simon's two-stage design

#### **Description**

Obtains Simon's two-stage minimax, admissible, and optimal designs.

# Usage

```
simon2stage(
  alpha = NA_real_,
  beta = NA_real_,
  piH0 = NA_real_,
  pi = NA_real_,
  n_max = 110L
)
```

# **Arguments**

alpha	Type I error rate (one-sided).
beta	Type II error rate (1-power).
piH0	Response probability under the null hypothesis.
pi	Response probability under the alternative hypothesis.
n_max	Upper limit for sample size, defaults to 110.

#### Value

A data frame containing the following variables:

- piH0: Response probability under the null hypothesis.
- pi: Response probability under the alternative hypothesis.
- alpha: The specified one-sided significance level.
- beta: The specified type II error.
- n: Total sample size.
- n1: Stage 1 sample size.
- r1: Futility boundary for stage 1.
- r: Futility boundary for stage 2.
- EN0: Expected sample size under the null hypothesis.
- attainedAlpha: Attained type 1 error.
- power: Attained power.
- PET0: Probability of early stopping under the null hypothesis.
- w\_lower: Lower bound of the interval for w.
- w\_upper: Upper bound of the interval for w.
- design: Description of the design, e.g., minimax, admissible, or optimal.

Here w is the weight in the objective function: w\*n + (1-w)\*EN0.

simonBayesAnalysis 341

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
simon2stage(0.05, 0.15, 0.1, 0.3)
```

simonBayesAnalysis

Analysis of Simon's Bayesian basket trials

# Description

Obtains the prior and posterior probabilities for Simon's Bayesian basket discovery trials.

#### Usage

```
simonBayesAnalysis(
  nstrata = NA_integer_,
  r = NA_integer_,
  n = NA_integer_,
  lambda = NA_real_,
  gamma = NA_real_,
  phi = NA_real_,
  plo = NA_real_)
```

#### **Arguments**

nstrata	The number of strata.
r	The vector of number of responders across strata.
n	The vector of number of subjects across strata.
lambda	The prior probability that the drug activity is homogeneous across strata.
gamma	The prior probability that the drug is active in a stratum.
phi	The response probability for an active drug.
plo	The response probability for an inactive drug.

# Value

A list containing the following five components:

- case: The matrix with each row corresponding to a combination of drug activity over strata represented by the columns.
- prior\_case: The vector of joint prior probabilities for the stratum-specific response rates.

342 simonBayesSim

 prior\_stratum: The vector of marginal prior probabilities for the stratum-specific response rates.

- post\_case: The vector of joint posterior probabilities for the stratum-specific response rates.
- post\_stratum: The vector of marginal posterior probabilities for the stratum-specific response rates.

#### Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### **Examples**

```
a = simonBayesAnalysis(
  nstrata = 10,
  r = c(8,0,1,1,6,2,0,0,3,3),
  n = c(19,10,26,8,14,7,8,5,4,14),
  lambda = 0.5, gamma = 0.33,
  phi = 0.35, plo = 0.15)
a$post_stratum
```

simonBayesSim

Simulation of Simon's Bayesian basket trials

## Description

Obtains the simulated raw and summary data for Simon's Bayesian basket discovery trials.

