

Introduction to continuous VPC

Introduction

When deriving a Visual Predictive Check (VPC) you must:

- Have both observed and simulated datasets that include x and y variables, typically TIME and DV
- Compute prediction intervals on simulated versus observed data

When deriving a VPC you may want to:

- Stratify over variables in your model
- Censor data below LLOQ
- Perform prediction correction (pcVPC)

The tidyvpc package makes these steps fast and easy:

- By providing readable syntax using the `%>%` operator from magrittr.
 - By using efficient backend computation, taking advantage of `data.table` parallelization.
 - By providing traditional binning methods and new binless methods
 - By using ggplot2 graphics engine to visualize the results of the VPC.
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This document introduces you to the `tidyvpc` set of tools, and shows you how to apply them to `tidyvpcobj` to derive VPC.

All of the `tidyvpc` functions require the `tidyvpcobj` as the first argument, with the exception of the first function `observed()` in the piping chain, which takes a `data.frame` or `data.table` of the observed dataset. Rather than forcing the user to either save intermediate objects or nest functions, `tidyvpc` provides the `%>%` operator from magrittr. The result from one step is then “piped” into the next step, with the final function in the piping chain always `vpcstats()`. You can use the pipe to rewrite multiple operations that you can read left-to-right, top-to-bottom (reading the pipe operator as “then”).

Data

To explore the functionality of `tidyvpc`, we’ll use an altered version of `obs_data(vpc::simple_data$obs)` and `sim_data(vpc::simple_data$sim)` from the `vpc` package. These datasets contain all necessary variables to explore the functionality of `tidyvpc` including:

- DV (y variable)

- TIME (x variable)
- NTIME (nominal time for binning on x-variable)
- GENDER (gender variable for stratification, “M”, “F”)
- STUDY (study for stratification, “Study A”, “Study B”)
- PRED (prediction variable for pcVPC)
- MDV (Missing DV)

Data Structure

`tidyvpc` requires specific structure of observed and simulated data to successfully generate VPC.

See `tidyvpc::obs_data` and `tidyvpc::sim_data` for example data structure.

```
obs_data <- data.table::as.data.table(tidyvpc::obs_data)
head(obs_data)
#>   ID      TIME    DV AMT DOSE MDV NTIME GENDER   STUDY
#> 1: 1 0.0000000 0.0 150 150  1  0.00      M Study A
#> 2: 1 0.2157624 37.3 0 150  0  0.25      M Study A
#> 3: 1 0.4694366 62.2 0 150  0  0.50      M Study A
#> 4: 1 0.8271844 74.1 0 150  0  1.00      M Study A
#> 5: 1 1.7724895 75.1 0 150  0  1.50      M Study A
#> 6: 1 1.7142415 58.3 0 150  0  2.00      M Study A
```

```
sim_data <- data.table::as.data.table(tidyvpc::sim_data)
head(sim_data)
#>   ID REP      TIME    DV IPRED    PRED AMT DOSE MDV NTIME
#> 1: 1  1 0.0000000 0.000 0.000 0.000 150 150  1  0.00
#> 2: 1  1 0.2157624 24.470 22.400 29.931 0 150  0  0.25
#> 3: 1  1 0.4694366 49.541 38.780 49.995 0 150  0  0.50
#> 4: 1  1 0.8271844 56.510 58.644 69.981 0 150  0  1.00
#> 5: 1  1 1.7724895 63.165 67.310 73.799 0 150  0  1.50
#> 6: 1  1 1.7142415 66.649 69.466 69.487 0 150  0  2.00
```

Preprocessing data

First, we'll need to subset our data by filtering `MDV == 0`, which removes rows where both `DV == 0` and `TIME == 0`.

```
obs_data <- obs_data[MDV == 0]
sim_data <- sim_data[MDV == 0]
```

Next, we'll add the prediction variable from the first replicate of simulated data into our observed data.

```
obs_data$PRED <- sim_data[REP == 1, PRED]
```

observed()

The `observed()` function is always the first function used in the VPC piping chain and is used to specify the observed dataset and corresponding variables. There are three arguments that are required to use `observed`. The first argument is either a `data.frame` or `data.table`, the second argument is the name of x-variable in the observed data, and the third argument is the name of the y-variable. Note that variable names should be unquoted.

```
library(tidyvpc)
vpc <- observed(obs_data, x = TIME, y = DV)
```

simulated()

The `simulated()` function is used to specify the simulated dataset and corresponding variables. There are two arguments that are required in order to use `simulated()`. Since the function is “piped” in after the `observed()` function, the first argument is the tidyvpcobj and should not be included, followed by the name of the simulated data, then the name of y-variable in the simulated data. Variable names should be unquoted and x-variable should not be included as it is recycled from the `observed()` function.

```
vpc <- observed(obs_data, x = TIME, y = DV) %>%
  simulated(sim_data, y = DV)
```

binning()

The `binning()` function provides the binning method to derive the VPC and should be inputted as a character string in the `bin` argument. Binning methods include: “ntile”, “pam”, “sd”, “equal”, “pretty”, “quantile”, “kmeans”, “jenks”, “centers”, “breaks”. Some methods such as “ntile” and “pam” will require you to specify the number of bins using the `nbins` argument (e.g., `nbins = 9`).

If using `bin = "centers"` or `bin = "breaks"`, you must also provide the centers/breaks argument as a numeric vector in the function (e.g., `centers = c(1,3,5,7)`).

You can also bin directly on x-variable. If using this type of binning, the `bin` argument should be the unquoted variable name that you used in the `observed()` function (e.g., `bin = NTIME` for the Nominal Time variable in the data).

Binning on x-variable, `NTIME`

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  binning(bin = NTIME)
```

Binning with “ntile”

```
vpc <- observed(obs_data, x = TIME, y = DV) %>%
  simulated(sim_data, y = DV) %>%
  binning(bin = "ntile", nbins = 9)
```

Binning with “breaks”

```
vpc <- observed(obs_data, x = TIME, y = DV) %>%
  simulated(sim_data, y = DV) %>%
  binning(bin = "breaks", breaks = c(1,5,7,9,10))
```

binless()

Note: The `binless()` examples below relate to a continuous VPC. See examples of `binless()` implementation for categorical VPC.

Binless methods for continuous VPC use Additive Quantile Regression (AQR) in place of traditional binning. By default, `binless()` performs AQR at the 5%, 50%, and 95% quantiles, but you can change this using the `qpred` argument in `vpcstats()`, which takes a numeric vector of length 3 (e.g., `qpred = c(.1, .5, .9)` for the 10%, 50%, 90% quantiles).

The lambda smoothing parameters for each quantile are optimized by default with AIC as indicated by the `optimize = TRUE` argument. If you would like to use different lambda values for each quantile set `optimize = FALSE` and specify lambda values for each quantile as a numeric vector of length 3 with the `lambda` argument (e.g., `lambda = c(1,3,2)` corresponds to the lambda values for the quantiles in the `qpred` argument (lower, median, upper)). Note: The higher the lambda value the smoother the fit to the data.

Binless optimized

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  binless()
```

Binless with user-specified lambda values at 10%, 50%, 90% quantiles. Set `optimize = FALSE` and provide lambda smoothing parameters as a vector of length 3 for lower, median, upper quantiles.

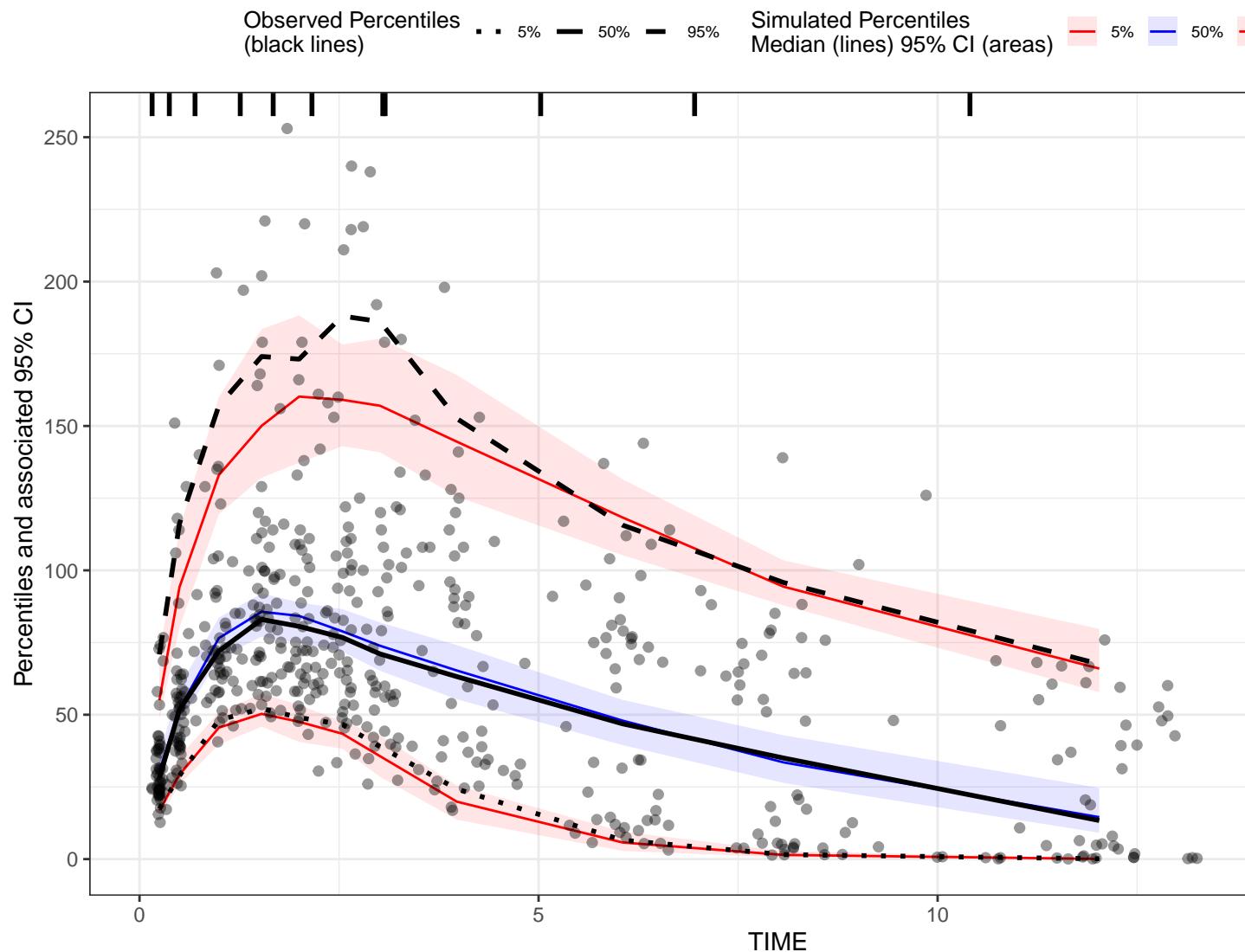
```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  binless(qpred = c(0.1, 0.5, 0.9), optimize = FALSE, lambda = c(1,3,2))
```

vpcstats()

The `vpcstats()` function is always the final function used in the piping chain and calculates the statistics needed to plot a VPC. If using `binning()` methods, you may specify alternative quantiles using the `qpred` argument. The default quantiles used are 5%, 50%, 95% (e.g., `qpred = c(0.05, 0.5, 0.95)`).