```
simonBayesSim(
 p = NA_real_,
 accrualTime = 0L,
  accrualIntensity = NA_real_,
  stratumFraction = 1L,
  lambda = NA_real_,
  gamma = NA_real_,
 phi = NA_real_,
 plo = NA_real_,
 T = NA_real_,
 maxSubjects = NA_integer_,
 plannedSubjects = NA_integer_,
 maxNumberOfIterations = 1000L,
 maxNumberOfRawDatasets = 1L,
  seed = NA_integer_
)
```

simonBayesSim 343

#### **Arguments**

p The vector of true response probabilities across strata.

accrualTime A vector that specifies the starting time of piecewise Poisson enrollment time

intervals. Must start with 0, e.g., c(0, 3) breaks the time axis into 2 accrual

intervals: [0, 3) and [3, Inf).

accrualIntensity

A vector of accrual intensities. One for each accrual time interval.

stratumFraction

A vector of stratum fractions that sum to 1. Defaults to 1 for no stratification.

lambda The prior probability that the drug activity is homogeneous across strata.

gamma The prior probability that the drug is active in a stratum.

phi The response probability for an active drug.

The response probability for an inactive drug.

The threshold for a conclusive posterior probability to stop enrollment.

maxSubjects The maximum total sample size.

plannedSubjects

The planned cumulative number of subjects at each stage.

maxNumberOfIterations

The number of simulation iterations. Defaults to 1000.

maxNumberOfRawDatasets

The number of raw datasets to extract.

seed The seed to reproduce the simulation results. The seed from the environment

will be used if left unspecified,

#### Value

A list containing the following four components:

- rawdata: A data frame for subject-level data, containing the following variables:
  - iterationNumber: The iteration number.
  - stageNumber: The stage number.
  - subjectId: The subject ID.
  - arrivalTime: The enrollment time for the subject.
  - stratum: The stratum for the subject.
  - y: Whether the subject was a responder (1) or nonresponder (0).
- sumdata1: A data frame for simulation and stratum-level summary data, containing the following variables:
  - iterationNumber: The iteration number.
  - stageNumber: The stage number.
  - stratum: The stratum number.
  - active: Whether the drug is active in the stratum.
  - n: The number of subjects in the stratum.
  - r: The number of responders in the stratum.

344 simonBayesSim

- posterior: The posterior probability that the drug is active in the stratum.
- open: Whether the stratum is still open for enrollment.
- positive: Whether the stratum has been determined to be a positive stratum.
- negative: Whether the stratum has been determined to be a negative stratum.
- sumdata2: A data frame for the simulation level summary data, containing the following variables:
  - iterationNumber: The iteration number.
  - numberOfStrata: The total number of strata.
  - n\_active\_strata: The number of active strata.
  - true\_positive: The number of true positive strata.
  - false\_negative: The number of false negative strata.
  - false\_positive: The number of false positive strata.
  - true\_negative: The number of true negative strata.
  - n\_indet\_strata: The number of indeterminate strata.
  - numberOfSubjects: The number of subjects.
- overview: A data frame for the summary across simulations, containing the following variables:
  - number Of Strata: The total number of strata.
  - n\_active\_strata: The average number of active strata.
  - true\_positive: The average number of true positive strata.
  - false\_negative: The average number of false negative strata.
  - false\_positive: The average number of false positive strata.
  - true\_negative: The average number of true negative strata.
  - n\_indet\_strata: The average number of indeterminate strata.
  - numberOfSubjects: The average number of subjects.

# Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

#### **Examples**

```
sim1 = simonBayesSim(
   p = c(0.25, 0.25, 0.05),
   accrualIntensity = 5,
   stratumFraction = c(1/3, 1/3, 1/3),
   lambda = 0.33, gamma = 0.5,
   phi = 0.25, plo = 0.05,
   T = 0.8, maxSubjects = 50,
   plannedSubjects = seq(5, 50, 5),
   maxNumberOfIterations = 1000,
   maxNumberOfRawDatasets = 1,
   seed = 314159)
```

sim1\$overview

survQuantile 345

survQuantile	Brookmeyer-Crowley	confidence	interval	for	quantiles	of	right-
	censored time-to-even	t data					

#### **Description**

Obtains the Brookmeyer-Crowley confidence interval for quantiles of right-censored time-to-event data.

# Usage

```
survQuantile(
  time = NA_real_,
  event = NA_real_,
  cilevel = 0.95,
  transform = "loglog",
  probs = c(0.25, 0.5, 0.75)
)
```

#### **Arguments**

time The vector of possibly right-censored survival times.

event The vector of event indicators.

cilevel The confidence interval level. Defaults to 0.95.

transform The transformation of the survival function to use to construct the confidence

interval. Options include "linear", "loglog", "log", "asinsqrt", and "logit". De-

faults to "loglog".

probs The vector of probabilities to calculate the quantiles. Defaults to c(0.25, 0.5,

0.75).

#### Value

A data frame containing the estimated quantile and confidence interval corresponding to each specified probability. It includes the following variables:

- prob: The probability to calculate the quantile.
- quantile: The estimated quantile.
- lower: The lower limit of the confidence interval.
- upper: The upper limit of the confidence interval.
- cilevel: The confidence interval level.
- transform: The transformation of the survival function to use to construct the confidence interval.

# Author(s)

Kaifeng Lu, <kaifenglu@gmail.com>

346 updateGraph

#### **Examples**

```
survQuantile( time = c(33.7, 3.9, 10.5, 5.4, 19.5, 23.8, 7.9, 16.9, 16.6, 33.7, 17.1, 7.9, 10.5, 38), event = c(0, 1, 1, 1, 1, 0, 1, 0, 0, 0, 0, 0, 1, 1), probs = c(0.25, 0.5, 0.75))
```

tobin

Tobin's tobit data from the survival package

# **Description**

```
Data from Tobin's original paper.
```

```
durable Durable goods purchase age Age in years quant Liquidity ratio (x 1000)
```

# Usage

tobin

# **Format**

An object of class data. frame with 20 rows and 3 columns.

updateGraph

Update graph for graphical approaches

## **Description**

Updates the weights and transition matrix for graphical approaches.

## Usage

```
updateGraph(w = NA_real_, G = NA_real_, I = NA_integer_, j = NA_integer_)
```

# Arguments

w The current vector	of weights for e	elementary hypotheses.
----------------------	------------------	------------------------

- G The current transition matrix.
- I The set of indices for yet to be rejected hypotheses.
- j The hypothesis to remove from index set I.

zstatOddsRatio 347

# Value

A list containing the new vector of weights, the new transition matrix for the graph, and the new set of indices of yet to be rejected hypotheses.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

zstatOddsRatio

Miettinen-Nurminen score test statistic for two-sample odds ratio

## **Description**

Obtains the Miettinen-Nurminen score test statistic for two-sample odds ratio possibly with stratification.

# Usage

```
zstatOddsRatio(
  oddsRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
```

#### **Arguments**

oddsRatioH0	The odds ratio under the null hypothesis. Defaults to 1.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

# **Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

348 zstatRateDiff

# Value

The value of the score test statistic.

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
zstatOddsRatio(oddsRatioH0 = 1, n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

zstatRateDiff

Miettinen-Nurminen score test statistic for two-sample rate difference

# **Description**

Obtains the Miettinen-Nurminen score test statistic for two-sample rate difference possibly with stratification.

# Usage

```
zstatRateDiff(
  rateDiffH0 = 0,
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_
```

# **Arguments**

rateDiffH0	The rate difference under the null hypothesis. Defaults to 0.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

## **Details**

The Mantel-Haenszel weights are used for stratified samples.

# Value

The value of the score test statistic.

zstatRateRatio 349

#### Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
zstatRateDiff(rateDiffH0 = 0, t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

zstatRateRatio

Miettinen-Nurminen score test statistic for two-sample rate ratio

# Description

Obtains the Miettinen-Nurminen score test statistic for two-sample rate ratio possibly with stratification.

# Usage

```
zstatRateRatio(
  rateRatioH0 = 1,
  t1 = NA_real_,
  y1 = NA_real_,
  t2 = NA_real_,
  y2 = NA_real_
)
```

# Arguments

rateRatioH0	The rate ratio under the null hypothesis. Defaults to 1.
t1	The exposure for the active treatment group.
y1	The number of events for the active treatment group.
t2	The exposure for the control group.
y2	The number of events for the control group.

# **Details**

The Mantel-Haenszel weights are used for stratified samples.

## Value

The value of the score test statistic.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

350 zstatRiskDiff

# **Examples**

```
zstatRateRatio(rateRatioH0 = 1, t1 = c(10,10), y1 = c(4,3), t2 = c(20,10), y2 = c(2,0))
```

zstatRiskDiff

Miettinen-Nurminen score test statistic for two-sample risk difference

# **Description**

Obtains the Miettinen-Nurminen score test statistic for two-sample risk difference possibly with stratification.

# Usage

```
zstatRiskDiff(
  riskDiffH0 = 0,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
```

# **Arguments**

riskDiffH0	The risk difference under the null hypothesis. Defaults to 0.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

## **Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

#### Value

The value of the score test statistic.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
zstatRiskDiff(riskDiffH0 = 0, n1 = c(10,10), y1 = c(4,3), 
 n2 = c(20,10), y2 = c(2,0))
```

zstatRiskRatio 351

zstatRiskRatio

Miettinen-Nurminen score test statistic for two-sample risk ratio

# Description

Obtains the Miettinen-Nurminen score test statistic for two-sample risk ratio possibly with stratification

#### Usage

```
zstatRiskRatio(
  riskRatioH0 = 1,
  n1 = NA_real_,
  y1 = NA_real_,
  n2 = NA_real_,
  y2 = NA_real_
)
```

# Arguments

riskRatioH0	The risk ratio under the null hypothesis. Defaults to 1.
n1	The sample size for the active treatment group.
y1	The number of responses for the active treatment group.
n2	The sample size for the control group.
y2	The number of responses for the control group.

# **Details**

The Mantel-Haenszel sample size weights are used for stratified samples.

# Value

The value of the score test statistic.