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  binning(bin = NTIME) %>%
  vpcstats()
```

```
plot(vpc)
```

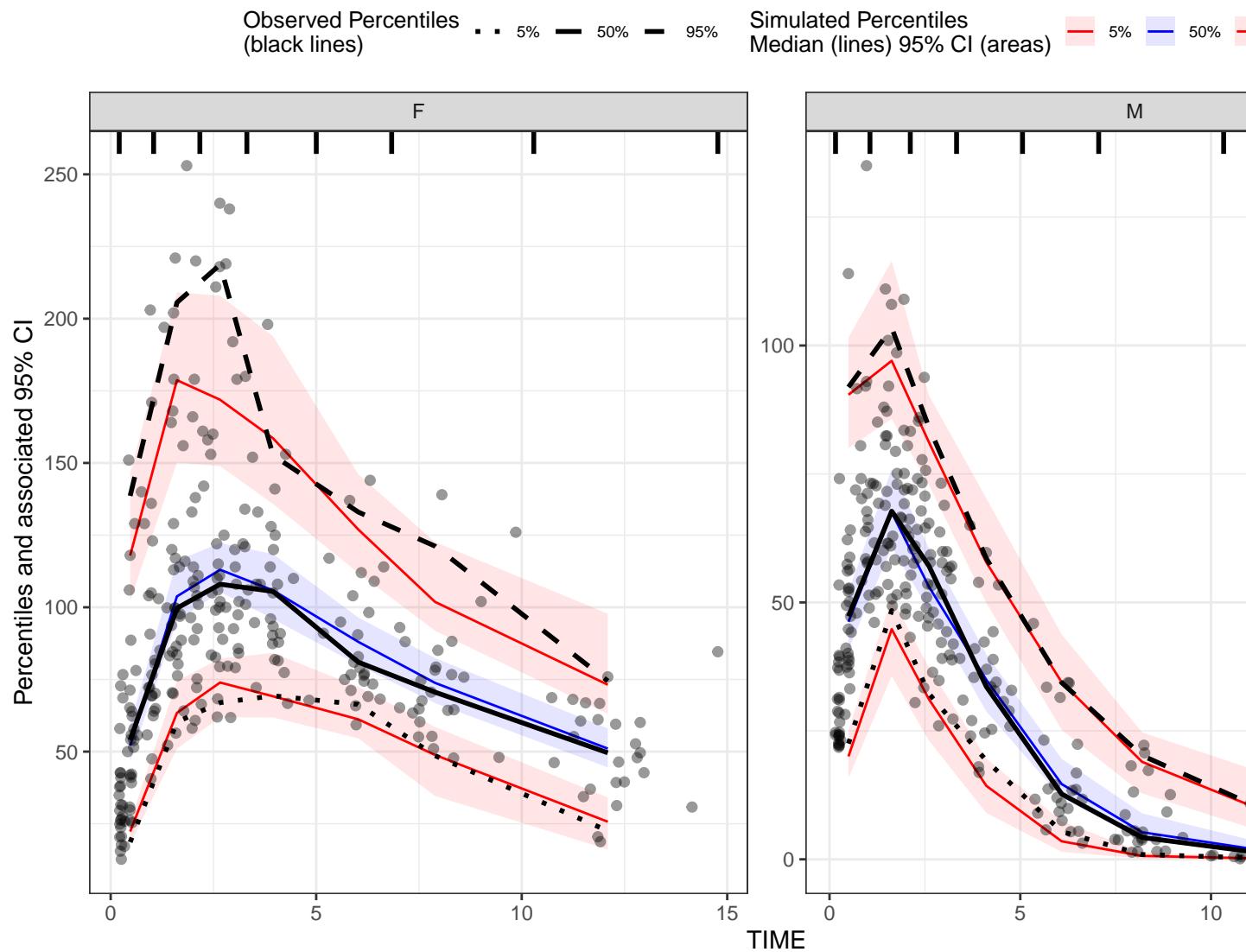


stratify()

To stratify VPC, include the `stratify()` function before using the `binning()` or `binless()` function and use the unquoted stratification variable(s) name as a formula. Let's stratify on GENDER in the data, which contains 2 levels (GENDER = "M", GENDER = "F"). Include as many stratification variables as your model calls for.

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  stratify(~ GENDER) %>%
  binning(bin = "pam", nbins = 7) %>%
  vpcstats()

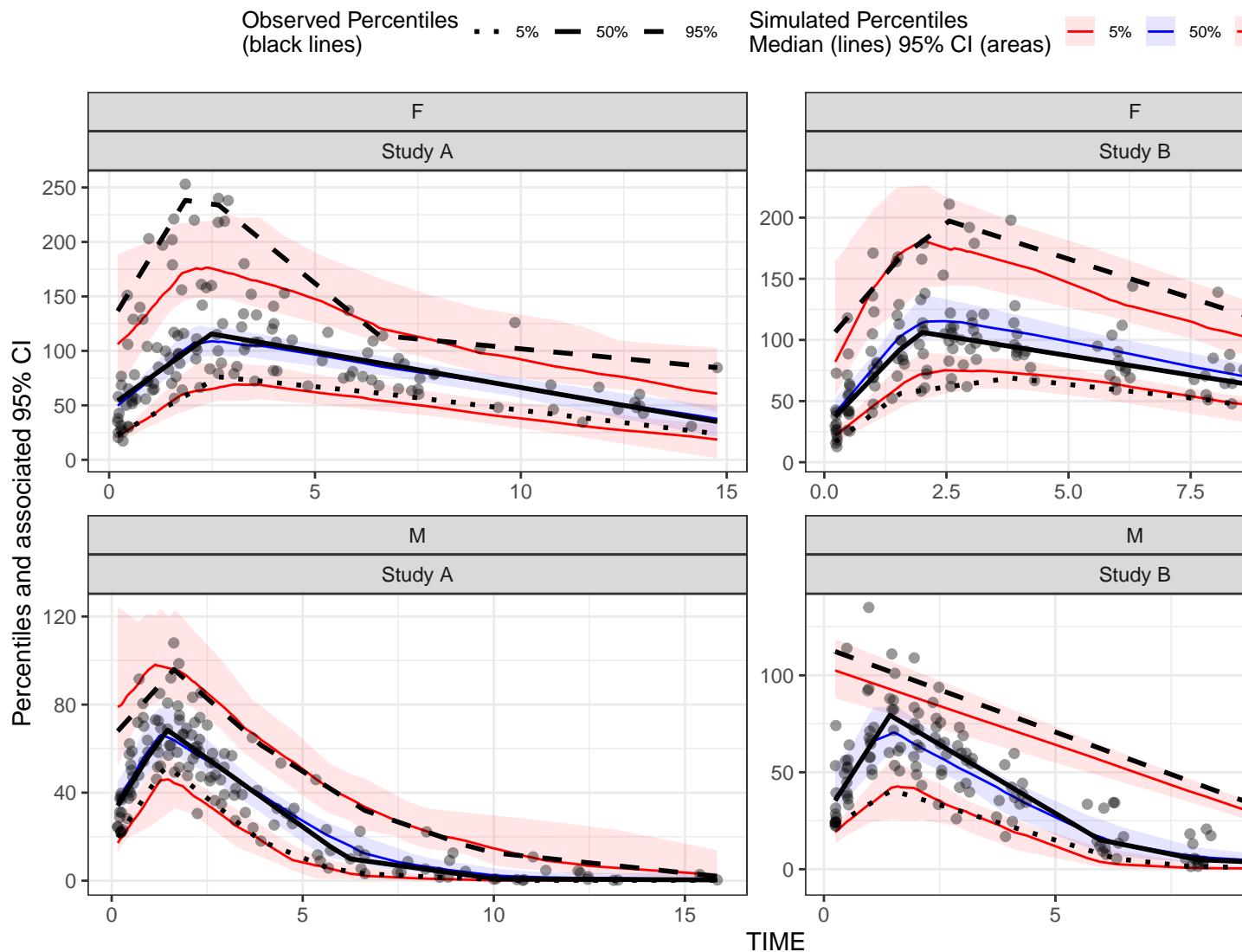
plot(vpc)
```



Using multiple stratification variables GENDER and STUDY.

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  stratify(~ GENDER + STUDY) %>%
  binless() %>%
  vpcstats()

plot(vpc)
```



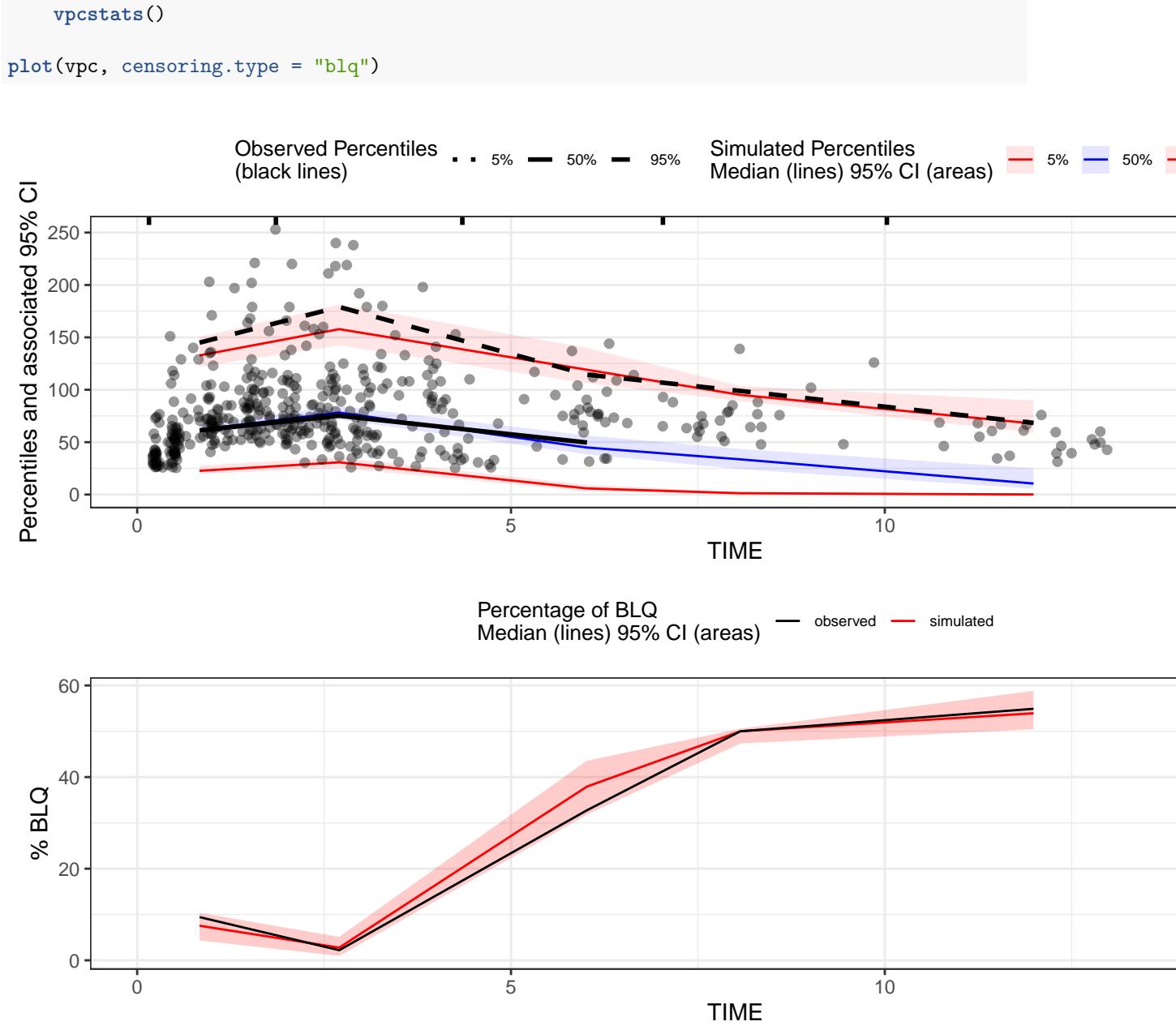
`censoring()`

Note: The `censoring()` function is only applicable for continuous VPC.

To censor observed data below lower limit of quantification (LLOQ), include the `censoring()` function after `simulated()` and use the `lloq` argument to specify either a variable in the data or specific value for censoring. The `blq` argument creates a logical TRUE/FALSE in the data that indicates whether the value is below the limit of quantification and is typically defined as rows with `DV < LLOQ` in the data. Using the `censoring()` function will censor only observed data below lower limit of quantification when plotting, simulated data will still be plotted.

Censoring using numeric value.

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  censoring(blq=(DV < 25), lloq=25) %>%
  binning(bin = "jenks", nbins = 5) %>%
```

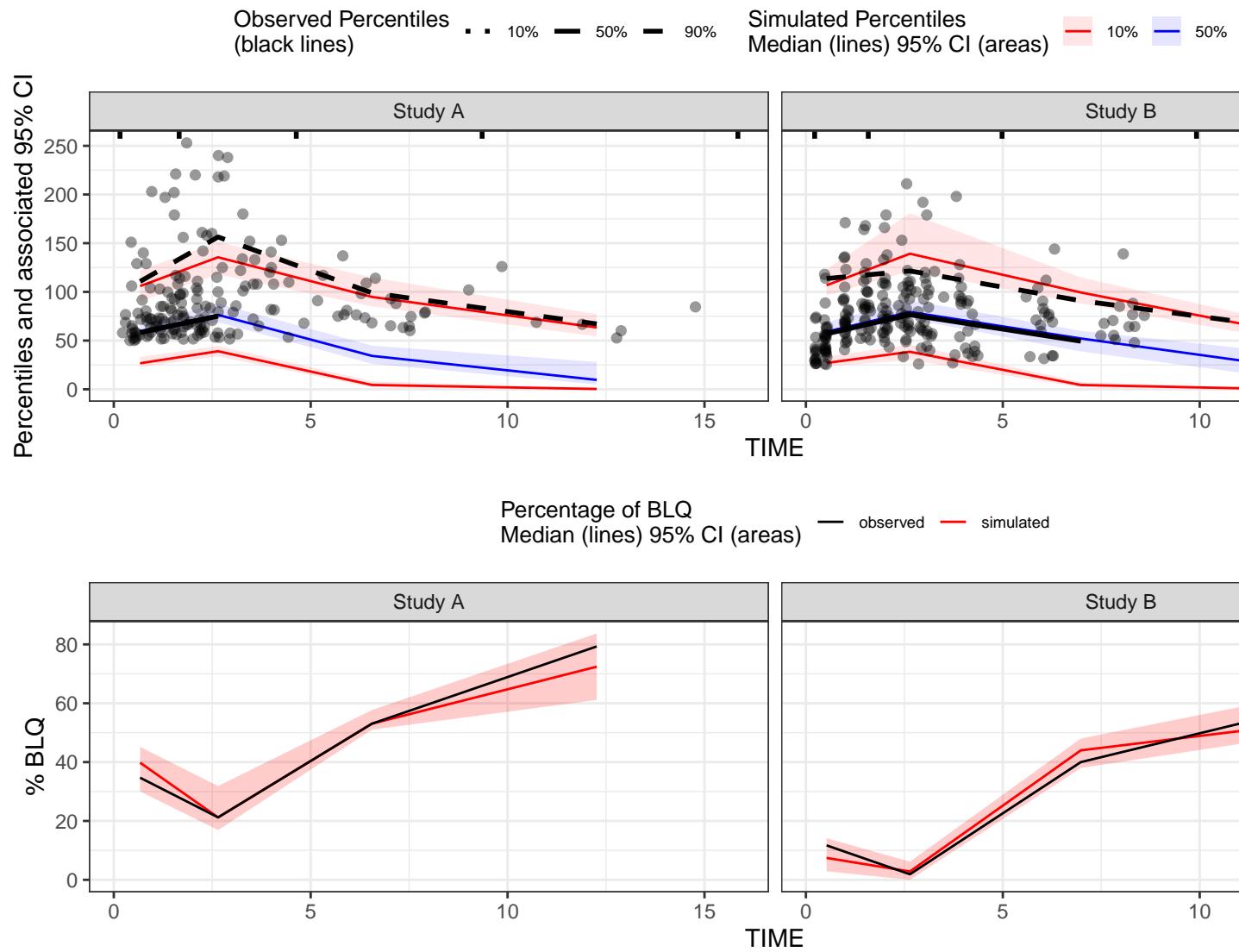


The `tidyvpc` package also allows you to use LLOQ values within your data and different LLOQ for each level of stratification variable. We'll set an LLOQ value of 50 for Study A and 25 for Study B and calculate statistics at 10%, 50%, 90% quantiles.

```
obs_data$LLOQ <- obs_data[, ifelse(STUDY == "Study A", 50, 25)]

vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  censoring(blq=(DV < LLOQ), lloq=LLOQ) %>%
  stratify(~ STUDY) %>%
  binning(bin = "pam", nbins = 4) %>%
  vpcstats(qpred = c(0.1, 0.5, 0.9))
```

```
plot(vpc, censoring.type = "blq", facet.scales = "fixed")
```



The tidyvpc package also supports usage of `censoring()` with ALQ data, similar to above usage with BLQ data.

```
obs_data$ULQ <- obs_data[, ifelse(STUDY == "Study A", 125, 100)]  
  
vpc <- observed(obs_data, x = TIME, y = DV) |>  
  simulated(sim_data, y = DV) |>  
  censoring(alq = DV > ULOQ, uloq = ULOQ) |>  
  stratify(~ STUDY) |>  
  binning(bin = NTIME) |>  
  vpcstats(qpred = c(0.1, 0.5, 0.9))
```

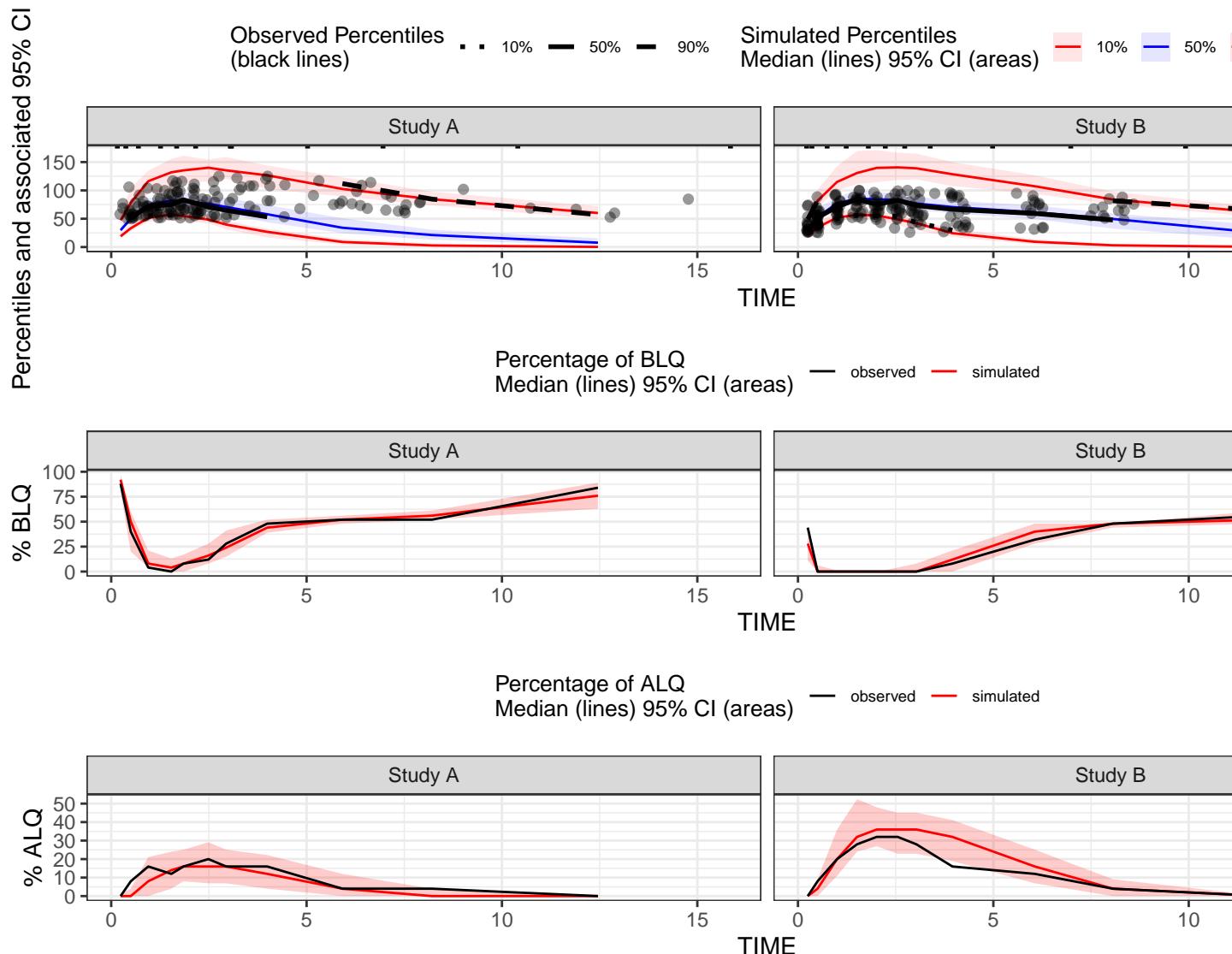
To plot the above vpc and include the percentage of ALQ plot, you'd run `plot(vpc, censoring.type = "alq")`.