# Author(s)

```
Kaifeng Lu, <kaifenglu@gmail.com>
```

# **Examples**

```
zstatRiskRatio(riskRatioH0 = 1, n1 = c(10,10), y1 = c(4,3), n2 = c(20,10), y2 = c(2,0))
```

# **Index**

* datasets	getDesignFisherExact, 59
aml, 10	getDesignLogistic, 60
heart, 187	getDesignMeanDiff, 63
rawdata, 300	getDesignMeanDiffCarryover,66
tobin, 346	getDesignMeanDiffEquiv, 69
	getDesignMeanDiffMMRM, 72
accrual, 5	getDesignMeanDiffXO,77
adaptDesign, $6, 32, 36$	getDesignMeanDiffXOEquiv, 81
am1, 10	getDesignMeanRatio, 84
BOINTable, 11	getDesignMeanRatioEquiv, 88
bointable, II	getDesignMeanRatioXO, 91
caltime, 12	getDesignMeanRatioXOEquiv, 94
ClopperPearsonCI, 14	getDesignOddsRatio, 97
covrmst, 15	getDesignOddsRatioEquiv, 101
	getDesignOneMean, 104
errorSpent, 16	getDesignOneMultinom, 107
exitprob, 17	getDesignOneProportion, 109
0.11.1	<pre>getDesignOneRateExact, 112</pre>
fadjpbon, 18	getDesignOneSlope, 114
fadjpdun, 19	getDesignOrderedBinom, 117
fadjpsim, 20	getDesignPairedMeanDiff, 119
fmodmix, 21	getDesignPairedMeanDiffEquiv, 122
fquantile, 22	getDesignPairedMeanRatio, 125
fseqbon, 23	getDesignPairedMeanRatioEquiv, 129
fstdmix, 25	getDesignPairedPropMcNemar, 131
fstp2seq, 27 ftrunc, 28	getDesignRepeatedANOVA, 135
fwgtmat, 29	<pre>getDesignRepeatedANOVAContrast, 137</pre>
i wg tillat, 29	getDesignRiskDiff, 138
getAccrualDurationFromN, 29	getDesignRiskDiffEquiv, 142
getADCI, 30	getDesignRiskDiffExact, 145
getADRCI, 34	getDesignRiskDiffExactEquiv, 146
getBound, 37	getDesignRiskRatio, 148
getCI, 38	getDesignRiskRatioEquiv, 151
getCP, 40	<pre>getDesignRiskRatioExact, 154</pre>
getDesign, $9, 43, 45$	<pre>getDesignRiskRatioExactEquiv, 156</pre>
getDesignAgreement,48	getDesignRiskRatioFM, 157
getDesignANOVA, 50	<pre>getDesignSlopeDiff, 161</pre>
getDesignANOVAContrast, 52	getDesignSlopeDiffMMRM, 164
getDesignEquiv, 54	getDesignTwoMultinom, 170

INDEX 353

ID : T 0 I: 1 171	2006
getDesignTwoOrdinal, 171	ptpwexp, 296
getDesignTwoWayANOVA, 173	pwexpcuts, 297
getDesignUnorderedBinom, 174	pwexploglik, 298
getDesignUnorderedMultinom, 175	200
getDesignWilcoxon, 177	qtpwexp, 299
getDurationFromNevents, 180	rawdata, 300
getNeventsFromHazardRatio, 183	remlOddsRatio, 300
getRCI, 185	
1	remlRateDiff, 301
heart, 187	remlRateRatio, 302
hedgesg, 187	remlRiskDiff, 303
l	remlRiskRatio, 304
kmdiff, 189	repeatedPValue, 305
kmest, 191	riskDiffExactCI, 306
kmpower, 192, 206	riskDiffExactPValue, 307
kmpower1s, 196, 210	riskRatioExactCI, 308
kmpowerequiv, 200, 213	riskRatioExactPValue, 309
kmsamplesize, 203	rmdiff, 310
kmsamplesize1s, 207	rmest, 312
kmsamplesizeequiv, 211	rmpower, 313, 328
kmstat, <i>199</i> , <i>203</i> , 214	rmpower1s, 318, <i>332</i>
	rmpowerequiv, 321, <i>335</i>
liferegr, 216	rmsamplesize, 325
1rpower, 218, 231	rmsamplesize1s, 329
1rpowerequiv, 223, 234	rmsamplesizeequiv, 333
lrsamplesize, 228	rmst, 335
lrsamplesizeequiv, 232	rmstat, 227, 321, 325, 336
1rsim, 235	rtpwexp, 338
lrsim2e, 239	runShinyApp, 339
lrsim2e3a, 243	
lrsim3a, 249	simon2stage, 340
lrstat, 252	simonBayesAnalysis, 341
lrtest, 255	simonBayesSim, 342
	survQuantile, 345
mnOddsRatioCI, 257	
mnRateDiffCI, 258	tobin, 346
mnRateRatioCI, 259	
mnRiskDiffCI, 261	updateGraph, 346
mnRiskRatioCI, 262	
mTPI2Table, 263	zstatOddsRatio, 347
	zstatRateDiff, 348
nbpower, 265, 281	zstatRateRatio, 349
nbpower1s, 270, 285	zstatRiskDiff, 350
nbpowerequiv, 274, 288	zstatRiskRatio, 351
nbsamplesize, 278	
nbsamplesize1s, 282	
nbsamplesizeequiv, 286	
nbstat, 269, 273, 278, 289	
, , , ,	
phregr, 294	