If using `censoring()` with both ALQ and BLQ data, set `censoring.type = "both"` in the `plot()` function to display both percentage of BLQ and ALQ plots as a grid in the resulting VPC plot.

```
obs_data$LLOQ <- obs_data[, ifelse(STUDY == "Study A", 50, 25)]
obs_data$ULOQ <- obs_data[, ifelse(STUDY == "Study A", 125, 100)]
```

```
vpc <- observed(obs_data, x = TIME, y = DV) |>
  simulated(sim_data, y = DV) |>
  censoring(blq = DV < LLOQ, lloq = LLOQ, alq = DV > ULOQ, uloq = ULOQ) |>
  stratify(~ STUDY) |>
  binning(bin = NTIME) |>
  vpcstats(qpred = c(0.1, 0.5, 0.9))
```

```
plot(vpc, censoring.type = "both", facet.scales = "fixed")
```



If you want to return the percentage of BLQ and/or ALQ plots individually as elements in a list, instead of arranged in a grid, use the `censoring.output` argument e.g., `plot_list <- plot(vpc, censoring.type = "both", censoring.output = "list")`.

`predcorrect()`

Note: The `predcorrect()` function is only applicable for continuous VPC.

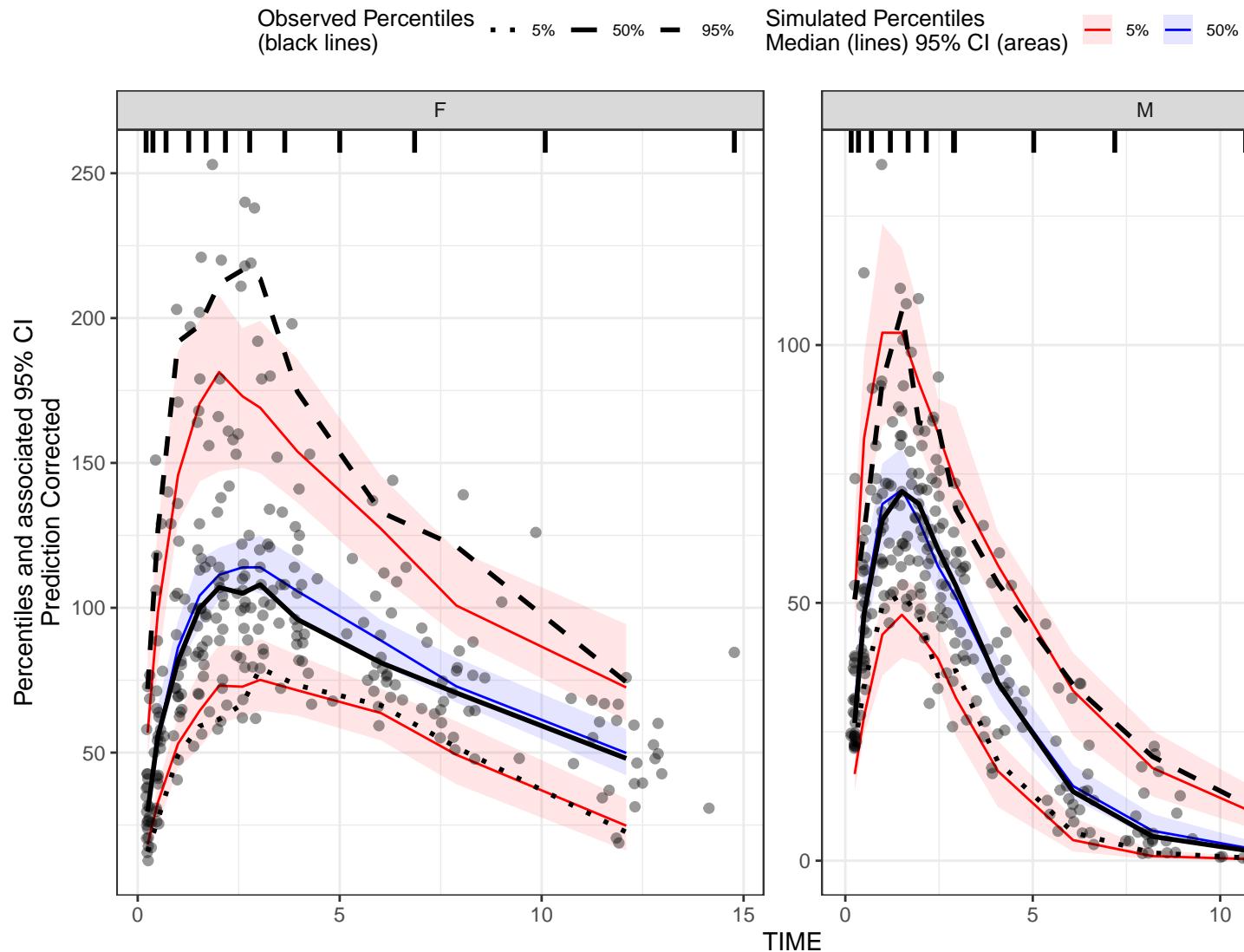
To derive a prediction corrected VPC (pcVPC), use the `predcorrect()` function. The `predcorrect()` function requires the argument, `pred`, which should be the unquoted variable name of the population prediction variable in the data. The `predcorrect()` function may be called either before or after specifying `binning()`/`binless()`. If using the `binless()` function with `predcorrect()`, LOESS pcVPC will be performed.

Note: If the model was fit using log scale of DV, make sure to include the argument `log = TRUE` in `predcorrect()` to perform the appropriate prediction correction calculation.

Prediction corrected using binning methods.

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  stratify(~GENDER) %>%
  binning(bin = NTIME) %>%
  predcorrect(pred=PRED) %>%
  vpcstats()

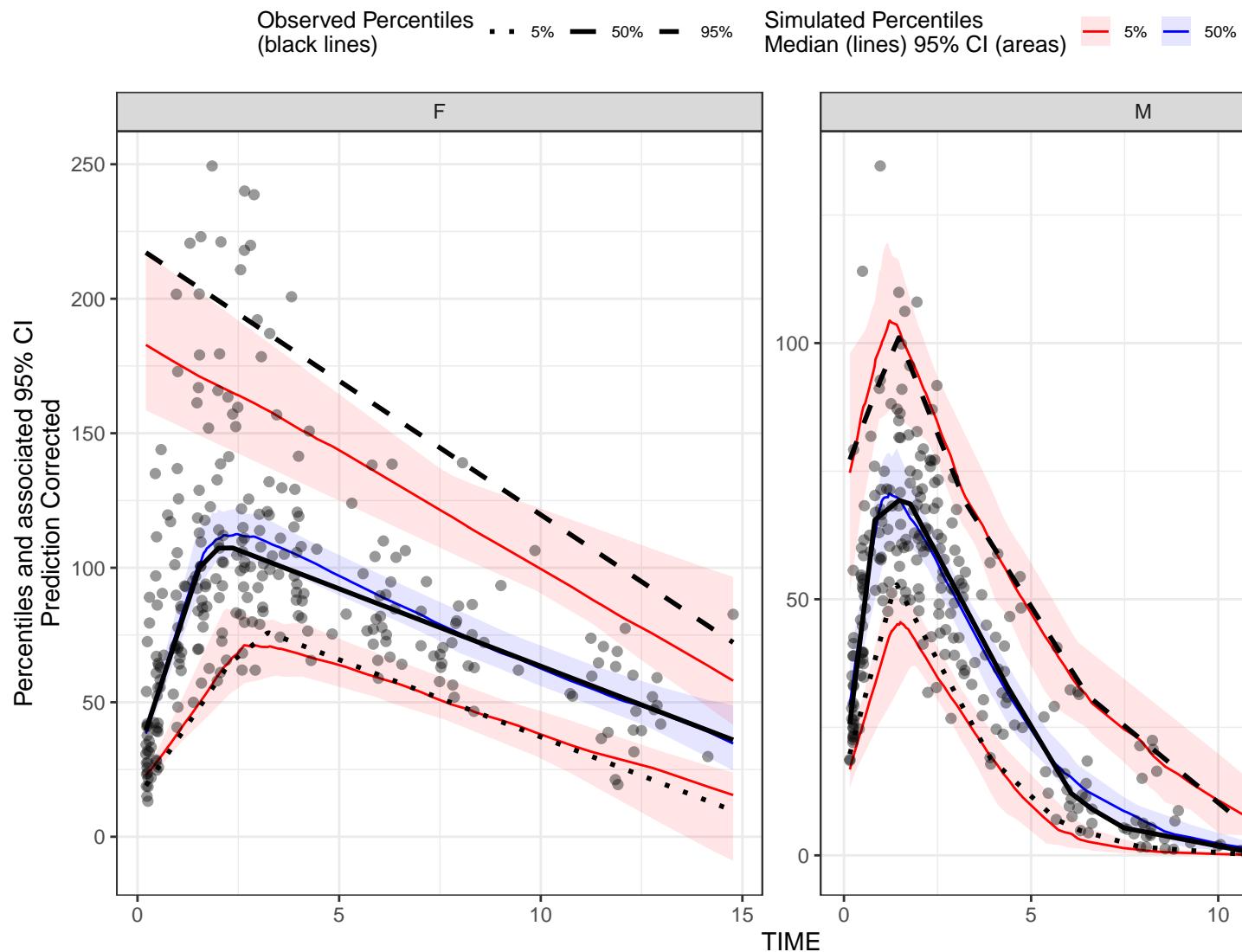
plot(vpc)
```



LOESS prediction corrected using binless method for 10%, 50%, 90% quantiles. If `optimize = TRUE`, the LOESS smoothing parameter, `span`, will be automatically optimized using AIC.

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  stratify(~GENDER) %>%
  binless(qpred = c(0.1, 0.5, 0.9), optimize = TRUE) %>%
  predcorrect(pred=PRED) %>%
  vpcstats()

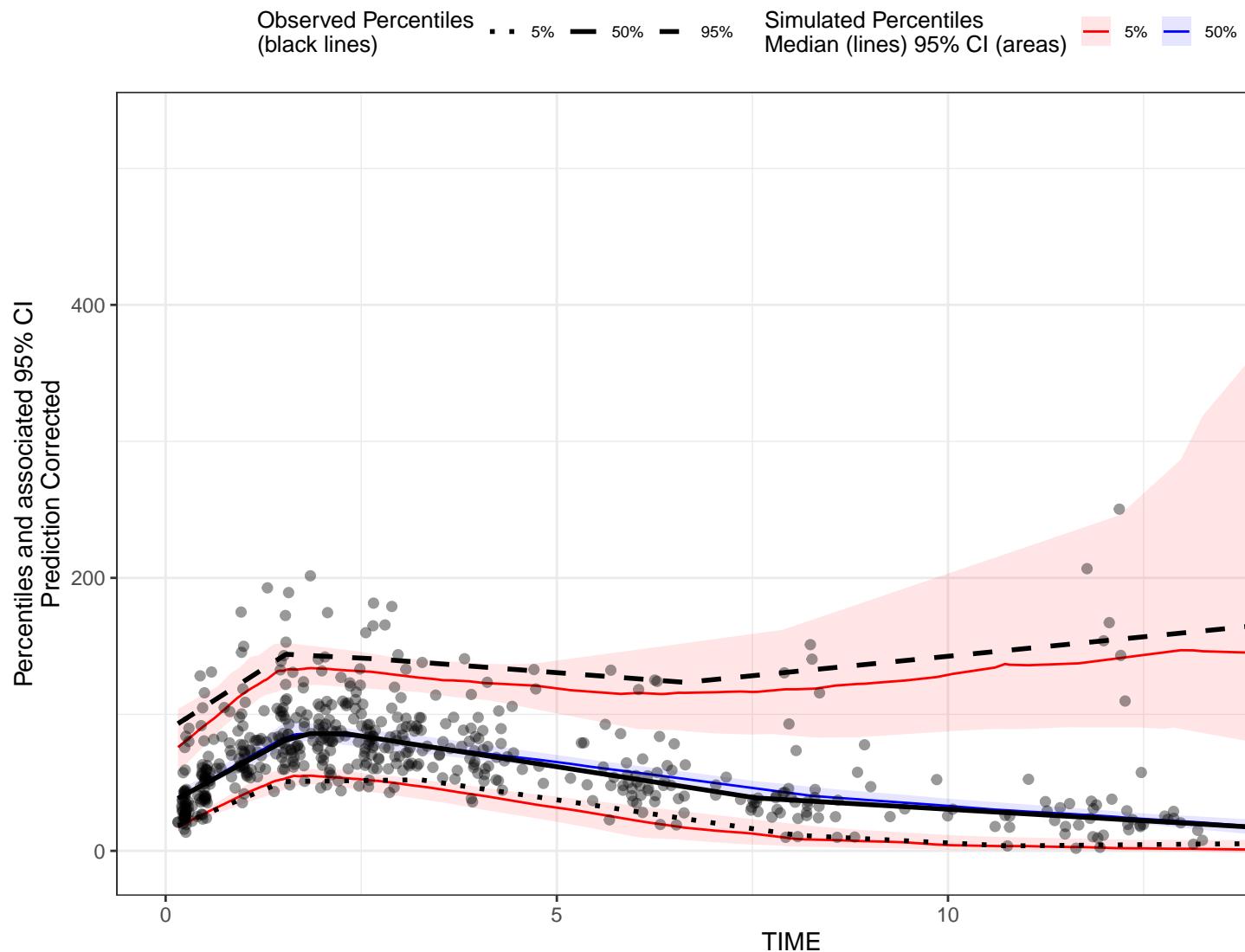
plot(vpc)
```



To specify your own smoothing value for LOESS pcVPC instead of optimizing with AIC, use the `span` argument in the `binless()` function. The `span` argument is a numeric value between [0,1], with higher values providing a smoother fit. Remember, to also include the smoothing parameters for AQR by using the `lambda` argument and set `optimize = FALSE`.

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  predcorrect(pred=PRED) %>%
  binless(optimize = FALSE, lambda = c(.95,3,1.2), span = .6) %>%
  vpcstats()

plot(vpc)
```



Extending further

Below are some examples of advanced use cases of the `tidyvpc` package.

Different binning methods by strata

To use different binning methods for different stratification variables, and/or for each level of stratification variable, use multiple calls to the `binning()` function in combination with the `stratum` argument. Make sure to set `by.strata = T`

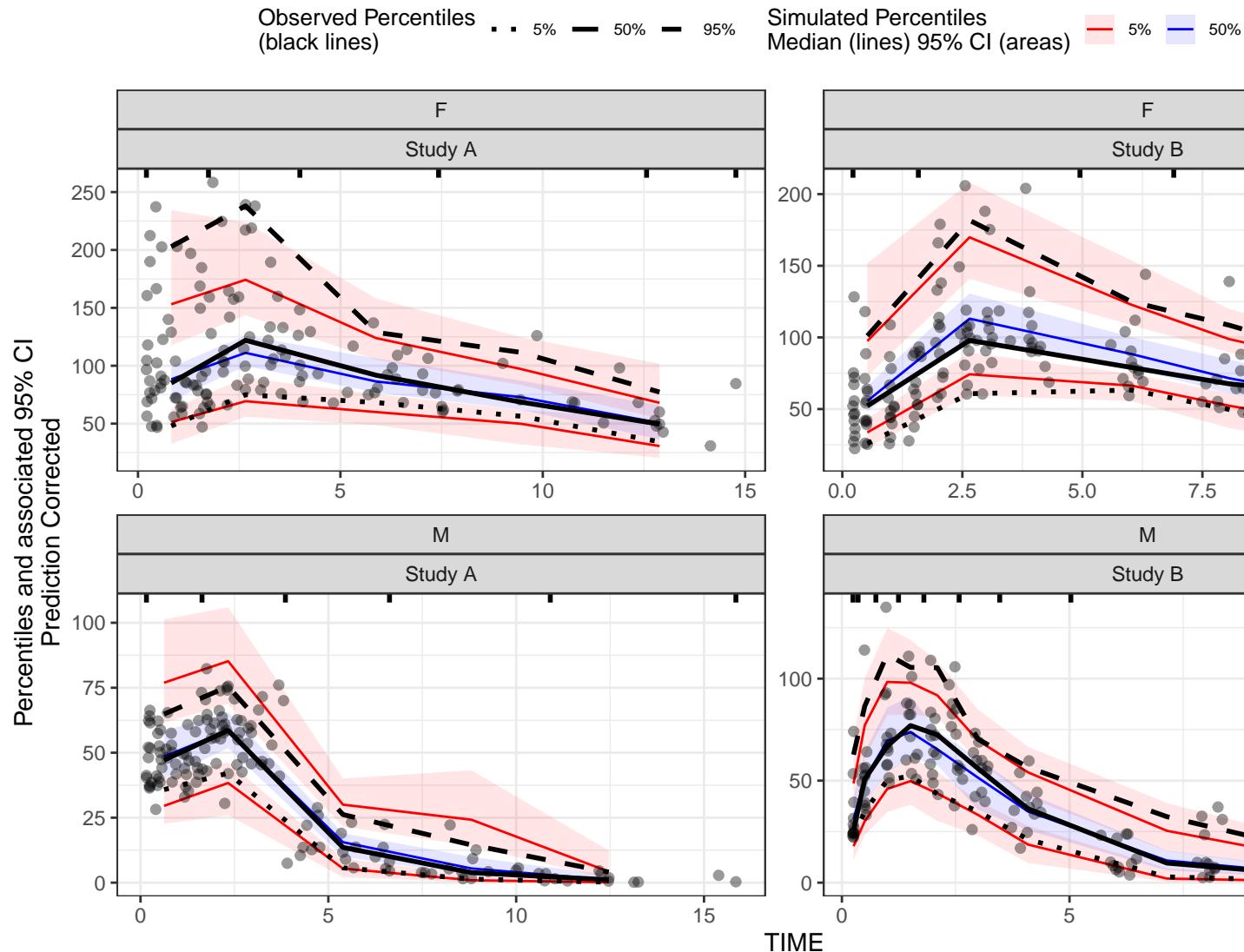
```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  stratify(~ GENDER + STUDY) %>%
  binning(stratum = list(GENDER = "M", STUDY = "Study A"), bin = "jenks", nbins = 5, by.strata = T) %>%
  binning(stratum = list(GENDER = "F", STUDY = "Study A"), bin = "centers", centers = c(0.5,3,5,10,15))
```

```

binning(stratum = list(GENDER = "M", STUDY = "Study B"), bin = "kmeans", by.strata = T) %>%
binning(stratum = list(GENDER = "F", STUDY = "Study B"), bin = "pam", nbins = 5, by.strata = T) %>%
predcorrect(pred=PRED) %>%
vpcstats()

plot(vpc)

```



Different smoothing values for each level of stratification variable

To use different smoothing parameters for each level of stratification variable if using the `binless()` function, use a single call of the `binless()` function and include a `data.frame` with the column names of stratification variable and corresponding level. To use different `span` values for each level of stratification variable, use a vector the length of n levels of strata. Note: If using more than one stratification variable with the `binless()` function, you must set `optimize = TRUE` and optimize lambda and span using AIC.

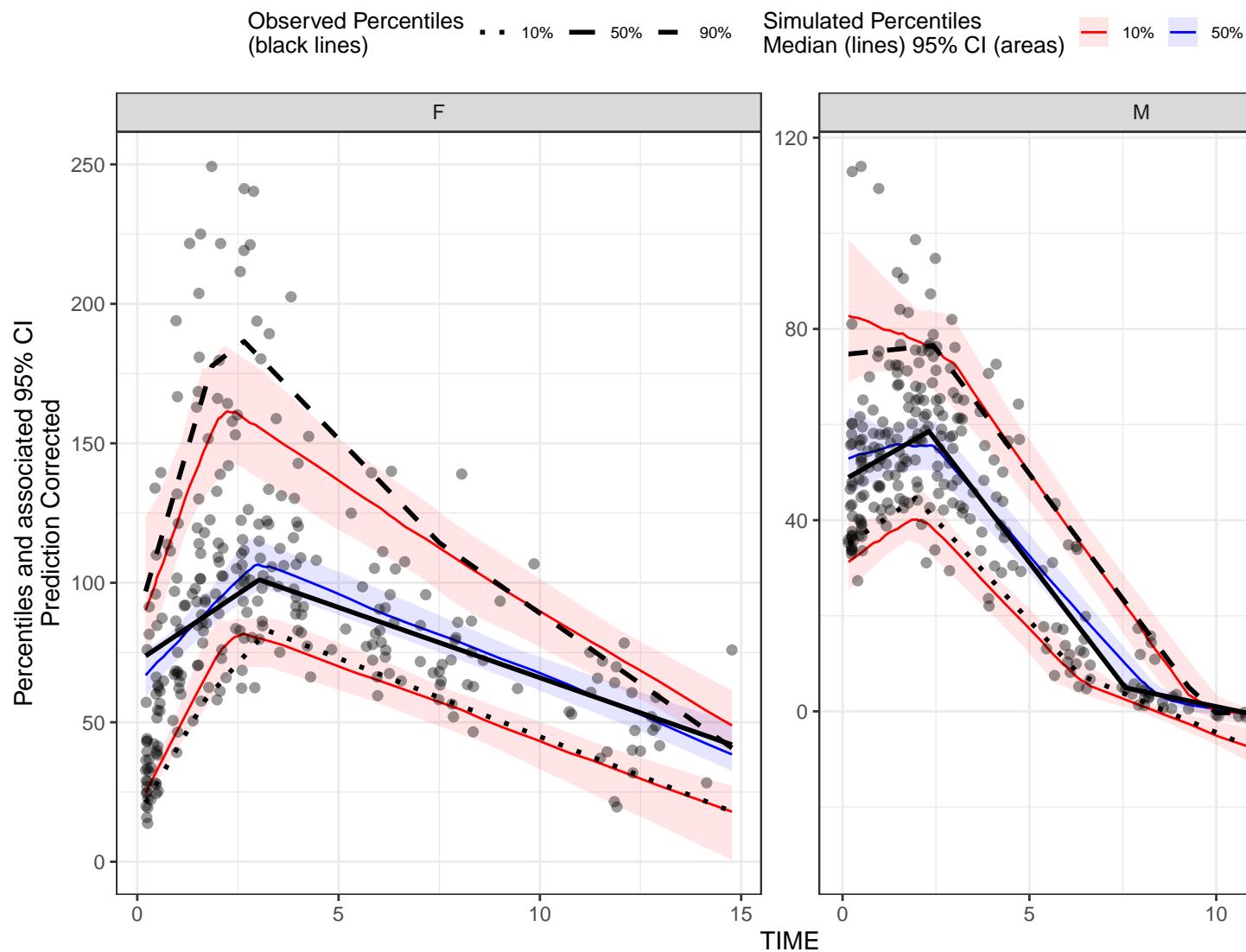
```

user_lambda <- data.frame(GENDER_F = c(2, 4, 2), GENDER_M = c(1.9, 3, 2.25) )

vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  stratify(~ GENDER) %>%
  binless(optimize = FALSE, lambda = user_lambda, span = c(.6, .85)) %>%
  predcorrect(pred=PRED) %>%
  vpcstats(qpred = c(0.1, 0.5, 0.9))

plot(vpc)

```

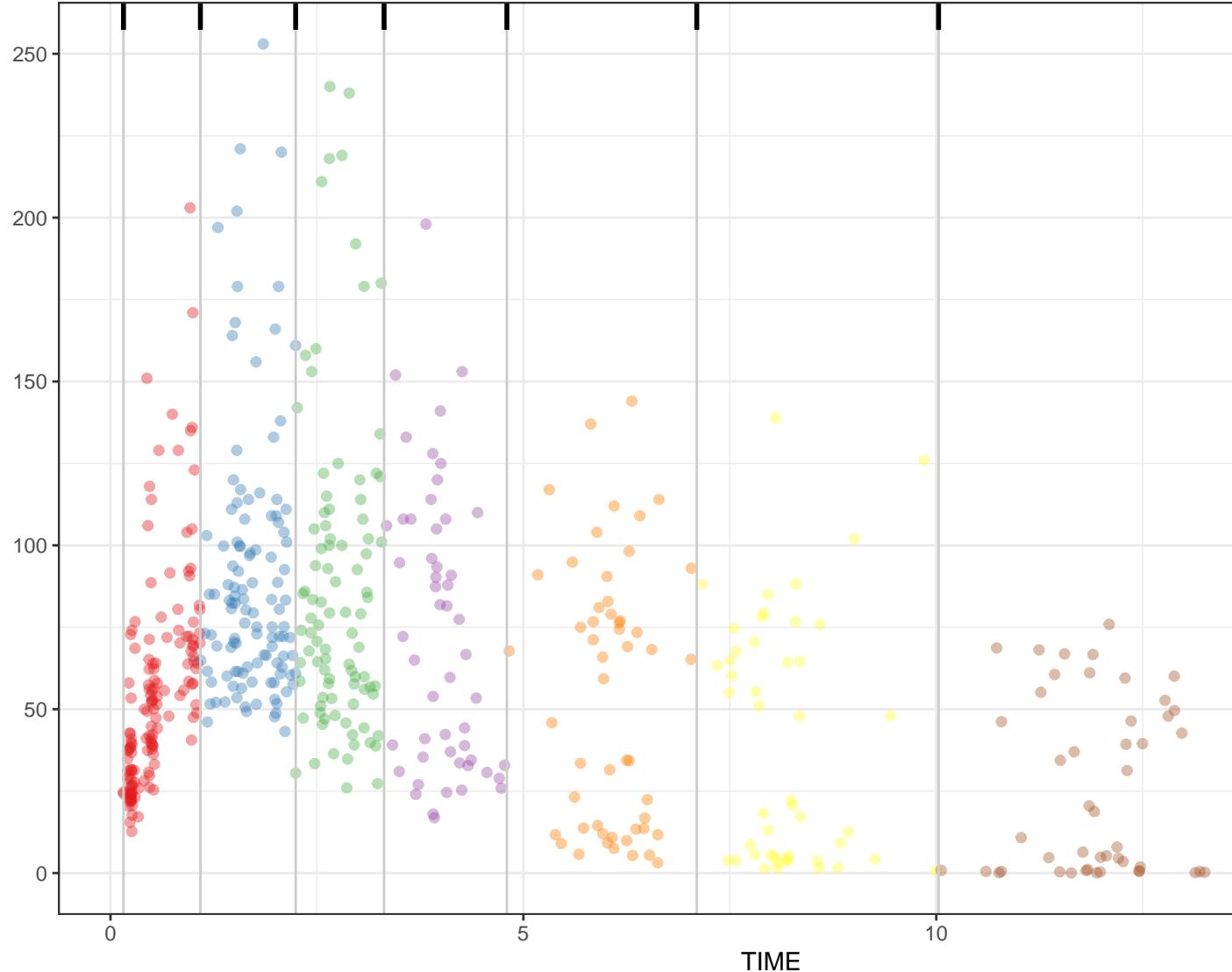


Visualize bins

If using `binning()` methods, you can visualize bins by using the `plot()` function on the `tidyvpcobj` without calling `vpcstats()`. Once you are satisfied with the binning method, simply call `vpcstats()` on the existing `tidyvpcobj` to compute VPC percentiles and prediction intervals (e.g., `vpc %>% vpcstats()`).

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  binning(bin = "jenks", nbins = 7)

plot(vpc)
```



Obtain bin information

To obtain information about the bins, including the number of observations, xmedian, xmean, xmin, xmax, xmidpoint, xleft, xright, and xceter, use the `bininfo()` function from `tidyvpc`.

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  binning(bin = "jenks", nbins = 4) %>%
  vpcstats()
```

```

bin_information <- bininfo(vpc)
head(bin_information)
#>      bin nobs   xmedian     xmean     xmin     xmax     xmid   xleft   xright xcent
#> 1: [0.158,1.89)  213  0.8418133  0.8717959 0.1575342  1.860852  1.009193 0.1575342  1.872980  1.0152
#> 2: [1.89,4.83)   187  2.8021930  2.9458444 1.8851078  4.772347  3.328727 1.8729798  4.800346  3.3366
#> 3: [4.83,9.45)    96  6.6279698  6.9869973 4.8283449  9.259398  7.043872 4.8003458  9.353216  7.0767
#> 4: [9.45,15.8]    54 11.9639045 12.0388598 9.4470340 15.848161 12.647597 9.3532162 15.848161 12.6006

```

Using ggplot2 with tidyvpc

While the built-in `plot()` function make it easy to quickly visualize the derived VPC, the `tidyvpcobj` can be plotted using `ggplot2` for complete plot customization.

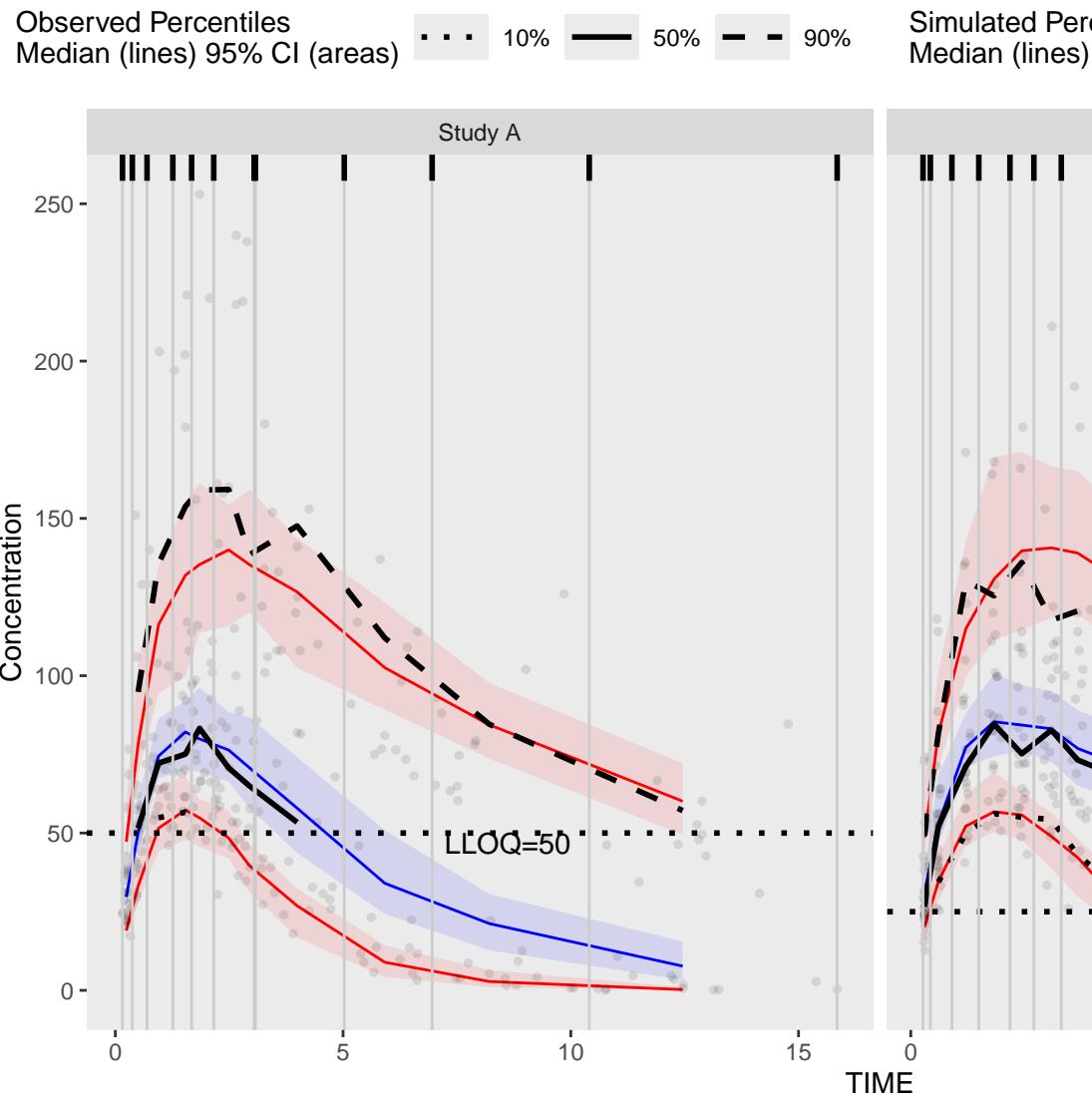
```

library(ggplot2)
obs_data$LLOQ <- obs_data[, ifelse(STUDY == "Study A", 50, 25)]

vpc <- observed(obs_data, x = TIME, y = DV) %>%
  simulated(sim_data, y = DV) %>%
  censoring(blq = DV < LLOQ, lloq = LLOQ) %>%
  stratify(~STUDY) %>%
  binning(bin = NTIME) %>%
  vpcstats(qpred = c(0.1, 0.5, 0.9))

ggplot(vpc$stats, aes(x = xbin)) +
  facet_grid(~STUDY, scales = "free", as.table = FALSE) +
  geom_ribbon(aes(ymin = lo, ymax = hi, fill = qname, col = qname, group = qname), alpha = 0.1, col = NA) +
  geom_line(aes(y = md, col = qname, group = qname)) +
  geom_line(aes(y = y, linetype = qname), size = 1) +
  geom_hline(data = unique(obs_data[, .(STUDY, LLOQ)]), aes(yintercept = LLOQ), linetype = "dotted", size = 1) +
  geom_text(data = unique(vpc$data[, .(LLOQ)], by = "STUDY")),
  aes(x = 10, y = LLOQ, label = paste("LLOQ", LLOQ, sep = "=")), vjust = 1, hjust = 1) +
  scale_colour_manual(name = "Simulated Percentiles\nMedian (lines) 95% CI (areas)",
    breaks = c("q0.1", "q0.5", "q0.9"),
    values = c("red", "blue", "red"),
    labels = c("10%", "50%", "90%")) +
  scale_fill_manual(name = "Simulated Percentiles\nMedian (lines) 95% CI (areas)",
    breaks = c("q0.1", "q0.5", "q0.9"),
    values = c("red", "blue", "red"),
    labels = c("10%", "50%", "90%")) +
  scale_linetype_manual(name = "Observed Percentiles\nMedian (lines) 95% CI (areas)",
    breaks = c("q0.1", "q0.5", "q0.9"),
    values = c("dotted", "solid", "dashed"),
    labels = c("10%", "50%", "90%")) +
  guides(fill = guide_legend(order = 2), colour = guide_legend(order = 2), linetype = guide_legend(order = 2)) +
  theme(panel.grid = element_blank()) +
  geom_rug(data = bininfo(vpc)[, .(x = sort(unique(c(xleft, xright))))], by = names(vpc$strat)], aes(x = :

```



Plot VPC with ggplot2

Plot rectangles using bininfo() The results from `bininfo()` make it easy to plot a rectangle VPC using `ggplot2`.

```
vpc <- observed(obs_data, x=TIME, y=DV) %>%
  simulated(sim_data, y=DV) %>%
  binning(bin = "jenks", nbins = 4) %>%
  vpcstats()

#Get vpcstats df
stats <- vpc$stats
#Get bininfo df
bin_information <- bininfo(vpc)
#Left join bin_info to vpcstats on bin
bin_information <- stats[bin_information, on = "bin"]
#Generate ymin
bin_information <- bin_information[, ymin := min(y), by = "bin"]
```

```

#Generate ymax
bin_information <- bin_information[, ymax := max(y), by = "bin"]
head(bin_information)
#>      bin     xbin qname     y      lo      md      hi nobs xmedian xmean      xm
#> 1: [0.158,1.89) 0.8418133 q0.05 22.94 19.58905 22.7307 27.73307 213 0.8418133 0.8717959 0.15753
#> 2: [0.158,1.89) 0.8418133 q0.5 61.50 57.45770 61.7670 67.05757 213 0.8418133 0.8717959 0.15753
#> 3: [0.158,1.89) 0.8418133 q0.95 144.40 121.90995 132.7460 149.47290 213 0.8418133 0.8717959 0.15753
#> 4: [1.89,4.83) 2.8021930 q0.05 29.38 21.34827 28.0135 32.11742 187 2.8021930 2.9458444 1.88510
#> 5: [1.89,4.83) 2.8021930 q0.5 74.10 70.76337 76.1745 82.59877 187 2.8021930 2.9458444 1.88510
#> 6: [1.89,4.83) 2.8021930 q0.95 179.00 141.91740 157.6140 181.46822 187 2.8021930 2.9458444 1.88510
#>      xmid    xleft    xright xcenter ymin   ymax
#> 1: 1.009193 0.1575342 1.872980 1.015257 22.94 144.4
#> 2: 1.009193 0.1575342 1.872980 1.015257 22.94 144.4
#> 3: 1.009193 0.1575342 1.872980 1.015257 22.94 144.4
#> 4: 3.328727 1.8729798 4.800346 3.336663 29.38 179.0
#> 5: 3.328727 1.8729798 4.800346 3.336663 29.38 179.0
#> 6: 3.328727 1.8729798 4.800346 3.336663 29.38 179.0

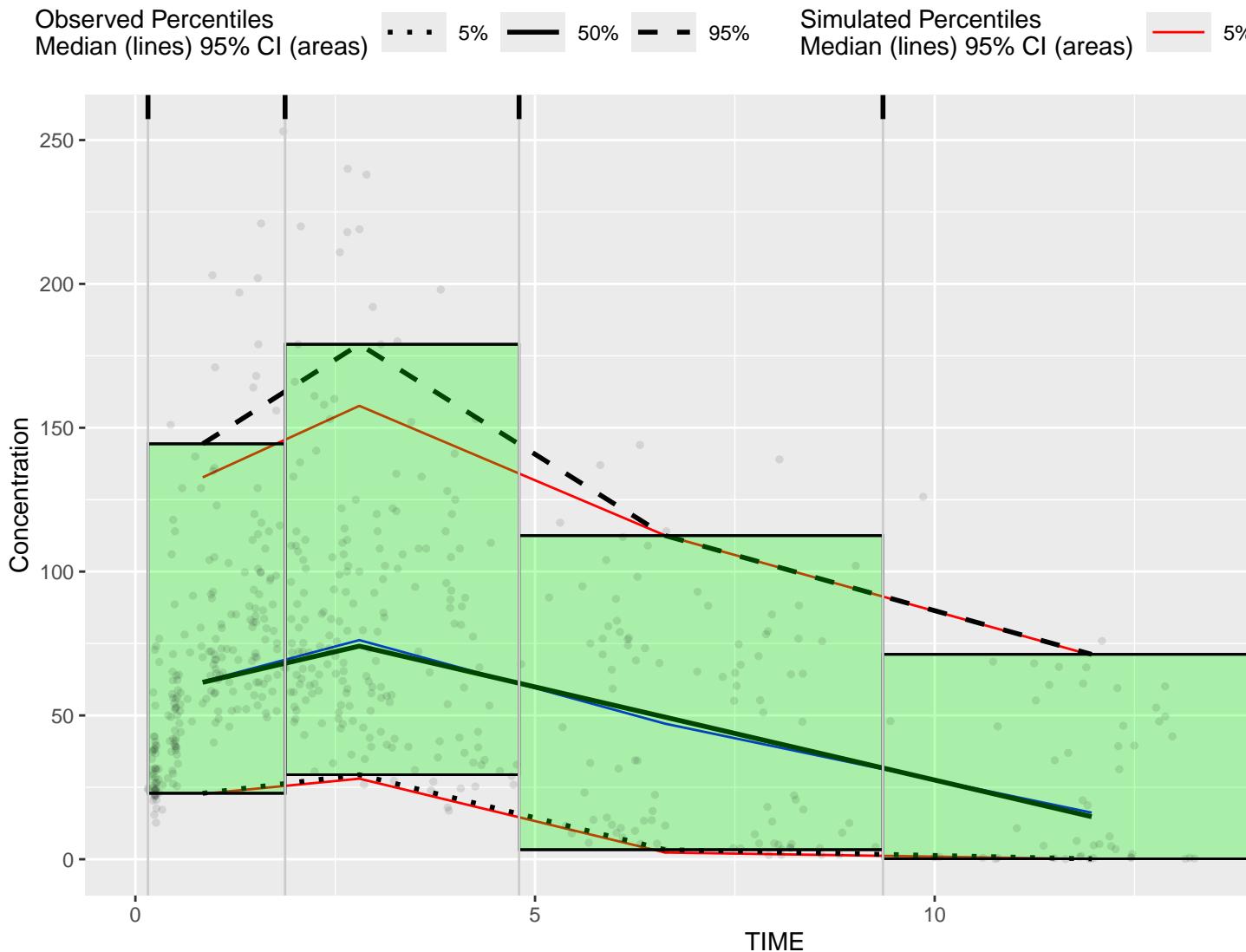
```

Plot rectangles using ymin and ymax, the min/max y values in vpc\$stats grouped by bin.

```

ggplot(bin_information, aes(x = xbin)) +
  geom_line(aes(y = md, col = qname, group = qname)) +
  geom_line(aes(y = y, linetype = qname), size = 1) +
  geom_rect(aes(xmin= xleft,xmax= xright, ymin = ymin, ymax = ymax),alpha = .1, col = "black", fill =
  geom_point(data = vpc$obs, aes(x = x, y = y), size = 1, alpha = 0.1, show.legend = FALSE) +
  scale_colour_manual(name = "Simulated Percentiles\nMedian (lines) 95% CI (areas)",
                      breaks = c("q0.05", "q0.5", "q0.95"),
                      values = c("red", "blue", "red"),
                      labels = c("5%", "50%", "95%")) +
  scale_linetype_manual(name = "Observed Percentiles\nMedian (lines) 95% CI (areas)",
                        breaks = c("q0.05", "q0.5", "q0.95"),
                        values = c("dotted", "solid", "dashed"),
                        labels = c("5%", "50%", "95%")) +
  geom_vline(data = bin_information[,.x = sort(unique(c(xleft, xright)))],aes(xintercept = x), size =
  geom_rug(data = bin_information[,.x = sort(unique(c(xleft, xright)))],aes(x = x), sides = "t", size =
  guides(fill = guide_legend(order = 2), colour = guide_legend(order = 2), linetype = guide_legend(order =
  theme(legend.position = "top", legend.key.width = grid::unit(1, "cm")) +
  labs(x = "TIME", y = "Concentration")

```



Alternatively, we can obtain the required data for plotting used in the above `bin_info` data frame by merging `vpc$stats` and `bininfo(vpc)` on `bin` in the `ggplot2` data argument. If stratifying, you will need to include the name of the stratification variable(s) in the `data.table` merge (e.g., `vpc$stats[bininfo(vpc), on=c("STUDY", "bin")]`). In the rectangle VPC below, we will stratify on `STUDY` and plot rectangles for each quantile.

```

obs_data$LLOQ <- obs_data[, ifelse(STUDY == "Study A", 50, 25)]

vpc <- observed(obs_data, x = TIME, y = DV) %>%
  simulated(sim_data, y = DV) %>%
  censoring(blq = DV < LLOQ, lloq = LLOQ) %>%
  stratify(~STUDY) %>%
  binning(bin = NTIME) %>%
  vpcstats(qpred = c(0.1, 0.5, 0.9))

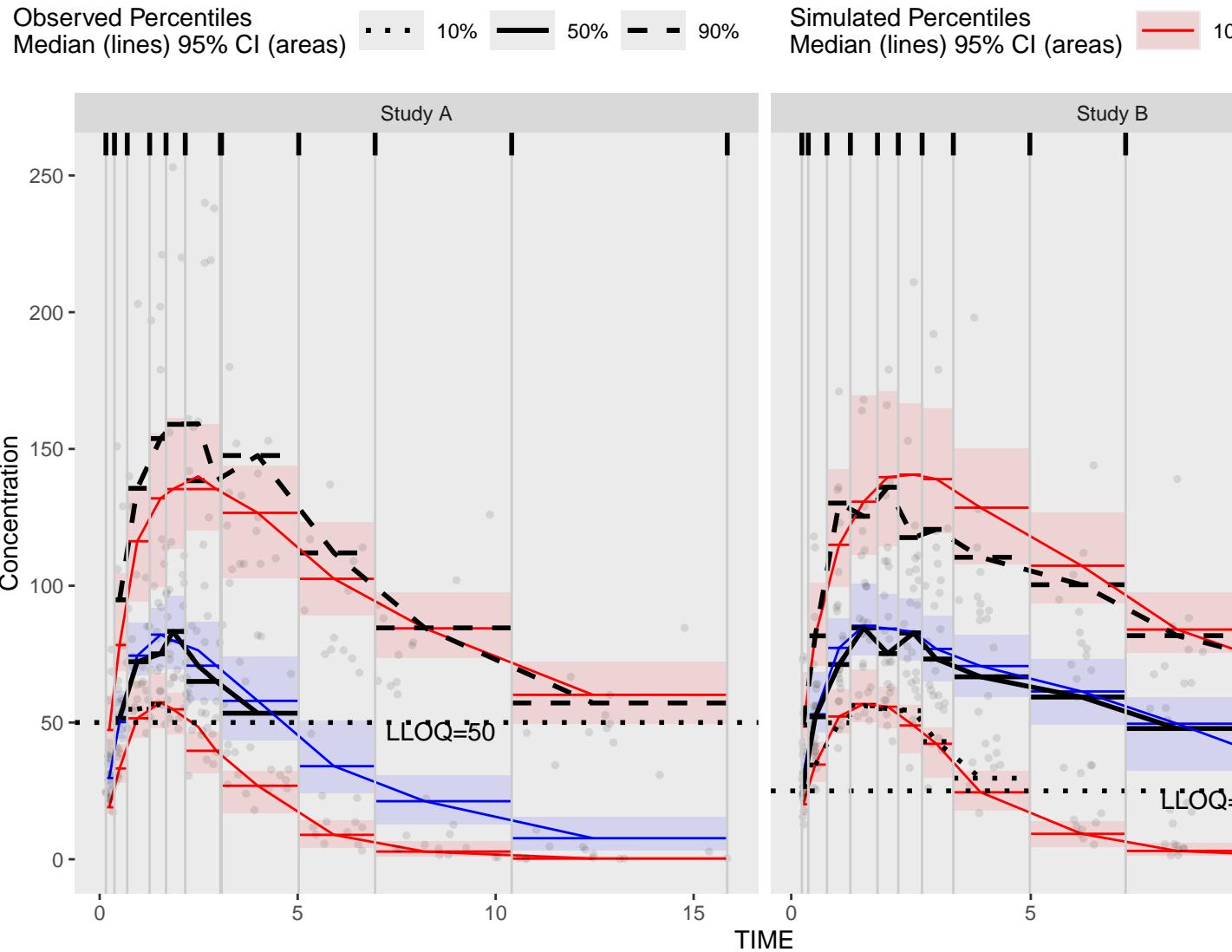
ggplot(vpc$stats[bininfo(vpc), on=c("STUDY", "bin")], aes(x = xbin)) +
  facet_grid(~STUDY, scales = "free", as.table = FALSE) +

```

```

geom_rect(aes(xmin = xleft, xmax = xright, ymin = lo, ymax = hi, fill = qname, col = qname, group = qname) +
  geom_segment(aes(x = xleft, xend = xright, y = md, yend = md, col = qname, group = qname)) +
  geom_segment(aes(x = xleft, xend = xright, y = y, yend = y, linetype = qname), size = 1) +
  geom_line(aes(y = md, col = qname, group = qname)) +
  geom_line(aes(y = y, linetype = qname), size = 1) +
  geom_hline(data=unique(obs_data[, .(STUDY, LLOQ)]), aes(yintercept=LLOQ), linetype="dotted", size=1) +
  geom_text(data = unique(vpc$data[, .(LLOQ)], by = "STUDY"]),
    aes(x = 10, y = LLOQ, label = paste("LLOQ", LLOQ, sep = "=")), vjust = 1, hjust = 1) +
  scale_colour_manual(name = "Simulated Percentiles\nMedian (lines) 95% CI (areas)",
    breaks = c("q0.1", "q0.5", "q0.9"),
    values = c("red", "blue", "red"),
    labels = c("10%", "50%", "90%")) +
  scale_fill_manual(name = "Simulated Percentiles\nMedian (lines) 95% CI (areas)",
    breaks = c("q0.1", "q0.5", "q0.9"),
    values = c("red", "blue", "red"),
    labels = c("10%", "50%", "90%")) +
  scale_linetype_manual(name = "Observed Percentiles\nMedian (lines) 95% CI (areas)",
    breaks = c("q0.1", "q0.5", "q0.9"),
    values = c("dotted", "solid", "dashed"),
    labels = c("10%", "50%", "90%")) +
guides(fill = guide_legend(order = 2), colour = guide_legend(order = 2), linetype = guide_legend(order = 2)) +
theme(legend.position = "top", legend.key.width = grid::unit(1, "cm")) +
labs(x = "TIME", y = "Concentration") +
geom_point(data = vpc$obs, aes(x = x, y = y), size = 1, alpha = 0.1, show.legend = FALSE) +
geom_vline(data = bininfo(vpc)[, .(x = sort(unique(c(xleft, xright))))], by = names(vpc$strat)], aes(x = x)) +
theme(panel.grid = element_blank()) +
geom_rug(data = bininfo(vpc)[, .(x = sort(unique(c(xleft, xright))))], by = names(vpc$strat)], aes(x = x)) +
#> Warning: Removed 18 rows containing missing values or values outside the scale range (`geom_segment()`) .
#> Warning: Removed 8 rows containing missing values or values outside the scale range (`geom_line()`) .

```



Plot Below Quantification Limit (BQL) If using the `censoring()` function, the resulting `tidyvpcobj` will also contain a `pcttblq` table. Use `ggplot2` to plot the percentage of data below the limit of quantification across bins.

We can include `geom_ribbon()` using the `lo` and `hi` columns in the `vpc$pcttblq` table to denote the lower/upper bounds of our confidence interval. Let's also plot the median %blq of the simulated data using the `md` column in the `vpc$pcttblq` table.

```
obs_data$LLOQ <- obs_data[, ifelse(STUDY == "Study A", 50, 25)]  
  
vpc <- observed(obs_data, x = TIME, y = DV) %>%  
  simulated(sim_data, y = DV) %>%  
  censoring(blq = DV < LLOQ, lloq = LLOQ) %>%  
  stratify(~STUDY) %>%  
  binning(bin = NTIME) %>%  
  vpcstats(qpred = c(0.1, 0.5, 0.9))
```

```

ggplot(vpc$pctblk) +
  facet_grid(~STUDY) +
  geom_ribbon(aes(x = xbin, ymin= lo, ymax = hi), fill = "red", alpha = .2) +
  geom_line(aes(x = xbin, y = y)) +
  geom_line(aes(x = xbin, y = md), color = "red") +
  labs(x= "TIME", y= "% BLQ")

```

